

Rotating Stars from *Kepler* Observed with Gaia DR2

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ABSTRACT

We have matched the astrometric data from *Gaia* Data Release 2 to the sample of stars with measured rotation periods from *Kepler*. Using 30,305 stars with good distance estimates, we select 16,248 as being likely main sequence single stars centered within a 0.5 mag region about a 1 Gyr isochrone, removing many sub-giants and unresolved binary stars from the sample. The rotation period bimodality, originally discovered by [McQuillan et al. \(2013\)](#), is clearly recovered for stars out to 525pc, but is not detectable at further distances. This bimodality correlates with Galactic height as well, dropping strongly for stars above $Z > 90$ pc. We also find a significant width in the stellar main sequence of $M_G \sim 0.25$ mag, as well as a coherent gradient of increasing rotation periods diagonal to the main sequence. We interpret this to be the simultaneous change in luminosity and loss of angular momentum as stars evolve along the main sequence. The diagonal offset from the main sequence is unexpected, however, and may provide a new independent test of both stellar evolution and gyrochronology models.

1. INTRODUCTION

Over the past decade the study of stellar rotation has transformed from a niche observation limited to a handful of nearby clusters and few thousand bright stars, to an area of great interest for field stars with a rapidly growing sample size. The *Kepler* mission ([Borucki et al. 2010](#)), through its unmatched combination of photometric precision and years-long observation baseline, has produced the largest precision sample of rotating stars to date – more than 30,000 sources to date ([McQuillan et al. 2014](#)). Although the light curves available from the *Gaia* mission are not as densely sampled

in time as *Kepler* ([Gaia Collaboration et al. 2016](#)), they have yielded over 147,000 candidate rotation periods as of Data Release 2 ([Lanzafame et al. 2018](#)). The extended *Kepler* mission, K2 ([Howell et al. 2014](#)), has now observed more stars than the original *Kepler* sample, potentially doubling the number of high precision stellar rotation periods available. Similarly, by the end of the *Gaia* mission [Lanzafame et al. \(2018\)](#) estimate a sample of 3–20 million rotation periods will be recovered. The era of statistical studies in stellar rotation has therefore begun.

Stellar rotation has long been noted as a means to possibly age-date stars due to their constant angular momentum loss via winds ([Skumanich 1972](#)). While studies of open clusters give hope that this “gyrochronology” model broadly works for solar-type and lower-mass

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stars, many uncertainties exist about the details of this spin-down and its utility as a clock. These include questions about the initial rotation period distribution for stars (e.g. Barnes 2010; Matt et al. 2015), the specific analytic prescription for modeling the spin-down (Anus et al. 2015), and exploring the efficiency of this angular momentum loss mechanism at older ages (van Saders et al. 2016).

One of the most compelling results from the rotating star sample in *Kepler* is the discovery of a bimodal period distribution. McQuillan et al. (2013) first found a bimodality in the distribution of field M dwarfs with periods between ~ 10 and ~ 50 days. This feature was also found in the *Kepler* field K dwarfs in McQuillan et al. (2014), but was not seen in the bluer stars. Using Gaia DR1, Davenport (2017) was able to remove contaminating sub-giants from the rotation sample, and found the bimodality extended to the G dwarfs as well. This bimodal surface rotation period distribution is either a new short-lived transition or instability phase of rapid angular momentum loss, or a signature of star formation history imprinted in the present-day rotation period distribution.

However, as Davenport (2017) notes this feature has only been observed in the *Kepler* rotation period catalog, and most critically only for stars within ~ 300 pc. The faint M dwarfs in the *Kepler* sample studied in McQuillan et al. (2013) have an average distance of < 250 pc. Gaia DR1 was also only able to provide precise distances for the nearest stars, and Davenport (2017) report an median distance of 285 pc for the blue stars in their sample.

In this paper we extend the work of Davenport (2017) in studying the *Kepler* rotation period distribution as a function of distance from the Sun using new astrometric data from the *Gaia* mission. By matching the McQuillan et al. (2014) rotation period catalog to the newest data from *Gaia* Data Release 2 (Gaia Collabora-

tion et al. 2018), we can use precise distances for essentially every star in the McQuillan catalog to select the most-likely main sequence dwarfs out to distances > 2 kpc. Importantly this filters out both sub-giants, the main contaminant noted by Davenport (2017), and unresolved binary stars. Here we demonstrate the power of such a combined time-domain and astrometric sample for constraining the detailed evolution of main sequence stars themselves, and exploring the star formation history of the Milky Way.

