

# Quantum Credit Risk Analysis

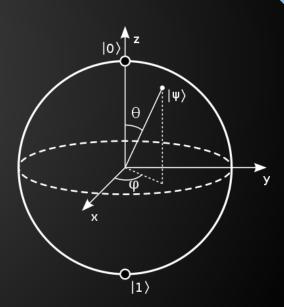
### **Presented by:**

Arjun Puppala, Jose Ramon Aleman, Marti Ciurana

### **Tutor:**

Giulio Gasbarri





## Outline - Draft

- Introduction
- Problem
  - Description
  - Definition
  - Parameters
- Methods
  - MC (Classical)
  - QAE
    - Grover's Algorithm
    - QFT
  - IQAE
- Results
  - Uncertainty model
    - Loss Distribution
    - Z Distribution
    - Default Probabilities
  - Expected Loss
  - Value at Risk (VaR)
  - Conditional Value at Risk (CVaR)
- Conclusions

### Introduction

We introduce and describe an iterative algorithm of the Quantum Amplitude Estimation (QAE), known as the Iterative QAE (IQAE). This is used for estimating credit risk that outperforms Monte Carlo (MC) simulations on traditional computers. We calculate the Economic Capital (EC) required, which is the difference between the Value at Risk (VaR) and the predicted Loss Distribution Value (LDV). The calculation of the EC required is of interest, because it quantifies the amount of capital required to be solvent at a certain level of confidence, making it an important risk statistic. We implement this problem for a realistic LDV and analyze its scaling to a realistic problem size. We present estimates of the overall number of necessary gubits, the expected circuit depth, and how this translates into an expected runtime on future fault-tolerant quantum hardware under acceptable assumptions.

## Problem

Description, Definition, and Parameters

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua.

## **Problem Description**

We can describe the problem as the simple default risk, that a lender takes on in the chance that a borrower will be unable to make the required payments on their debt obligation. Whenever a lender extends credit to a borrower, there is a chance that the loan amount will not be paid back. The measurement that looks at this probability is the default risk.

The default risk applies to both individuals who borrow money, and companies that issue bonds and due to financial constraints, are not able to make interest payments on those bonds. Whenever a lender extends credit, calculating the default risk of a borrower is crucial as part of its risk management strategy. Whenever an investor is evaluating an investment, determining the financial health

### **Problem Definition**

We analyze the credit risk of a portfolio of

k

assets. The default probability of every asset

k

follows a Gaussian Conditional Independence model, i.e., given a value

Ζ

sampled from a latent random variable

### Problem Parameters

The introduced quantum algorithm for estimating the credit at risk, Iterative Quantum Amplitude Estimation (IQAE), does not rely on Quantum Phase Estimation (QPE), and is based on Grover's Algorithm, reducing the required number of qubits and gates needed. We provide a rigorous analysis of IQAE and prove that it achieves a quadratic speedup up to a double-logarithmic factor compared to classical Monte Carlo simulation. We test the algorithm in a two (2) assets portfolio.

## Methods

MC, QAE, Grover's Algorithm, QFT, IQAE Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua.

### Methods

In order to further demonstrate the capabilities of IQAE, we used classical simulations of quantum hardware to show that it can also be applied to speed up the computation of risk measures of a simple two-asset (2) portfolio. Nevertheless, we notice that to achieve quantum advantage in a real-world scenario, the quality of current quantum hardware needs to be improved. Errors arising from the limited coherence time and cross-talk when measuring the states of qubits need to be substantially suppressed. Furthermore, because of this reason, the number of qubits must be increased.

We went on to show how IQAE can be applied to the task of pricing an asset using real quantum hardware. However, the current pace of advances in research directed at improving both quantum hardware and quantum algorithms makes us optimistic that real quantum advantage in risk analysis can be achieved in the

## Classical Method: Monte Carlo (MC)

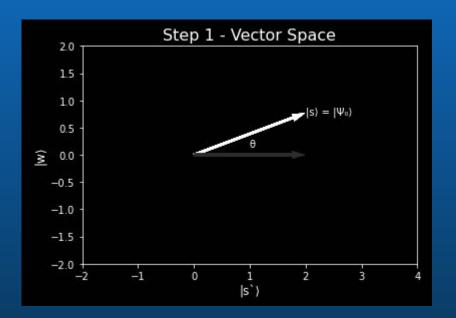
The Monte Carlo (MC) method is a broad class of computational algorithms that rely on repeated random sampling to obtain numerical results. The underlying concept is to use randomness to solve problems that might be deterministic in principle. MC predicts a set of outcomes based on an estimated range of values versus a set of fixed input values.

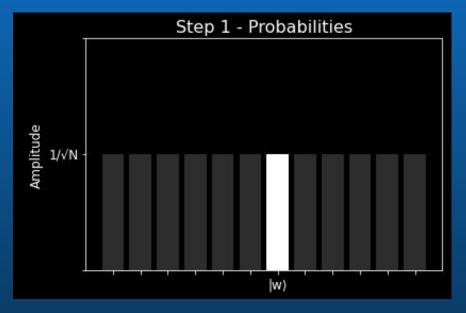
In other words, a MC simulation builds a model of possible results by leveraging a probability distribution, such as a uniform or normal distribution, for any variable that has inherent uncertainty. It recalculates the results over and over, each time using a different set of random numbers between the minimum and maximum values. In a typical MC experiment, this exercise can be repeated thousands of

