



Announcements

- Last video homework due tonight!
- I am, unfortunately, still not done with the Test 3 grading
- Hopefully I got a grade report posted with what I DO have graded though...
- We'll talk the final at the end of the day

$$E_3 = 3E_1$$

$$E_2 = 4E_1$$

$$E_1$$

$$d$$

$$x$$

$$h^2 = u^2 E_1$$

$$|d\vec{E}| = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2}$$

$$= \frac{\lambda}{4\pi\epsilon_0} \frac{dx}{r^2}$$

$$dE_y = \frac{\lambda}{4\pi\epsilon_0} \frac{dx}{r^2} \frac{y}{r}$$

$$dE_x = \frac{\lambda}{4\pi\epsilon_0} \frac{dx}{r^2} \frac{x}{r}$$

$$\cos\theta = \frac{y}{r}$$

$$d\vec{E} = |d\vec{E}| \cos\theta$$

$$dE_y = \frac{\lambda}{4\pi\epsilon_0} \frac{dx}{r^2} \frac{y}{r}$$

$$dE_x = \frac{\lambda}{4\pi\epsilon_0} \frac{dx}{r^2} \frac{x}{r}$$

$$\lambda_1 = \frac{u_1}{f}$$

$$\lambda_2 = \frac{u_2}{f}$$

$$\sin\theta_2 = \frac{\lambda_1}{AB'}$$

$$\frac{\sin\theta_1}{\sin\theta_2} = \frac{\lambda_2}{\lambda_1} = \frac{u_1}{u_2} = \frac{n_2}{n_1}$$

$$U = F_e r = F_r \sin\theta = F_L$$

$$v = v_0 \sin\theta$$

$$F_n \cdot x + F_g \cdot x = m a$$

$$F_n \cdot x = 0$$

$$F_g \cdot x = F_g \sin\theta$$

$$= m g \sin\theta$$

$$a_x = g \sin\theta$$

$$v^2 = 2 g h$$

$$v_s = \sqrt{2 g h} \cdot \sin\theta$$

Upcoming:

A Semester in Review

$$|u|^2 = A^2 \exp\left(-\frac{x^2}{2\sigma^2}\right)$$

$$B(x) = \frac{\sigma}{\sqrt{\pi}} e^{-\sigma^2(x-x_0)^2}$$

$$E(\psi) = A \cos(k_0 x - \omega t)$$

$$|F| = \frac{1}{4\pi\epsilon_0} \frac{ze^2}{r}$$

$$= \frac{mv^2}{r}$$

$$E_{pot} = -\frac{1}{4\pi\epsilon_0} \frac{ze^2}{r}$$

$$E_{kin} = \frac{1}{2} m v^2$$

$$= \frac{1}{2} \frac{1}{4\pi\epsilon_0} \frac{ze^2}{r}$$

$$E_{pot} = -2 E_{kin}$$

$$E_{pot} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{ze^2}{r}$$

$$\frac{1}{s} = \frac{1}{s} + \frac{1}{s'}$$

$$F_2 = \frac{F_L}{2}$$

$$E = F_2 \cdot s$$

$$= \frac{F_L}{2} \cdot u \cdot h$$

$$F_L = F_L \cdot h$$

$$= m \cdot g \cdot h$$

$$s = u \cdot h$$

$$b = b_2 + \mu_0 u = b_2 (1 + \lambda u_y)$$

$$E = c b$$

$$= \mu_0 c u h J = \mu_0 J$$

$$m_1 v_{1x} + m_2 v_{2x} = m_1 v_{1x}' + m_2 v_{2x}'$$

$$\frac{1}{2} m_1 v_{1x}^2 + \frac{1}{2} m_2 v_{2x}^2 = \frac{1}{2} m_1 v_{1x}'^2 + \frac{1}{2} m_2 v_{2x}'^2$$

$$= \frac{1}{2} m_1 v_{1x}^2 + \frac{1}{2} m_2 v_{2x}^2$$

$$F_s = \frac{m g}{\cos\theta}$$

$$F_s = \frac{m g}{\cos\theta}$$

$$F_s = \frac{m g}{\cos\theta}$$



Chapter 13: The Electric Field

- Concept of “fields” (dividing out the object contribution)

$$\vec{\mathbf{E}} = \frac{\vec{\mathbf{F}}}{q}$$

- Electric fields due to point charges

$$\vec{\mathbf{E}} = \frac{1}{4\pi\epsilon_0} \frac{q}{|\vec{\mathbf{r}}|^2} \hat{\mathbf{r}}$$

