

1)

$$\begin{array}{l}
 F_1 \begin{bmatrix} 1 & 1 & 1 & C \\ F_2 & 2 & 2 & 2 \\ F_3 & 0 & C & 2 & 3 \\ F_4 & 7 & 1 & 2 & 3 \end{bmatrix} \begin{array}{l} F_4 = 7F_1 - F_4 \\ F_2 \leftrightarrow F_3 \end{array} \rightarrow \begin{bmatrix} 1 & 1 & 1 & C \\ 0 & C & 2 & 3 \\ 2 & 2 & 2 & 2 \\ 7 & 1 & 2 & 3 \end{bmatrix} \begin{array}{l} F_3 = 2F_1 - F_2 \\ F_4 \leftrightarrow F_3 \end{array} \rightarrow \begin{bmatrix} 1 & 1 & 1 & C \\ 0 & C & 2 & 3 \\ 0 & 6 & 5 & (7C-3) \\ 0 & 0 & 0 & (2C-2) \end{bmatrix} \begin{array}{l} F_2 = \frac{F_2}{C} \\ F_3 = 6F_2 - F_3 \end{array}
 \end{array}$$

$$\begin{bmatrix} 1 & 1 & 1 & C \\ 0 & 1 & \frac{2}{C} & \frac{3}{C} \\ 0 & 0 & \frac{12}{C} - 5 & \frac{18}{C} - 3 \\ 0 & 0 & 0 & (2C-2) \end{bmatrix} = A$$

$$\begin{aligned}
 \det(A) &= 1 \cdot 1 \cdot \left(\frac{12}{C} - 5\right) \cdot (2C-2) = 24 - \frac{24}{C} - 10C + 10 \\
 &= 34 - \frac{24}{C} - 10C
 \end{aligned}$$