2. THE *Kepler*–GAIA DATA

We used the largest homogeneous catalog of rotation periods available from the *Kepler* mission. The sample from McQuillan et al. (2014) provides rotation periods for more 34,030 stars, measured using the Auto-Correlation Function (ACF). While the ACF does not recover periods with as much precision as methods such as the Lomb-Scargle Periodogram, it is more robust to detecting the true period as opposed to an alias, and more complete for batch analysis of all stars (e.g. see Aigrain et al. 2015).

The *Kepler* data was matched to the *Gaia* DR2 source catalog using a 1 arcsecond radius. We used the *Kepler*–Gaia cross-match made publicly available by M. Bedell, which included entries for 195,830 sources. *Kepler*-based stellar parameters are included in this cross-match from the Data Release 25 *Kepler* catalog. Joining this cross-matched table to the McQuillan et al. (2014) catalog, we found 33,538 sources with *Gaia* astrometry and *Kepler*-derived rotation periods.

To select stars with good parallaxes, as well as high quality photometry from *Gaia*, we selected stars with the following criteria:

- Parallax error < 0.1 mas
- $\sigma(M_G)/M_G < 0.01$
- $\sigma(G_{BP})/G_{BP} < 0.01$
- $\sigma(G_{RP})/G_{RP} < 0.01$

Rather than simply use the inverse *Gaia* parallax values to measure the distance to sources, we use the improved distance prescription from Bailer-Jones et al. (2018), who provided independent distance estimates for 1.33 billion *Gaia* sources using a weak prior on the distribution of stars in our Galaxy. We follow their suggested use of the distance catalog, including only sources with `modality_flag == 1` (i.e. not a bimodal distance solution) and `result_flag == 1` (i.e. a well constrained distance).

Our final sample contained 30,305 stars in *Gaia* DR2 with measured *Kepler* rotation periods that passed these selection criteria. A color-magnitude diagram (CMD) of this sample using the *Gaia* bands is presented in Figure 1, with points colored by their measured *Kepler* rotation periods.

3. SELECTING MAIN SEQUENCE STARS

As in Davenport (2017), the color-magnitude diagram in Figure 1 shows many of the bluer stars in the McQuillan et al. (2014) sample are located significantly above the main sequence. These are likely subgiant stars, which no longer follow the main sequence stars spin-down evolution (e.g. do Nascimento et al. 2012; van Saders & Pinsonneault 2013). Since Davenport (2017) found subgiants could obscure the rotation period bimodality for G dwarfs, these must be excluded from our analysis, but we encourage future studies to explore the wealth of angular momentum evolution data from these post-main sequence objects.

Beyond the subgiant contamination, we also see a secondary population of stars in a parallel track ~ 0.75 mag above the normal main sequence, as expected and seen in other color-magnitude diagrams. This parallel main sequence occurs due to unresolved equal-mass (or nearly equal-mass) field binaries, and was seen in the *Gaia* DR1 data as well (Anderson et al. 2017). Since the tightest of these systems may have experienced tidal evolution that could sig-

