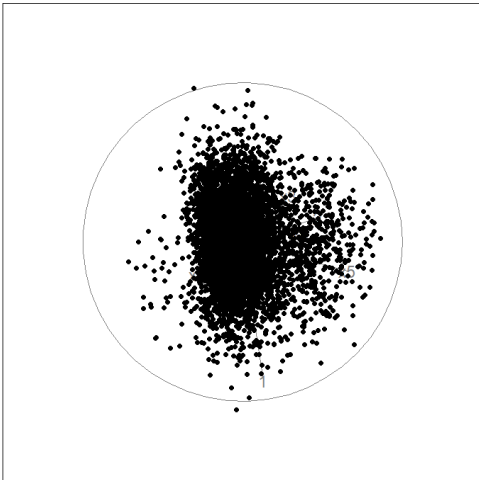
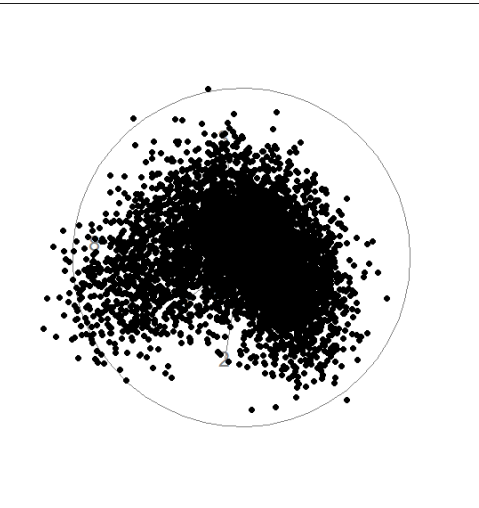


ANIMATE MYSTERY9, INTERESTING PLOTS:

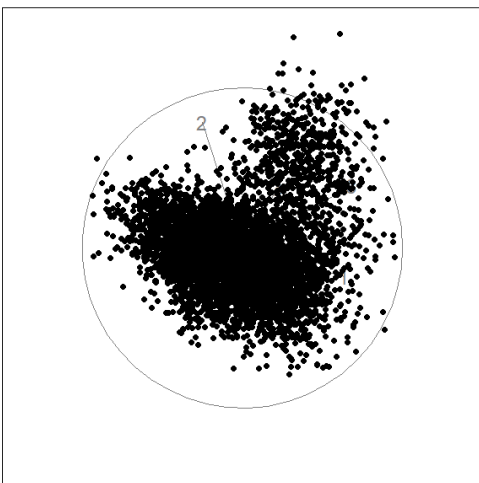


Plot appears squished/narrow, like an oval rather than circular (unlike usual)

Mostly condensed except for the less populated group (coming off the “oval”) on the right



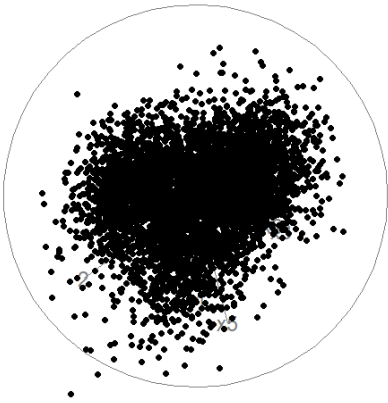
**Plot takes a shape similar to a heart or butterfly
One side (left) is less populated/filled in than the other**



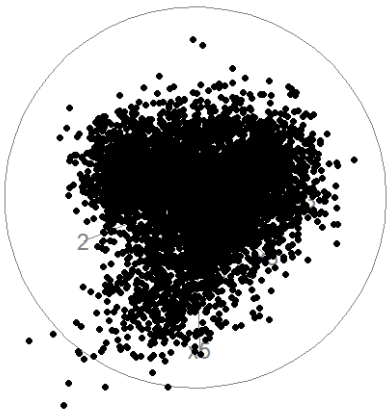
**Similar to plot above, except rotated
Right side is also less dense than the left**

ANIMATE MYSTERY2, INTERESTING PLOTS:

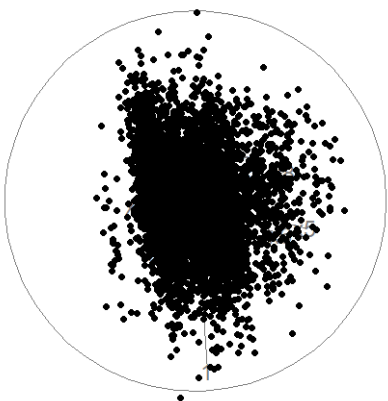
Plot appears triangular, rather than circular

