

## Homework 2

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2.1

$$\epsilon(M, N, \delta) = \sqrt{\frac{1}{2N} \ln \frac{2M}{\delta}}$$

a)

$$.05 \leq \sqrt{\frac{1}{2N} \ln \frac{2(1)}{.03}}$$

$$.0025 \leq \frac{1}{2N} \ln \frac{2}{.03}$$

$$.0025 \leq \frac{1}{2N} (4.1997)$$

$$.005N \leq 4.1997$$

$$840 \leq N$$

b)

$$.05 \leq \sqrt{\frac{1}{2N} \ln \frac{2(100)}{.03}}$$

$$.0025 \leq \frac{1}{2N} \ln \frac{200}{.03}$$

$$.0025 \leq \frac{1}{2N} \ln(8.80487)$$

$$.0025 \leq \frac{1}{2N} (2.1753)$$

$$.005N \leq 2.1753$$

$$435 \leq N$$

c)

$$.05 \leq \sqrt{\frac{1}{2N} \ln \frac{2(1000)}{.03}}$$

$$.0025 \leq \frac{1}{2N} \ln \frac{2000}{.03}$$

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$$.0025 \leq 11.10746)$$

$$.005N \leq 11.10746$$

$$2221.492 \leq N$$

2.11

$$\text{Theorem: } E_{out}(g) \leq E_{in}(g) + \sqrt{\frac{8}{N} \ln \frac{4m_H(2N)}{\delta}}$$

a) N = 100:

$$\sqrt{\frac{8}{100} \ln \frac{(4)(101)(2)(100)}{.1}}$$

$$\sqrt{.08 \ln(808,000)}$$

$$\sqrt{1.088185387}$$

$$1.043161247$$

The out-of-sample error is less than or equal to 1.043161247 + E<sub>in</sub>(g).

b) N = 1000:

$$\sqrt{\frac{8}{1000} \ln \frac{(4)(1001)(2)(1000)}{.1}}$$

$$\sqrt{.008 \ln(8,008,000)}$$

$$\sqrt{.127167612}$$

$$.356605682$$

The out-of-sample error is less than or equal to .356605682 + E<sub>in</sub>(g).

2.12

$$\text{Theorem: } N \geq \frac{8}{\epsilon^2} \ln \left( \frac{4((2N)^{d_{vc}} + 1)}{\delta} \right)$$

$$N \geq \frac{8}{.05^2} \ln \left( \frac{4((2N)^{10} + 1)}{.05} \right)$$

$$N \geq 320 \ln \left( \frac{4(1024N^{10} + 1)}{.05} \right)$$

$$N \geq 320 \ln \left( \frac{4096N^{10} + 4}{.05} \right)$$

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$$N \geq 320 \ln \frac{4096N^{10}}{.05} + 80$$

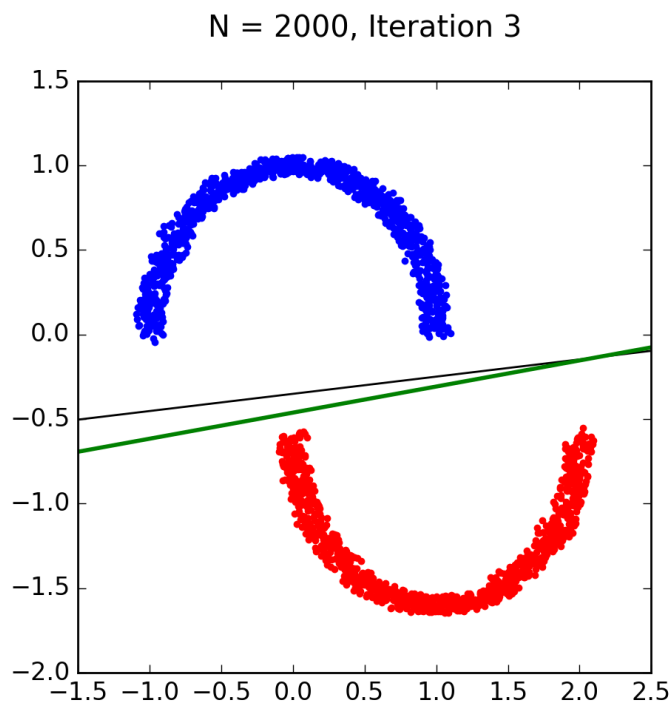
$$N - 80 \geq 320 \ln \frac{4096N^{10}}{.05}$$

$$.05N - 4 \geq 16 \ln(4096N^{10})$$

$$N \geq 36,344.2$$

3.1

a)



The perceptron learning algorithm took 3 iterations to converge and find the best fit line in between the two semi-circles.  $w$  is equal to  $[-1. \quad 0.33415214 \quad -2.16534827]$ .

b)

Using linear regression,  $w$  ends up being  $[-0.32193933 \quad 0.09342563 \quad -0.91802757]$ . It seemed to run faster than with the perceptron learning algorithm. I find it very interesting that  $w_0$  is -1 when using PLA and -0.32193933 when using linear regression. Both  $w$ 's fit the data, but they are very different results.