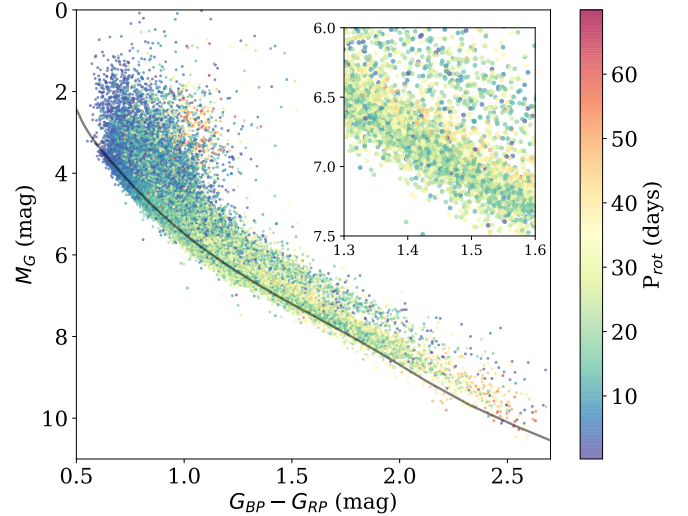


Figure 1. Color-magnitude diagram for 30,305 *Kepler* stars from the McQuillan et al. (2014) sample that are included in *Gaia* DR2, colored by their measured rotation period. For reference we show a 10^9 year MIST isochrone used to select likely main sequence, single stars (black line). As in Davenport (2017), the bluer stars in the sample are significantly contaminated by sub-giants. A track of binary stars is apparent ~ 0.75 mag above the main sequence. The inset figure highlights a portion of the single star and equal-mass binary main sequences.

nificantly impact their rotation evolution (e.g. Lurie et al. 2017), and we lack the ability with the *Gaia* DR2 data to adequately constrain their physical separations, we must also remove these unresolved binaries from our analysis. We do not explore the binary population in any detail here, but this sample could provide useful insight into the tidal evolution of binary stars, and are good targets for radial velocity follow-up to characterize binary system properties. We also note a small number of systems above the even the equal-mass binary main sequence track, which could be due to unresolved triple star systems.

We use an isochrone from the Mesa Isochrones and Stellar Tracks suite (MIST; Choi et al. 2016) to choose likely main sequence stars in

Figure 1. Our favored model to represent the main sequence in this study had $[\text{Fe}/\text{H}] = +0.25$ and an age of 10^9 years, and was chosen by-hand. Single, main sequence stars were selected in a region spanning 0.1 mag fainter and 0.4 mag brighter than the MIST isochrone, resulting in a final sample of 16,248 stars for analysis of their rotation period distributions.

4. TRACING THE PERIOD BIMODALITY

Using this sample of likely single, main sequence stars from *Kepler* and *Gaia*, we are able to explore the distribution of rotation periods for stars as a function of their distance and Galactic location. The rotation period bimodality in *Kepler* stars was previously detected only for stars within ~ 300 pc of the Sun due to the limits of available parallax data. Now with *Gaia* DR2, our sample of main sequence stars with measured rotation periods from *Kepler* with adequate distance estimates for filtering out subgiants extends to over 2 kpc.

In Figure 2 we present the period–color diagram for our sample of stars, split into six bins of projected distance. The first panel (0–350 pc) effectively reproduces the results of Davenport (2017) for bluer stars and McQuillan et al. (2014) for the redder stars. A gap in the observed rotation periods as a function of color is seen, at a period of approximately 5 days for $G_{BP} - G_{RP} \approx 1$, 20 days for $G_{BP} - G_{RP} \approx 2$, and increasing towards 30 days for the reddest stars in our sample. This gap corresponds with a line of approximately constant age, consistent with a gyrochrone with age ~ 600 Myr (Davenport 2017).

The bimodality is still apparent in the second distance bin (350–525 pc), clearly visible in the redder stars, but seems to fade in the final three bins. Other structures in the period distributions are visible, however. For example, a thin sequence of stars with rotation periods near 10 days is faintly visible in the most distant bin (900–2500 pc) for stars with colors of

$0.8 < G_{BP} - G_{RP} < 1.2$. This feature is due to the 1 Gyr open cluster NGC 6811 in the *Kepler* field (Meibom et al. 2011), whose distance is ~ 1100 pc (Sandquist et al. 2016).

To better illustrate the evolution of rotation periods for all the stars between the distance bins, in Figure 3 we follow Davenport (2017) and subtract the rotation period of a 600 Myr gyrochrone. As no published gyrochronology model yet exists that has been tuned to the *Gaia* photometric colors, we adopt the same gyrochronology model of Eqn. 2 from Meibom et al. (2009) used by Davenport (2017) to approximately trace the rotation period gap at 600 Myr as a function of $B - V$ color. We convert stars from the observed *Gaia* $G_{BP} - G_{RP}$ color to $B - V$ using the same 1 Gyr MIST isochrone model used to define the main sequence in Figure 1 above.