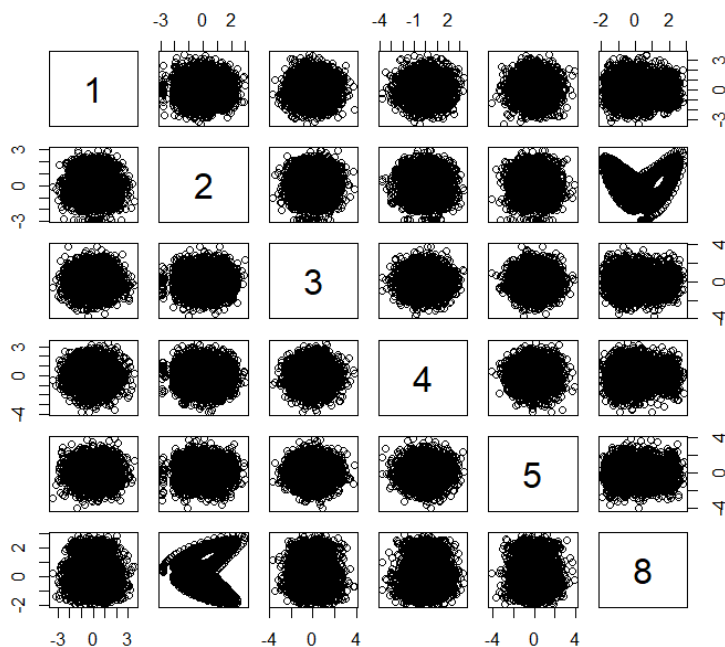


Similar to above plot except there appears to be a dip in the plot's left side, making it more similar to the heart/butterfly shape seen with `animate(mystery9)`



Plot is narrow and almost has straight sides, to the point of being rectangular
Mostly condensed except for the less populated area (coming off the "rectangle") on the right, similar to the first plot screenshotted for `animate(mystery9)`



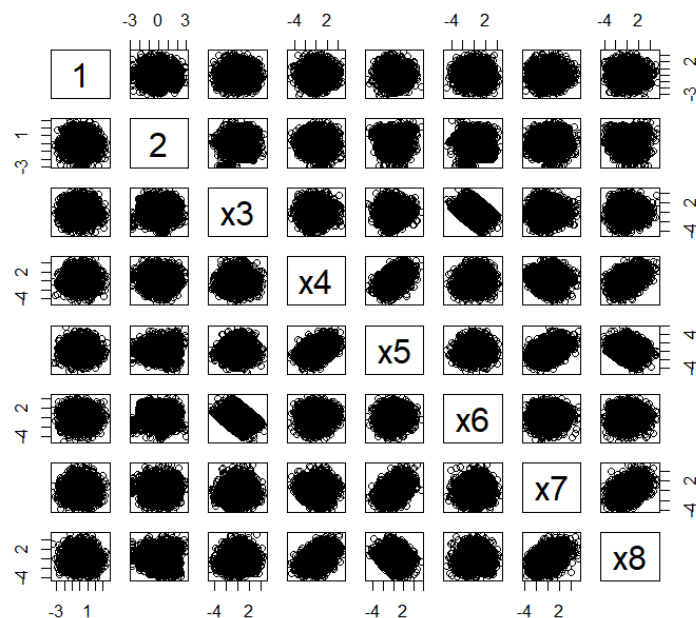


PAIRS MYSTERY9:

interesting plots: (2, 6), (6, 2)

Plots are shaped like butterflies

Note: we describe the butterfly effect at the end of page 2



PAIRS MYSTERY2:

interesting plots: (3, 6), (6, 3)

Plots appear rectangular, unlike the more circular plots surrounding them
(8, 5) and (5, 8) are also vaguely rectangular, although their sides appear less straight/defined

If we look at the mystery9 pairs graphs, we notice that two of the graphs follow butterfly effect trends. The butterfly effect, as mentioned above in the document, is when an action occurs and a rapid process of larger and larger actions happen because of it. This is not visible in the mystery2 pairs data as that has a lot more noise, so it's harder to see definitive shapes.

