Practice quiz on Bayes Theorem and the Binomial Theorem

TOTAL POINTS 9

1. A jewelry store that serves just one customer at a time is concerned about the safety of its isolated customers.

1 / 1 point

The store does some research and learns that:

- 10% of the times that a jewelry store is robbed, a customer is in the store.
- A jewelry store has a customer on average 20% of each 24-hour day.
- The probability that a jewelry store is being robbed (anywhere in the world) is 1 in 2 million.

What is the probability that a robbery will occur while a customer is in the store?

- 1 0 500000
- 1 0 2000000
- 1 • 4000000
- 0 1 5000000

✓ Correct

What is known is:

A: "a customer is in the store," P(A)=0.2

B: "a robbery is occurring," $P(B) = \frac{1}{2.000,000}$

 $P(\text{a customer is in the store} \mid \text{a robbery occurs}) = P(A \mid B)$

$$P(A \mid B) = 10\%$$

What is wanted:

 $P(a \text{ robbery occurs} \mid a \text{ customer is in the store}) = P(B \mid A)$

By the product rule:

$$P(B \mid A) = \frac{P(A, B)}{P(A)}$$

and
$$P(A,B) = P(A \mid B)P(B)$$

Therefore:

$$P(B \mid A) = \frac{P(A \mid B)P(B)}{P(A)} = \frac{(0.1)\left(\frac{1}{2000000}\right)}{0.2} = \frac{1}{4000000}$$

- 2. If I flip a fair coin, with heads and tails, ten times in a row, what is the probability that I will get exactly six heads?
 - 0.021
 - 0.187
 - 0.2051
 - 0.305





3. If a coin is bent so that it has a 40% probability of coming up heads, what is the probability of getting *exactly* 6 heads in 10 throws?

1 / 1 point

- 0.0974
- 0.1045
- 0.1115
- 0.1219
- \checkmark Correct ${10 \choose 6} \times 0.4^6 \times 0.6^4 = 0.1115$
- 4. A bent coin has 40% probability of coming up heads on each independent toss. If I toss the coin ten times, 0/1 point what is the probability that I get at least 8 heads?

0.0132

- 0.0213
- 0.0312
- 0.0123
 - Incorrect

The answer is the sum of three binomial probabilities:

$$\left(\left(\begin{smallmatrix} 10 \\ 8 \end{smallmatrix} \right) imes \left(0.4^8 \right) imes \left(.6^2 \right)
ight) + \left(\left(\begin{smallmatrix} 10 \\ 9 \end{smallmatrix} \right) imes \left(0.4^9 \right) imes \left(0.6^1
ight)
ight) +$$

$$\left(\left(\begin{smallmatrix} 10 \\ 10 \end{smallmatrix} \right) \right) imes \left(0.4^{10}
ight) imes \left(0.6^0
ight)
ight)$$

5. Suppose I have a bent coin with a 60% probability of coming up heads. I throw the coin ten times and it comes up heads 8 times.

1/1 point

What is the value of the "likelihood" term in Bayes' Theorem -- the conditional probability of the data given the parameter.

- 0.120932
- 0.043945
- 0.122885
- 0.168835
 - Correct

Bayesian "likelihood" --- the p(observed data | parameter) is

p(8 of 10 heads \mid coin has p = .6 of coming up heads)

$$\binom{10}{8} imes (0.6^8) imes (0.4^2) = 0.120932$$

We have the following information about a new medical test for diagnosing cancer. 1 / 1 point

Before any data are observed, we know that 5% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer. The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 90% of them get an accurate test result of "Negative" for cancer. The other 10% get a false test result of "Positive" for cancer.

What is the conditional probability that I have Cancer, if I get a "Positive" test result for Cancer?

**Formulas in the feedback section are very long, and do not fit within the standard viewing window. Therefore, the font is a bit smaller and the word "positive test" has been abbreviated as PT.

32.1% probability that I have cancer

9.5%

O 4.5%

O 67.9%



 $7.\;\;$ We have the following information about a new medical test for diagnosing cancer.

1/1 point

Before any data are observed, we know that 8% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer.

The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 95% of them get an accurate test result of "Negative" for cancer.

The other 5% get a false test result of "Positive" for cancer.

What is the conditional probability that I have cancer, if I get a "Negative" test result for Cancer?

O 88.2%

0.9%

 $\bigcirc\ .80\%$

O 99.1%

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✓ correct
p(\text{cancer} \mid \text{negative test}) =
\frac{p(\text{negative test} \mid \text{Cancer}) p(\text{Cancer})}{p(\text{negative test} \mid \text{cancer}) p(\text{cancer}) + p(\text{negative test} \mid \text{no cancer}) p(\text{no cancer})}
\frac{(10\%)(8\%)}{(10\%)(8\%) + (95\%)(92\%)}
\frac{0.8\%}{0.8\% + 87.4\%}
\frac{0.8\%}{88.2\%}
= 0.9\%
```

✓ Correct

Bayes' Theorem, the answer is

 $\frac{(.65)(.01)}{((.65)(.01) + (.08)(.99))}$

=7.58%