Our sample naturally becomes biased towards the bluer (brighter) stars as we reach larger distances. Since bluer stars have more rapid rotation and more dramatic period evolution, gyrochronology models are “bent” strongly for these stars, and thus the period bimodality (or other structures) become difficult to distinguish. Davenport (2017) used an ad-hoc modification of the gyrochrone model for the hottest stars to illustrate the existence of the period bimodality. However, in Figure 3 we limit our analysis to stars with $0.8 < B - V < 1.5$ (approximately $0.9 < G_{BP} - G_{RP} < 2.2$, or $0.5 < M_{\odot} < 0.9$), where the gyrochrone is most flat as a function of color. This color range was chosen to ensure ample stars were available in each distance bin, but without having to use the ad-hoc gyrochrone model correction from Davenport (2017).

Figure 3 (left) shows clearly that the short period component of the rotation period bimodality dominates only for the nearest stars, and steadily decreases with increasing distance. The *Kepler* field is centered on a Galactic latitude

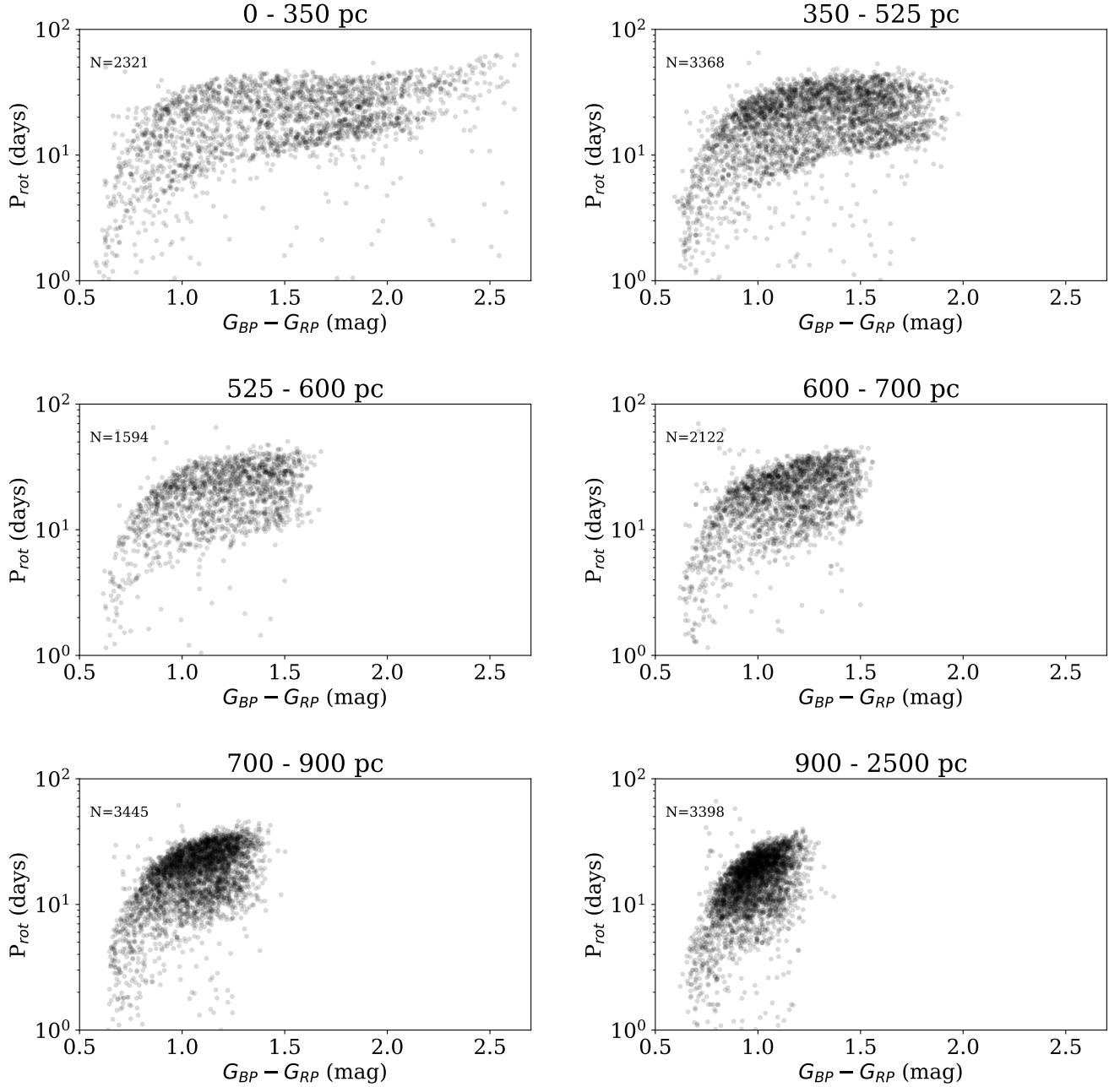