MVNTEST ON MYSTERY2 DATA

```
> Multivariate.normal.test(mystery2, 35)
```

```
$Interesting.directions
```

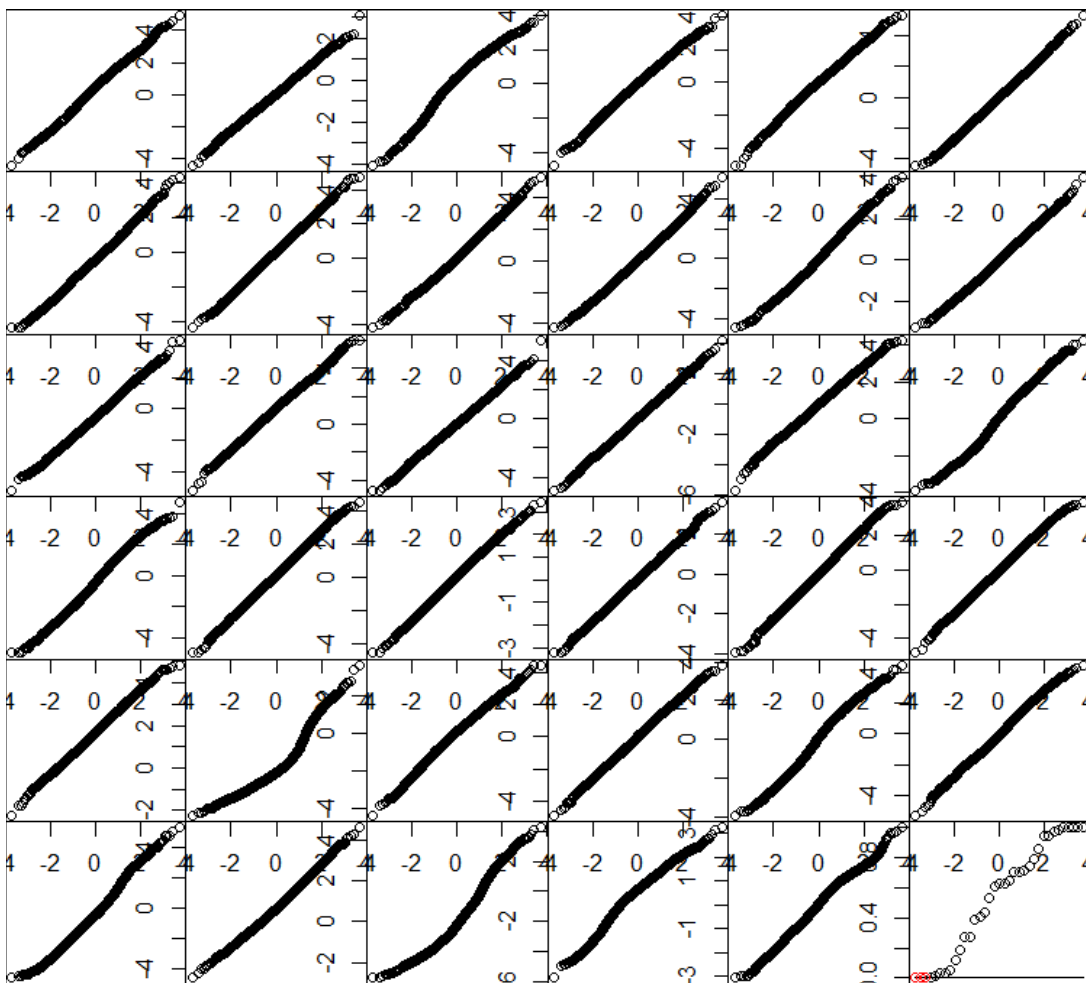
```
      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]
u1 -0.1278779  0.3991551  0.17085251 -0.1549844  0.46399746 -0.20386283 -0.18828536
u1  0.1050744  0.1236882  0.27363828 -0.1866246  0.58775779 -0.08583574  0.04233545
u1  0.3385767 -0.5628584 -0.07990759  0.5525457  0.05927245 -0.05570119  0.48393710
      [,8]
u1 0.6919585
u1 0.7136769
u1 0.1267016
```

```
$rejectingplots
```

```
[1] 26 33 31
```

```
$pvals
```

```
[1] 0.9975 0.1904 1.0000 0.9460 0.9815 0.6465 0.3910 0.6996 0.1212 0.6239 0.0291
[12] 0.6033 0.0482 0.9414 0.7174 0.5333 0.7413 0.9711 0.2706 0.0345 0.7932 0.4112
[23] 0.2753 0.6278 0.4339 0.0000 0.9999 0.7028 0.9985 0.0128 0.0001 0.0016 0.0000
[34] 1.0000 0.8558
```