## Quantum Amplitude Estimation (QAE)

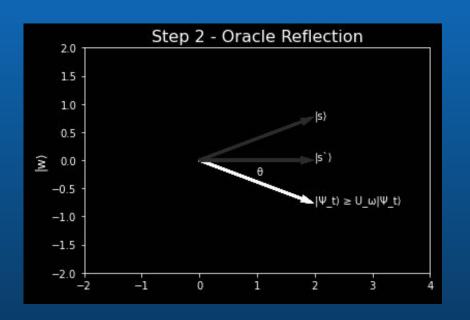
# Grover's Algorithm

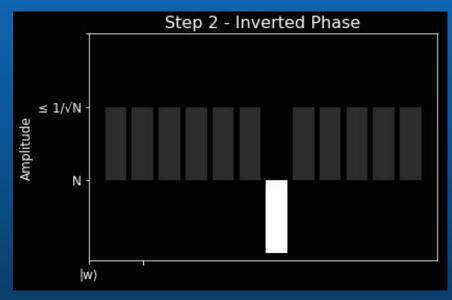
## Step 1 - Initialize System



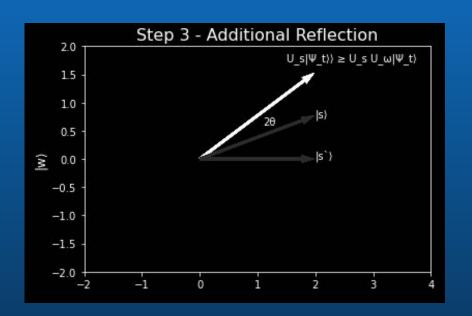


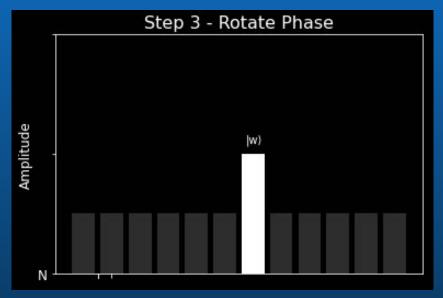
## Step 2 - Oracle Reflection and Inverted Phase



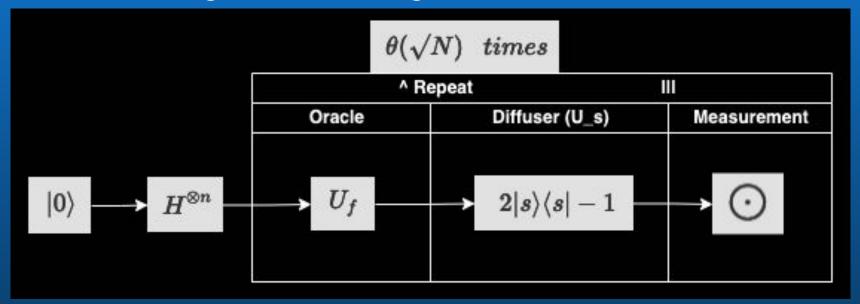


## Step 3 - Additional Reflection and Rotate Phase





## Grover's Algorithm Diagram

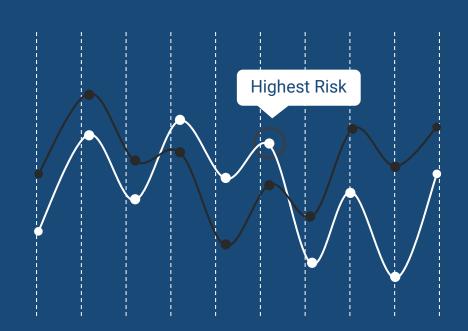


## Quantum Fourier Transform (QFT)

# Iterative QAE (IQAE)

# Results

UM, EL, VaR, CVaR



## **Uncertainty Model (UM)**

# Expected Loss (EL)

# Value at Risk (VaR)

## Conditional Value at Risk (CVaR)

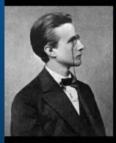
### Conclusions

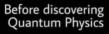
<Conclusions goes here>

# Thank you for your time



#### Theoretical physicist Max Planck







After discovering Quantum Physics

### The problem

#### Company

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua.

Ut enim ad minim veniam, quis nostrud

#### Context

Ut enim ad minim veniam, quis nostrud exercitation

 Duis aute irure dolor in reprehenderit in voluptate velit

#### Problem statement

Excepteur sint occaecat cupidatat non proident, sunt in culpa qui officia deserunt mollit anim id est laborum.

## Challenges deep-dive

#### Challenge 1

#### **Expand audience**

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua.

#### Challenge 2

#### Up 30-day actives

Ut enim ad minim veniam, quis nostrud exercitation

 Duis aute irure dolor in reprehenderit in voluptate velit

### Challenge 3

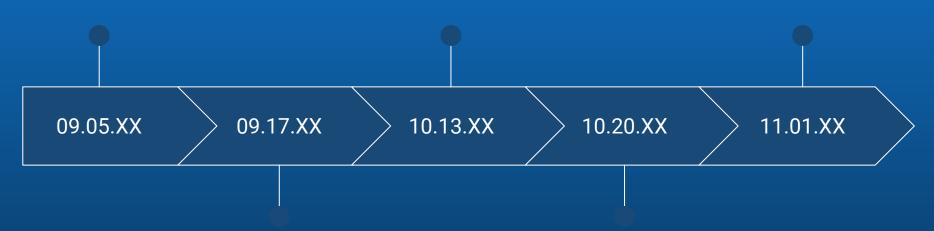
#### **Increase conversion**

Excepteur sint occaecat cupidatat non proident, sunt in culpa qui officia deserunt mollit anim id est laborum.

Lorem ipsum dolor sit amet, consectetur adipiscing elit

Lorem ipsum dolor sit amet, consectetur adipiscing elit

Lorem ipsum dolor sit amet, consectetur adipiscing elit



Lorem ipsum dolor sit amet, consectetur adipiscing elit

Lorem ipsum dolor sit amet, consectetur adipiscing elit

### The team