Figure 2. Color–period diagrams for our sample of likely main sequence stars, divided into six bins of distance. Our nearest bin (within 350pc) is effectively the distance analyzed in [Davenport \(2017\)](#) using Gaia DR1, and clearly shows the rotation period bimodality for the entire sample. The brighter magnitude limit of the *Kepler* sample results in redder (fainter) stars missing in our further distance bins. The rotation period bimodality can be seen in the 350-525 pc bin, but is not found in the bluer stars at further distances.

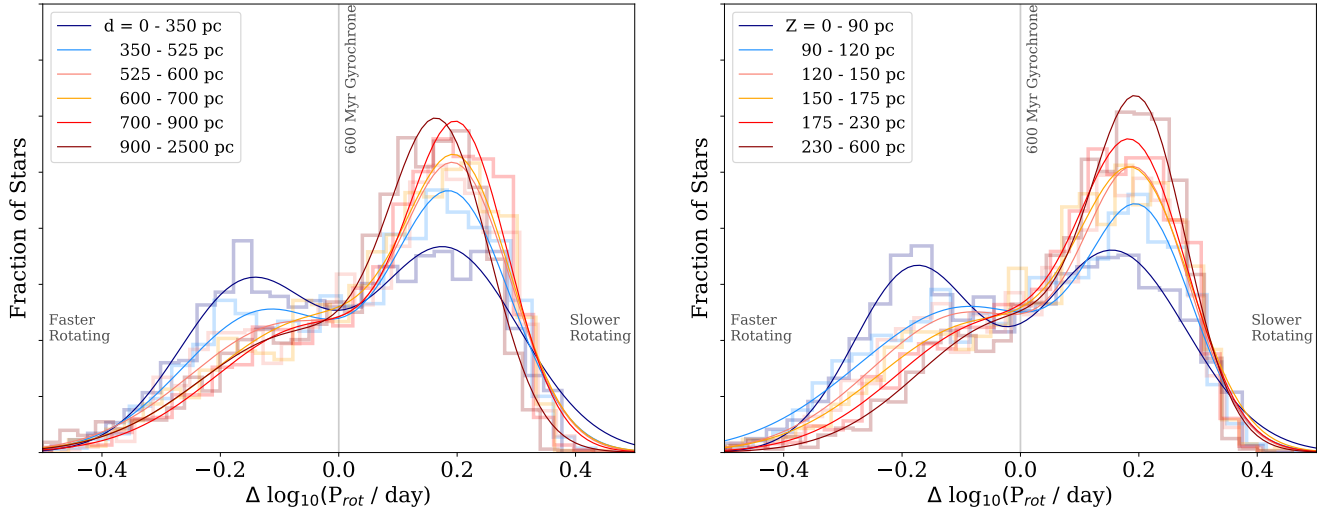


Figure 3. Left: Distribution of the log rotation periods after a 600 Myr gyrochrone was subtracted, using the same distance bins shown in Figure 2 (faint lines). Two-gaussian models were fit to each histogram (bold lines). The rotation period bimodality for stars within 350 pc has two nearly equal peaks similar to those found in Davenport (2017), at -0.15 and +0.18 dex. The fast rotating peak (left side) declines sharply at further distances. Right: Same as Left, but in bins of Galactic height above the plane (Z). The drop-off of fast rotating, young stars is even more pronounced as a function of height.