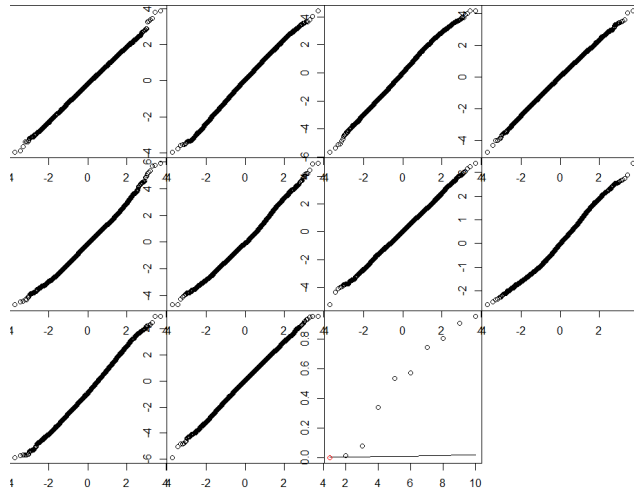
```

> gui.mvntest()
[1] "mystery2" "10"      ".05"
$Interesting.directions
[1] 0.10005193 -0.17899805 -0.03051417 0.20663077 0.30326321
[6] -0.29337609 0.85538098 -0.06787637

$rejectingplots
[1] 6

$spvals
[1] 0.8035 0.9059 0.5353 0.9529 0.5708 0.0000 0.3370 0.0799 0.0122 0.7446

```



Similar plots of a line going from bottom left to top right; while the line is fairly straight, some of the plots have a dip in the lower half or a bump in the upper half/middle

INTERESTING DIRECTION MATRIX (directions taken from mvntest)

```

directions = c(0.10005193, -0.17899805, -0.03051417, 0.20663077, 0.30326321,
-0.29337609, 0.85538098, -0.06787637)
directions = c(directions, as.matrix(c(-0.1278779, 0.3991551, 0.17085251, -0.1549844,
0.46399746, -0.20386283, -0.18828536, 0.6919585, 0.1050744, 0.1236882, 0.27363828,
-0.1866246, 0.58775779, -0.08583574, 0.04233545, 0.7136769, 0.3385767, -0.5628584,
-0.07990759, 0.5525457, 0.05927245, -0.05570119, 0.48393710, 0.1267016)))
directions = matrix(directions, 8, 4)
directions = t(directions)
> directions
      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]
[1,] 0.1000519 -0.1789980 -0.03051417 0.2066308 0.30326321 -0.29337609
[2,] -0.1278779 0.3991551 0.17085251 -0.1549844 0.46399746 -0.20386283
[3,] 0.1050744 0.1236882 0.27363828 -0.1866246 0.58775779 -0.08583574
[4,] 0.3385767 -0.5628584 -0.07990759 0.5525457 0.05927245 -0.05570119
      [,7]      [,8]
[1,] 0.85538098 -0.06787637
[2,] -0.18828536 0.69195850
[3,] 0.04233545 0.71367690
[4,] 0.48393710 0.12670160

```

ORTHOGONALIZE MYSTERY2:

> orthogonalize(mystery2)

```
      1      2      x3      x4      x5      x6      x7
[1,] 0.4296331 -0.5149734 -0.2003239 0.1902949 -0.3204298 -0.4258319 -0.04901055
      x8
[1,] 0.4329733

      1      2      x3      x4      x5      x6
[1,] 0.4296330754 -0.51497341 -0.2003239 0.19029489 -0.3204298 -0.42583191
[2,] -0.4839322794 -0.44044313 -0.6786419 0.15551375 0.2237785 0.14420640
[3,] 0.0858550079 -0.25432661 0.2679039 0.09452947 0.5390926 -0.57515442
[4,] 0.7072496109 0.09866441 -0.2784294 0.23386000 0.2989446 0.42548588
[5,] 0.2576173879 -0.14705042 -0.1991832 -0.60898676 0.1550408 0.04379119
[6,] 0.0774206873 0.03050791 -0.1811894 0.03078715 -0.6536852 -0.10626728
[7,] -0.0359315766 0.12639694 0.0811292 0.70977787 0.0313174 0.04688244
[8,] 0.0003397716 0.65411375 -0.5205138 -0.01948482 0.1222146 -0.52021390
[9,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[10,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[11,] 0.0023221877 0.65475750 -0.5254535 -0.01781054 0.1031847 -0.52318107
[12,] 0.0023221876 0.65475750 -0.5254535 -0.01781054 0.1031847 -0.52318107
[13,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[14,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[15,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[16,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[17,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[18,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[19,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[20,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[21,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[22,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[23,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[24,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[25,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[26,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[27,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[28,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[29,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107

[30,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[31,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[32,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[33,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[34,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[35,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[36,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[37,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[38,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[39,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[40,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[41,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[42,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[43,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[44,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[45,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[46,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[47,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[48,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[49,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[50,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[51,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[52,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[53,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[54,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[55,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[56,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[57,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[58,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[59,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[60,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[61,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[62,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[63,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[64,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
[65,] -0.0023221877 -0.65475750 0.5254535 0.01781054 -0.1031847 0.52318107
```