- Superposition of electric fields (they just add!)
- Dipoles
- Included HW1-3, VHW1



Chapter 14: E-Field Interactions

- Charge is conserved
- Differences between conductors and insulators
- How to charge objects
- Polarization of Insulators
 - Induced dipoles
- Polarization of Conductors
 - Electron Sea
 - Drift Speeds
 - Electric field inside conductors
- Included HW4,5, VHW2,3



Chapter 15: Charge Distributions

- For any distribution:
 - Divide into small pieces
 - Determine direction and expression for $\Delta \vec{E}$
 - Add up all contributions
 - Check yourself!
- Looked at electric fields due to:
 - Charged lines
 - Charged rings
 - Charged surfaces
 - Charged shells and spheres
- Introduction to capacitors
- Included HW6,7, VHW4



Chapter 16: Electric Potential

- Relation to potential energy

$$\Delta U = q\Delta V$$

- Potential Difference in electric field

$$\Delta V = - \sum \vec{\mathbf{E}} \cdot d\hat{\ell} = - \int \vec{\mathbf{E}} \cdot d\hat{\ell}$$

- Relation to electric fields:

$$E_x = -\frac{\partial V}{\partial x}, \quad E_y = -\frac{\partial V}{\partial y}, \quad E_z = -\frac{\partial V}{\partial z}$$

- Potential differences add
- Path independent
- Potential at single location defined with respect to infinity
- Dielectrics
- Included HW8-10



Chapter 17: Magnetic Fields

- Need moving charges

$$\vec{\mathbf{B}} = \frac{\mu_0}{4\pi} \frac{q\vec{\mathbf{v}} \times \hat{\mathbf{r}}}{|\vec{\mathbf{r}}|^2}$$

- Definition of current

$$I = |q|nA\bar{v}$$

- Magnetic fields due to currents

$$\Delta\vec{\mathbf{B}} = \frac{\mu_0}{4\pi} \frac{I\Delta\hat{\ell} \times \hat{\mathbf{r}}}{|\vec{\mathbf{r}}|^2}$$

- Magnetic field due to current distributions: line current, loop of current (magnetic dipole)
- No magnetic monopoles!
- Included HW11,12



Chapter 18: Electric Fields and Circuits

- Equilibrium vs Steady State
- Current Node Rule: What goes in must come out
- Electric field and drift speed related

$$\bar{v} = u\vec{E}$$

- Charge buildup on wire surfaces
 - Same current throughout the circuit
 - E Field always points in direction of current
- Loop Rule: $\Delta V = 0$ along any closed path in a steady state circuit
- Role of batteries
- Included HW13,14



Chapter 19: Capacitors and Resistors

- Defining capacitance

$$Q = C|\Delta V|$$

- How capacitors add in circuits
- Charge the same in capacitors in series, voltage the same in capacitors in parallel
- Resistance

$$R = \frac{L}{\sigma A}$$

- Dependence on microscopic properties
- How resistors add in circuits
- Power in circuits

$$\text{Power} = I\Delta V$$

- Real batteries
- Included HW15, VHW5,6



Chapter 20: Magnetic Forces

- Magnetic Force:

$$\vec{\mathbf{F}} = q\vec{\mathbf{v}} \times \vec{\mathbf{B}} = I\Delta\vec{\ell} \times \vec{\mathbf{B}}$$

- Determining circular motion and properties
- The Hall Effect
- Motional Emfs
 - Motion of conductor in magnetic field creates force
 - Force separates charges, creates ΔV , so current flows
 - Current flowing creates opposing force
 - Converts between mechanical and electrical energy
- Included HW16-18