of $b \sim 13.5^\circ$, and so we can also study the period bimodality as a function of height above the Galactic mid-plane. Both galaxy formation simulations (Ma et al. 2017) and observations of stars in the nearby Milky Way (Xiang et al. 2017) indicate that height above the mid-plane correlates strongly with the median ages for stars out to distances of several kpc. For low-mass stars the Milky Way thin disk has a scaleheight of ~ 300 pc (Gilmore & Reid 1983). However, since the *Kepler* field is oriented towards low latitudes we do not reach significant heights above the disk. The projected height above the mid-plane for the distance bins shown in Figures 2 and 3 ranges from $Z \sim 100$ pc at a distance of $d = 350$ pc to $Z \sim 230$ pc at $d = 900$ pc. As a result, we are only sensitive to changes in the youngest stars within this span of Z .

In Figure 3 (right) we find that the drop-off of the short-period (rapid rotating) component of the period bimodality is even more pronounced as a function of Z , decreasing rapidly after only 90 pc. With increasing height we also see that the shift to the longer period component is more smooth. However, from these two projections in Figure 3 alone (distance and height) we cannot definitively determine the spatial structure of the rotation period bimodality.

To further understanding the spatial extent of this age-related feature, in Figure 4 we break the lowest height stars ($Z < 100$ pc) in to two roughly even samples, split as a function of their projected distance. Note we have also repeated this exercise for stars in higher ranges of Z , and find the decline of the rapid rotators is again uniform between subsamples of varying projected distance. The rotation period bimodality is clearly seen in both distance bins of Figure 4, indicating that the feature is likely not a localized star formation history artifact centered around the Sun. Instead, we believe this feature is characteristic of the age- Z dynamical

correlation observed within the solar neighborhood of our Galaxy.

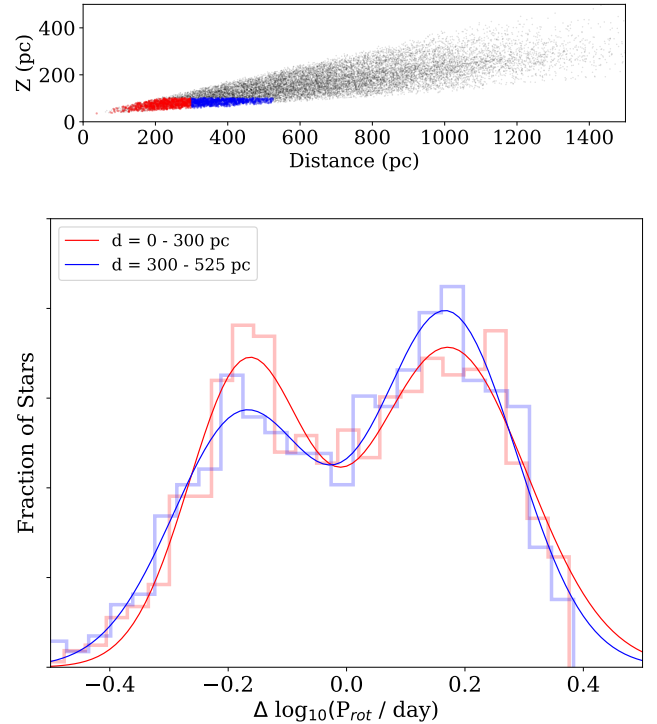


Figure 4. Top: Galactic height versus distance for the stars in our sample. Two approximately equal subsets of stars near the Galactic mid-plane have been highlighted, with distances of $d < 300$ pc (red), and $300 < d < 525$ pc (blue). Bottom: As in Figure 3, the distribution of rotation periods after a 600 Myr gyrochrone was subtracted (faint lines), and with two-Gaussian fits (bold lines) for the same subsets of stars as above. The period bimodality is seen in both distance bins, suggesting it is not localized around the Sun.