[illegible]

[12,] -0.01568009 0.1012779
[13,] 0.01568009 -0.1012779
[14,] 0.01568009 -0.1012779
[15,] 0.01568009 -0.1012779
[16,] 0.01568009 -0.1012779
[17,] 0.01568009 -0.1012779
[18,] 0.01568009 -0.1012779
[19,] 0.01568009 -0.1012779
[20,] 0.01568009 -0.1012779
[21,] 0.01568009 -0.1012779
[22,] 0.01568009 -0.1012779
[23,] 0.01568009 -0.1012779
[24,] 0.01568009 -0.1012779
[25,] 0.01568009 -0.1012779
[26,] 0.01568009 -0.1012779
[27,] 0.01568009 -0.1012779
[28,] 0.01568009 -0.1012779
[29,] 0.01568009 -0.1012779
[30,] 0.01568009 -0.1012779
[31,] 0.01568009 -0.1012779
[32,] 0.01568009 -0.1012779
[33,] 0.01568009 -0.1012779
[34,] 0.01568009 -0.1012779
[35,] 0.01568009 -0.1012779
[36,] 0.01568009 -0.1012779
[37,] 0.01568009 -0.1012779
[38,] 0.01568009 -0.1012779
[39,] 0.01568009 -0.1012779
[40,] 0.01568009 -0.1012779
[41,] 0.01568009 -0.1012779
[42,] 0.01568009 -0.1012779
[43,] 0.01568009 -0.1012779
[44,] 0.01568009 -0.1012779
[45,] 0.01568009 -0.1012779
[46,] 0.01568009 -0.1012779
[47,] 0.01568009 -0.1012779

[84,] 0.01568009 -0.10127792
[85,] 0.01568009 -0.10127792
[86,] 0.01568009 -0.10127792
[87,] 0.01568009 -0.10127792
[88,] 0.01568009 -0.10127792
[89,] 0.01568009 -0.10127792
[90,] 0.01568009 -0.10127792
[91,] 0.01568009 -0.10127792
[92,] 0.01568009 -0.10127792
[93,] 0.01568009 -0.10127792
[94,] 0.01568009 -0.10127792
[95,] 0.01568009 -0.10127792
[96,] 0.01568009 -0.10127792
[97,] 0.01568009 -0.10127792
[98,] 0.01568009 -0.10127792
[99,] 0.01568009 -0.10127792
[100,] 0.01568009 -0.10127792
[101,] 0.01568009 -0.10127792
[102,] 0.01568009 -0.10127792
[103,] 0.01568009 -0.10127792
[104,] 0.01568009 -0.10127792
[105,] 0.01568009 -0.10127792
[106,] 0.01568009 -0.10127792
[107,] 0.01568009 -0.10127792
[108,] 0.01568009 -0.10127792
[109,] 0.01568009 -0.10127792
[110,] 0.01568009 -0.10127792
[111,] 0.01568009 -0.10127792
[112,] 0.01568009 -0.10127792
[113,] 0.01568009 -0.10127792
[114,] 0.01568009 -0.10127792
[115,] 0.01568009 -0.10127792
[116,] 0.01568009 -0.10127792
[117,] 0.01568009 -0.10127792
[118,] 0.01568009 -0.10127792
[119,] 0.01568009 -0.10127792


```
[48,] 0.01568009 -0.10127792
[49,] 0.01568009 -0.10127792
[50,] 0.01568009 -0.10127792
[51,] 0.01568009 -0.10127792
[52,] 0.01568009 -0.10127792
[53,] 0.01568009 -0.10127792
[54,] 0.01568009 -0.10127792
[55,] 0.01568009 -0.10127792
[56,] 0.01568009 -0.10127792
[57,] 0.01568009 -0.10127792
[58,] 0.01568009 -0.10127792
[59,] 0.01568009 -0.10127792
[60,] 0.01568009 -0.10127792
[61,] 0.01568009 -0.10127792
[62,] 0.01568009 -0.10127792
[63,] 0.01568009 -0.10127792
[64,] 0.01568009 -0.10127792
[65,] 0.01568009 -0.10127792
[66,] 0.01568009 -0.10127792
[67,] 0.01568009 -0.10127792
[68,] 0.01568009 -0.10127792
[69,] 0.01568009 -0.10127792
[70,] 0.01568009 -0.10127792
[71,] 0.01568009 -0.10127792
[72,] 0.01568009 -0.10127792
[73,] 0.01568009 -0.10127792
[74,] 0.01568009 -0.10127792
[75,] 0.01568009 -0.10127792
[76,] 0.01568009 -0.10127792
[77,] 0.01568009 -0.10127792
[78,] 0.01568009 -0.10127792
[79,] 0.01568009 -0.10127792
[80,] 0.01568009 -0.10127792
[81,] 0.01568009 -0.10127792
[82,] 0.01568009 -0.10127792
[83,] 0.01568009 -0.10127792

[120,] 0.01568009 -0.10127792
[121,] 0.01568009 -0.10127792
[122,] 0.01568009 -0.10127792
[123,] 0.01568009 -0.10127792
[124,] 0.01568009 -0.10127792
[125,] 0.01568009 -0.10127792
[ reached getOption("max.print") -- omitted 4876 rows ]
```

