Introduction to Bayesian inference using Rstan: practical 1

The aim of this practical is to provide an introduction to the syntax and structure of the Stan programming language and to demonstrate some of the efficiency gains that can be achieved by using vectorized operations.

- 1 Getting started
- 1.1 Files in Rstudio
- Open Rstudio
- Open a new text file:

```
File -> New File -> Text File
```

and type the following Stan programme:

```
data {
   int<lower=1> N;
   real<lower=0,upper=1> p;
}
model {
}
generated quantities {
   int x[N];
   for(n in 1:N) {
      x[n] = bernoulli_rng(p);
   }
}
```

Save the text file as simulation.stan.

• Open a new R script:

```
File -> New File -> R Script
```

and type the following sequence of commands, omitting the comments if you wish:

```
## Format as vector, removing the log posterior (i.e. "__lp"):
x = out[1, -length(out)]
## Plot data:
barplot(table(x))
```

Save the R script. Note that Rstudio will correctly add the file extension .R. We can run our R script by sending the commands to the R console. For example, to send one line at a time, press Ctrl + Enter at the end of each line in turn.

1.2 Course R package

Installing the the course R package is straightforward. First install drat:

```
install.packages("drat")
Then
drat::addRepo("rcourses")
install.packages("jrRstan")
```

This R package contains copies of the practicals, solutions and data sets for the course in addition to some helpful functions that we will use. To load the package, use

```
library("jrRstan")
```

2 Simulating data

In the Stan programme above, we are not attempting to carry out any inference. Instead we're using the generated quantities block to sample some data; in this case a random sample of size 30 from the Bernoulli distribution with probability 0.8. In other words a sequence of 30 0s and 1s where the probability of getting a 1 is 0.8. When we simply want to use Stan to simulate data in this way, notice that the (required) model block is empty. We will learn about the stan function in Chapter 4, but for now, we simply note that the file argument should be the name of the text file where the Stan programme is saved and, if the programme contains a data block, the data argument should be a list with a named element for each variable declared. When it is being used to simulate data, we generally set algorithm="Fixed_param", iter=1 and chains=1.

 What happens if you try to pass a value for N or p that violates the constraints in the data block? For example, what happens if you set:

```
faulty_constants = list(N=30, p=10)
```

• Add a transformed parameter block and include a print statement to check whether the constants, N and p, have been correctly passed.

- Rather than passing the constants N and p through the data block, we can alternatively omit the data block and declare and assign values to these variables in the transformed data block. We can then omit the data argument in the call to the stan function in R. Write a new Stan programme of this form called simulation_v2.stan then compile and run the programme in R.
- In R, we can generate uniform random numbers using the runif function. For example:

```
runif(5, min=-3, max=3)
## [1] -1.59230277 -0.01920278 0.96426277 2.55942248 -2.40614843
```

Use the lookup function to find a corresponding function in Stan.

- Augment your programme simulation_v2.stan to additionally simulate 30 uniform random numbers in a vector z with lower bound -3 and upper bound 3. Call the new programme simulation_v3.stan. Compile and run it in R and check that the output looks reasonable.
- Modify simulation_v3.stan, saving the file as simulation_v4.stan, so that instead of representing x and z as separate objects, you represent them as a length-2 array of vectors called xz.
- Modify simulation_v4.stan, saving the file as simulation_v5.stan, to additionally simulate 30 normal random variables in a vector y where y[n] has mean 2.5 * x[n] + 1.5 * z[n] and standard deviation 0.1. Compile and run your Stan programme in R and check that the output looks reasonable.
- If you wanted your Stan programme to return only y and not xz how could you modify your code?

3 Vectorized operations

In this part of the practical we will investigate the efficiency gains we can realise through the vectorized operations discussed in Chapter 3.

- Copy the Stan programme from Figure 3.1 into a text file and save it as figure3_1.stan.
- Create a revised version of this programme which exploits the
 vectorization tricks described later in the Chapter. Save it as
 figure3_1_v2.stan. Note that in lectures we considered optimising only the model block. It is also possible to make the functions
 and generated quantities blocks more efficient.
- Load the data to pass to the Stan function. For convenience in this practical, the list that we will construct in Chapter 4 has been saved in a data set called practical1_data which can be loaded through:

```
## Load data to pass to stan function:
data(practical1_data)
```

We can now compile and run each programme by executing the following code:

```
## Run the programme from Figure 3.1:
fig3_1 = stan("figure3_1.stan", data=practical1_data)
## Run the revised programme:
fig3_1_v2 = stan("figure3_1_v2.stan", data=practical1_data)
```

We will consider the stan function and its usage in Chapter 4. For now, simply make a note of the time taken to run each programme. (It will be printed at the bottom of the Stan output). How much speed-up do you gain by using the revised programme?

Solutions

Solutions are available as a vignette:

```
library("jrRstan")
vignette("solutions1", package="jrRstan")
```