5. RECALIBRATING STELLAR EVOLUTION MODELS

A subtle feature we noticed in Figure 1 is the color gradient (i.e. rotation period gradient) for the stars in between the single and binary star main sequence populations. In Figure 1 this appears as a yellow stripe (i.e. rotation periods of 30-40 days) between these blue-green sequences for systems with colors of $G_{BP} - G_{RP} \approx 1.5$. To

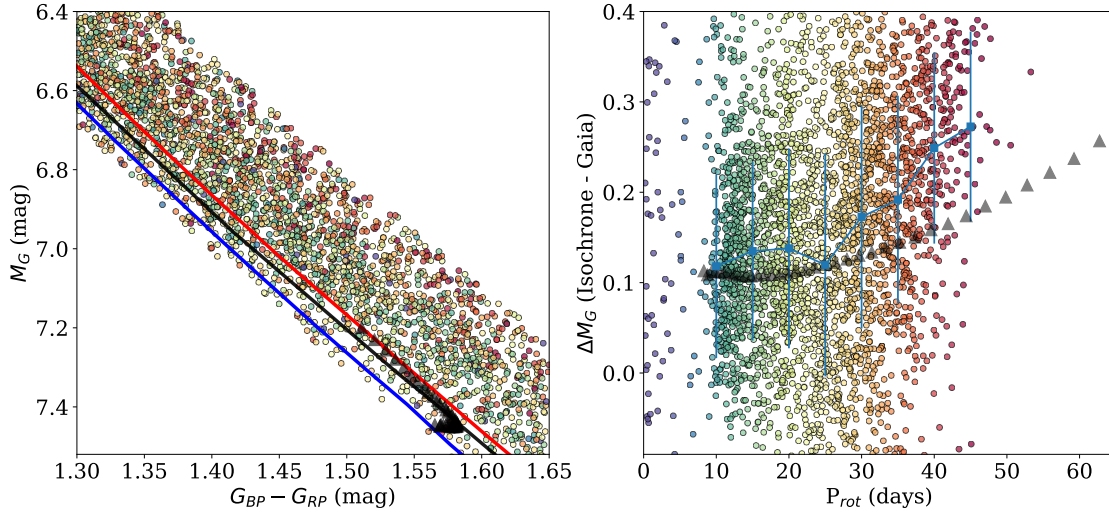


Figure 5. Left: Enlarged portion of the color–magnitude diagram from Figure 1 in a region centered near $\sim 0.75 M_{\odot}$, with main sequence stars colored by their measured rotation periods from [McQuillan et al. \(2014\)](#). MIST isochrones at ages of 10^8 , 10^9 , and 10^{10} yr are shown for comparison (blue, black, and red lines). The predicted evolution of a $0.7 M_{\odot}$ star is highlighted (black triangles). Right: Difference in M_G from the 10^9 yr MIST isochrone as a function of rotation period (point color again indicates rotation period, as in Left panel). Blue squares show an increase in the median M_G offset in bins of increasing rotation period. Error bars shown are the standard deviation of ΔM_G in each bin. The $0.7 M_{\odot}$ star brightness evolution is shown as a function of rotation evolution from [Meibom et al. \(2009\)](#) (black triangles).

exaggerate this feature, we have reproduced a portion of our color–magnitude diagram focused on the main sequence near this stellar color in the left panel of Figure 5. A clear color gradient is present, with red points (slower rotators) appearing preferentially above the main sequence. The right panel of Figure 5 concretely demonstrates a correlation between the measured rotation period and the vertical offset (i.e. absolute magnitude) from the 10^9 year MIST isochrone. Slower rotating stars are brighter at a given color.

We interpret this observation as being due to the increase in luminosity of stars across their main sequence lives, coupled with the angular momentum loss that underpins gyrochronology. Indeed, the three MIST isochrones shown in Figure 5 with ages of 10^8 , 10^9 , and 10^{10} years clearly predict a net increase in brightness of the main sequence over time. We also track the color–magnitude evolution of a $0.7 M_{\odot}$ star over

its lifetime in Figure 5, which shows the “hook” the star takes over its main sequence life.

Inverting the color–magnitude diagram into precise ages for main sequence stars using *Gaia* is beyond scope of this work. However, Figure 5 clearly demonstrates that age information is not only present for main sequence stars, but it may also be a critical factor in accurately modeling the CMD. For example: younger, presumably more metal rich stars, should have redder main sequence colors. This in turn should move the entire main sequence track to the right in the CMD. However, we find older stars (slower rotators) appearing on the right side of the main sequence, due to their increased luminosity with age. The main sequence location of a star is therefore not simply due to its mass and metallicity in the *Gaia* era, but its age must also be taken into account.