ORTHOGONALIZE DIRECTIONS MATRIX

```
> odirections = orthogonalize(directions)
```

```
      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]      [,8]  
[1,] 0.1000519 -0.178998 -0.03051417 0.2066308 0.3032632 -0.2933761 0.855381 -0.06787637
```

```
> odirections
```

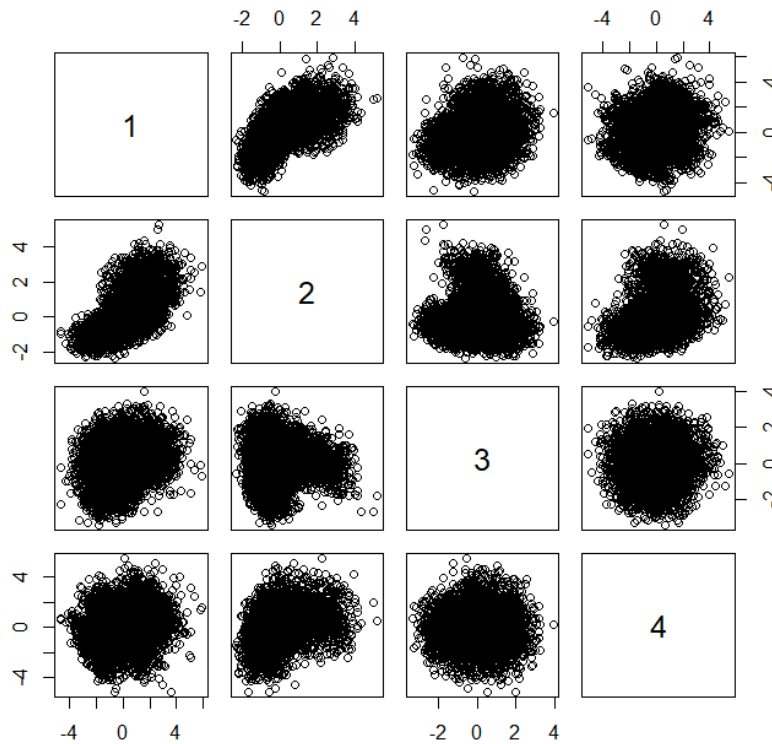
```
      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]      [,8]  
[1,] 0.1000519 -0.1789980 -0.03051417 0.2066308 0.3032632 -0.29337609 0.855380977 -0.06787637  
[2,] -0.1159415 0.3792354 0.16832275 -0.1294138 0.5073509 -0.24373901 -0.078613368 0.68895861  
[3,] 0.5103657 -0.5129479 0.32055821 -0.2478510 0.2185414 0.45324882 0.001523396 0.24295363  
[4,] 0.1308678 -0.3046210 -0.19895077 0.7600294 -0.1590077 -0.09460374 -0.210854464 0.44063659
```

