

- ① 1. Conducting studies and collecting data
2. Summarizing and analyzing data to extract information
3. Making decisions and reaching conclusions based on data.

- ② a) quantitative
b) categorical

c) Filter C. Amount of impurities remaining in water, for the most part, is lower than the other filters.

- ③ X = weight loss; may have a skewed-to-right distribution.



A: Sample median = 15

B: $\bar{X} = 15$

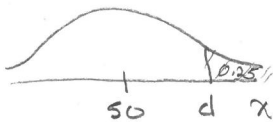
Most likely, many people lose only a few pounds and only a few people lose a lot of weight. This suggests that weight loss distribution is skewed to the right so \bar{X} is pulled to the right. Clinic A would be preferred because more people would be apt to lose a significant amount of weight.

- ④ Set 1: 9, 9, 10, 11, 11 $\bar{X} = 10, s^2 = 1$
Set 2: 7, 7, 10, 13, 13 $\bar{X} = 10, s = \sqrt{9} = 3, \text{Range} = 6$

- ⑤ X = # seeds that germinate out of n . $X \sim \text{binomial}(10, 0.8)$
 $P(X=9) = \frac{10!}{9!1!} (0.80)^9 (0.20)^1 = 10 (0.80)^9 (0.20) = 0.2684$

- ⑥ a.) X = bead diameter (cm). Assuming that $X \sim N(50, 12)$,
 $P(X \leq 44) = \text{pnorm}(44, 50, 12) = 0.3085$

b.)



Find X such that $P(X \leq x) = 0.75$
 $\text{qnorm}(0.75, 50, 12) = 58.09 \text{ cm}$

- ⑦ a.) For a population having mean μ and (finite) standard deviation σ , if $n > 30$, then the sampling distribution of \bar{X} is well approximated by a normal distribution with mean μ and standard deviation $\frac{\sigma}{\sqrt{n}}$.
i.e. $\bar{X} \overset{\text{approx}}{\sim} N(\mu, \frac{\sigma^2}{n})$

- b.) If the objective of the study is make inferences about μ and \bar{X} is used to estimate μ , the sampling distribution provides information about \bar{X} 's mean, variability, and the probability that \bar{X} varies about μ . As n increases, the variance of \bar{X} decreases.

8. a.) $\bar{X} = 60$

b.) It appears that \bar{x}^* 's distribution is bell-shaped so that \pm one standard from the center should capture about 68% of the values. i.e. $\frac{136}{200} = 0.68$ and ≈ 136 values are trapped within ± 6 or 7 units from the center. i.e., calculation-wise, $\hat{\sigma}_{\bar{x}} \approx 6.8$.

c.) $\frac{190}{200} = 0.95$ so ≈ 190 values are trapped in the CI.

Based on plot, consider, say, (46, 74).

d.) ii)

e.) iii)

9. a.) $\mu_{\bar{x}} = \mu = 2.1$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{0.4}{\sqrt{64}} = \frac{0.4}{8} = 0.05$$

b.) Using CLT, $\bar{X} \overset{\text{approx}}{\sim} N(2.1, 0.05)$

$$\begin{aligned} \text{c.) } P(1.9 \leq \bar{X} \leq 2.3) &= \text{pnorm}(2.3, 2.1, 0.05) - \text{pnorm}(1.9, 2.1, 0.05) \\ &= 0.9999307 - 3.167124 \times 10^{-5} \\ &\approx 0.9999 \end{aligned}$$