In Figure 5 we also show each stars’ offset from the main sequence as a function of its rotation period within our zoomed-in CMD, as

well as a prediction for the evolution of a $0.7 M_{\odot}$ star. The spin-down model here is a combination of the MIST isochrone evolution, as well as the Meibom et al. (2009) gyrochronology model. Note this spin-down model has been arbitrarily offset in ΔM_G to approximately match the observed rapid rotators. While *Kepler* light curves are not able to measure rotation reliably for stars with periods longer than ~ 30 days, we find that stars with brightness (vertical) offsets in the CMD consistent with being several Gyr old have average rotation periods far shorter than the 60–80 days values predicted from the spin-down models.

One interpretation of this result may be that the older stars are spinning *faster* than expected for stars their age. This is qualitatively similar to the model of broken spin-down occurring at a critical Rossby number suggested by van Saders et al. (2016). Though we cannot definitively confirm such intriguing rotation evolution from this initial investigation given the observation bias for long rotation periods from *Kepler*, matching the *Gaia* CMD with other rotation period measurements may provide an ideal dataset to test the van Saders et al. (2016) model against.

In tracking only the brightness evolution of stars as they age, we neglect the color evolution shown in Figure 5 (left panel), which predicts a star will move roughly *along* the main sequence track as it changes in luminosity over time. Instead we clearly observe a diagonal gradient in the rotation periods consistent with being a stellar age affect, which may point to missing physics in the MIST models. We believe simultaneous constraints on both the precise CMD location and surface rotation rate for stars, as demonstrated here, will be a valuable utility for calibrating a new generation of isochrone and gyrochronology models.

6. DISCUSSION

Using a sample of 16,248 single main sequence stars with measured rotation periods from *Kepler* and parallaxes from *Gaia* DR2, we have begun to explore the spatial distribution of stellar ages near the Sun using gyrochronology. The bimodality in rotation periods first reported by McQuillan et al. (2013) appear to be constrained to low galactic heights, rather than in a bubble centered around the Sun. This is consistent with the rotation period bimodality being a direct tracer of the star formation history, and indicates a burst of star formation within the past ~ 600 Myr within the galactic disk.

Unfortunately the *Kepler* survey only covers a single pointing, and so our volume analysis of the stellar ages is limited here. However, with more than 15 distinct lines of sight available from K2, the extended *Kepler* mission, we will soon be able to more than double our sample of rotating field stars and probe a much wider range of stellar ages. This may enable us to determine the spatial scales that star formation histories are coherent over in the nearby Milky Way, and make comparisons to the ~ 100 pc resolved star formation history maps available for nearby galaxies such as Andromeda (Lewis et al. 2015; Williams et al. 2017). For example, gyrochronology ages for disk stars within 1 kpc of the Sun could be used to test if star formation propagates due to spiral arm density waves (e.g. see Choi et al. 2015).

While we have removed as contaminants the prominent parallel main sequence of nearly equal-mass binary stars in this analysis, as well as sub-giant stars, both of these samples are clearly deserving of further analysis. For example, comparing the rotation period distribution for binary versus single main sequence stars may provide constraints on their dynamical histories.

Finally, in the *Gaia* era, stellar evolution modelers have the daunting task to explain an increasing number of precisely determined features from survey observations, such as the fas-

cinating new main sequence gap revealed by [Jao et al. \(2018\)](#), and the main sequence width seen here in Figure 1. This work has presented strong motivation for a new generation of stellar evolution and rotation models to be produced to accurately model the *Gaia* main sequence. With *Kepler*, K2, and soon TESS, rotation measurements will be available for hundreds of thousands of nearby stars that *Gaia* has provided precise distances for. We hope new isochrone models will reproduce both the observed colors and luminosities of stars due to their ages and abundances, as well as the evolution of their surface rotations.

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Software: Python, IPython ([Pérez & Granger 2007](#)), NumPy ([Oliphant 2007](#)), Matplotlib ([Hunter 2007](#)), SciPy ([Jones et al. 2001](#)–), Pandas ([McKinney 2010](#)), Astropy ([Astropy Collaboration et al. 2013](#))

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