EXPLORE MYSTERY2 (gui.explore()):

gui.explore pairs plot

```
> gui.explore()
```

```
[1] "odirections" "mystery2" "T" "F" "F" "c(1,2,3)"
```

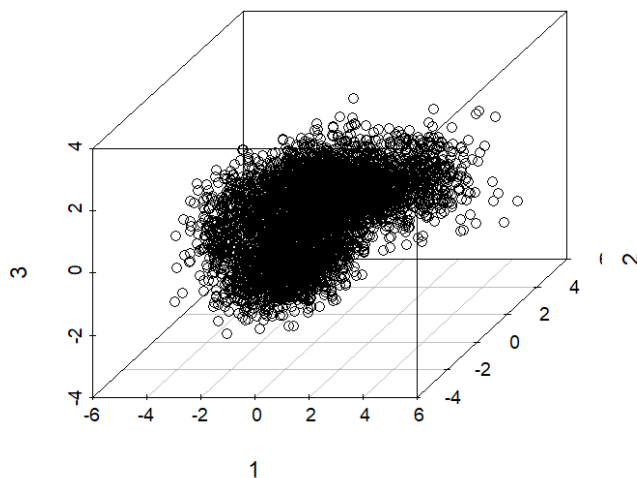


Butterfly shape is now shown, especially in (2, 3) and (3, 2), unlike with pairs(mystery2)

gui.explore 3d plot

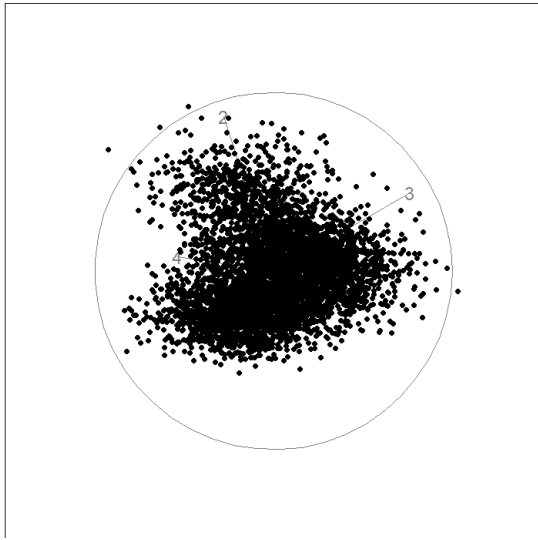
```
> gui.explore()
```

```
[1] "odirections" "mystery2" "F" "F" "T" "c(1,2,3)"
```

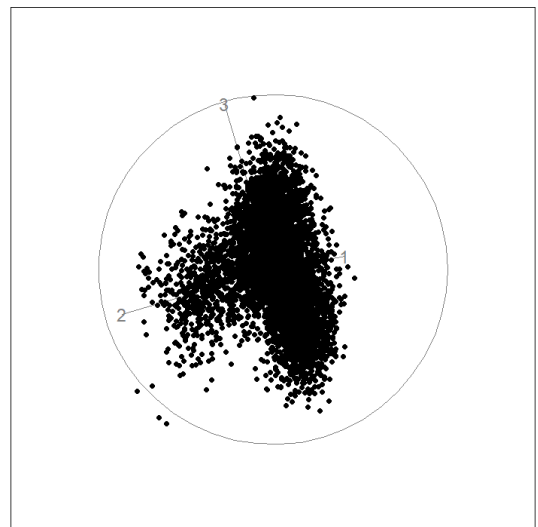
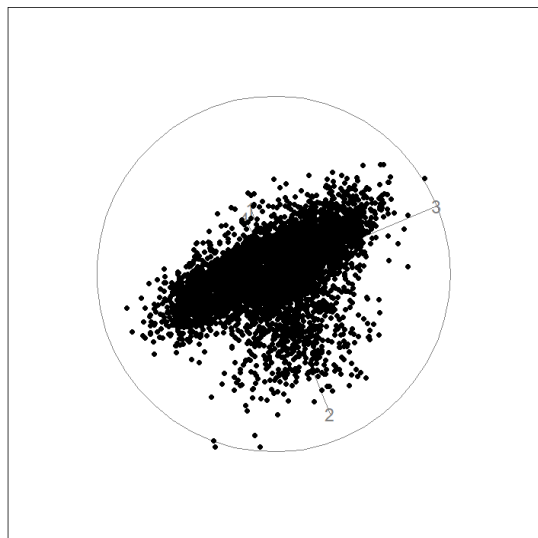