Chapter 21: Gauss and Ampere

- Electric Flux

$$\Phi_E = \int \vec{\mathbf{E}} \cdot \hat{\mathbf{n}} dA$$

- Gauss's Law

- Electric flux through a closed surface proportional to the charge enclosed

$$\oint \vec{\mathbf{E}} \cdot \hat{\mathbf{n}} dA = \frac{Q_{enc}}{\epsilon_0}$$

- Ampere's Law

- The sum of magnetic fields around a loop is proportional to the current enclosed

$$\oint \vec{\mathbf{B}} \cdot d\hat{\ell} = \mu_0 I_{enc}$$

- Included HW19, VHW7



Chapter 22: Faraday's Law

- Magnetic Flux

$$\Phi_B = \int \vec{\mathbf{B}} \cdot \hat{\mathbf{n}} \, dA$$

- Faraday's Law:

- Changes in magnetic flux create curling electric fields

$$\oint \vec{\mathbf{E}} \cdot d\hat{\ell} = -\frac{d}{dt} \int \vec{\mathbf{B}} \cdot \hat{\mathbf{n}} \, dA$$

- If a conductor surrounds the loop, can get an emf:

$$\mathcal{E} = -\frac{d\Phi_B}{dt}$$

- Also relates to motional emfs
- Included HW20



Chapter 23: Radiation

- Maxwell-Ampere's Law
 - Adds correction term for changing electric flux

$$\oint \vec{\mathbf{B}} \cdot d\vec{\ell} = \mu_0 \left(I_{enc} + \epsilon_0 \frac{d\Phi_E}{dt} \right)$$

- Light Waves are self-propagating electromagnetic fields
 - $\vec{\mathbf{E}}$ crossed with $\vec{\mathbf{B}}$ points in direction of wave travel
 - $|\vec{\mathbf{E}}| = c|\vec{\mathbf{B}}|$
 - Waves travel at the speed of light
- Created by accelerating charges
 - Create ripple in electric/magnetic fields
- Poynting Vector contains information about wave energy

$$\vec{\mathbf{S}} = \frac{1}{\mu_0} \vec{\mathbf{E}} \times \vec{\mathbf{B}}$$

- Included HW21-23



Supplementary: Optics

- Sinusoidal waves

$$f = A \cos(\omega t - kx - \phi_0)$$

- Waves travel slower or faster in different materials

$$n = \frac{c}{v}$$

- Snell's Law

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

- Interference

$$\Delta(\text{phase}) = k\Delta x + \Delta\phi_0 = \begin{cases} \pm 2\pi m & \text{constructive} \\ \pm 2\pi(m + \frac{1}{2}) & \text{destructive} \end{cases}$$

- Special Lens Rays
- Included HW24, VHW8



Class Picture!

- I always take an end-of-semester class picture in each class I teach
- Unfortunately we can not gather together this year, so if you would be so kind to take a snapshot of yourself with your webcam or phone at the moment and email it to me, I'm going to compile them all together so I have something from this class for this semester!
- Do it now so you don't forget!



Final Plans

- Due on **Saturday by noon**
- I'm going to be posting more formal instructions by this evening but the main gist is:
 - One video solution for a problem I will give you from this latest section on optics and waves
 - 4 test questions written by you for me from objectives from the entire rest of the semester
 - Choose the 4 objectives you feel to be the most important / capture the essence of what you were supposed to learn in this class. In your solution key, take a sentence or two to justify why you chose this objective and felt it to be of this importance.
 - There are lots of fine answers here, but there are some objectives I would definitely raise my eyebrows at unless you explained yourself *REALLY* well.
 - If it is the same objective as one you already did, then ok, but the question needs to be new
 - Should still be valid *test* questions, so capable of being done in 10 minutes.
 - Still need to submit your solution key separately.



So long! Farewell!

Thank you all so much for the lovely and *memorable* semester!
Stay healthy!