**Shape appears curved and has a dip in one side
Could be interpreted as the shape of a butterfly (dip is between two "wings")**

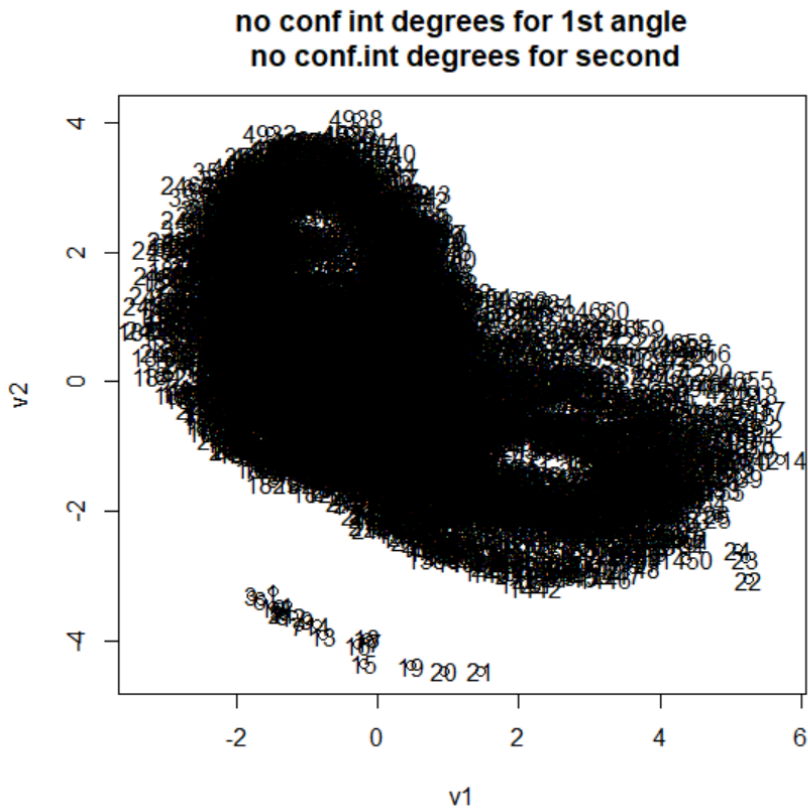
gui.explore animate: more examples of the butterfly shape



Due to the curse of dimensionality, shapes look different from different angles. As a result, without using certain directions or starting values, it could take a while for this butterfly shape to be visible (if it becomes visible at all).



ASYMMETRY TEST ON MYSTERY2 DATA:



Plot is fairly flat on the lower left, but is curved on the top and other sides, with a dip in the middle of the side going from the top left to the middle right

Shape could be compared to a B, a rabbit (rotated), etc. Regardless, it also has a vague butterfly effect shape.

```

[[1]]$new$vector1
      1      2      x3      x4      x5      x6
0.04373604 0.54356502 0.17321542 0.29052929 0.46392029 0.02872508
      x7      x8
0.41582675 0.44637913

[[1]]$new$vector2
      1      2      x3      x4      x5
0.08057901 0.65739700 0.32121212 -0.16269253 -0.36540765
      x6      x7      x8
0.40623551 -0.15250333 -0.33148577

$vector1
      1      2      x3      x4      x5
0.043221478 0.507811472 0.152560303 0.307100220 0.455034934
      x6      x7      x8
-0.006430106 0.444877254 0.466540794

$vector2
      1      2      x3      x4      x5
0.07142552 0.69790611 0.30721495 -0.14456972 -0.33414627
      x6      x7      x8

[[1]]$new[[1]]$new
[[1]]$new[[1]]$new[[1]]
[[1]]$new[[1]]$new[[1]]$1b1
[1] "no conf int"

[[1]]$new[[1]]$new[[1]]$1b2
[1] "no conf.int"

[[1]]$new[[1]]$new$vector1
      1      2      x3      x4      x5      x6
0.03131996 0.58344126 0.20061554 0.28679734 0.44700213 0.06549721
      x7      x8
0.38041211 0.43278388

[[1]]$new[[1]]$new$vector2
      1      2      x3      x4      x5
0.07615825 0.61039786 0.32154913 -0.16954084 -0.38539080
      x6      x7      x8
0.41744283 -0.19534969 -0.35851129

```