



- Webwork due on Wednesday
- Test 3 on Friday!
  - Review questions, old test, and all accompanying solutions posted
  - Equation sheet also updated
  - Covers Lectures 21–30
    - Corresponds to Chapter 15-24 (minus Ch 20)
  - Email me if you need to borrow a calculator!
- Polling: `rembold-class.ddns.net`





What happens as a white dwarf star gains enough mass to equal the Chandrasakhar Limit?

- A. Carbon fusion ignites in the star, causing a supernova
- B. Hydrogen fusion ignites in a shell around the star, causing a small nova
- C. The star collapses into a neutron star, giving off a tremendous amount of energy in the process
- D. Rotational forces rip the star apart, scattering its gases



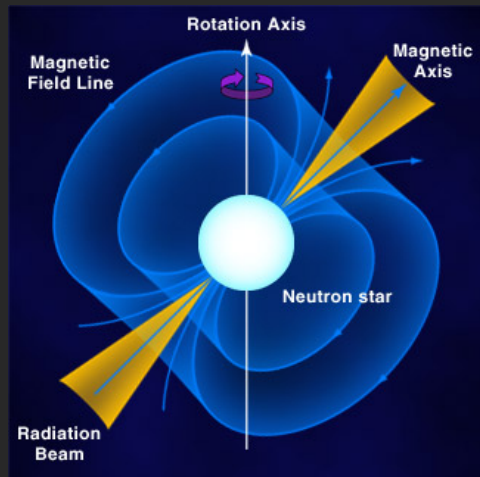
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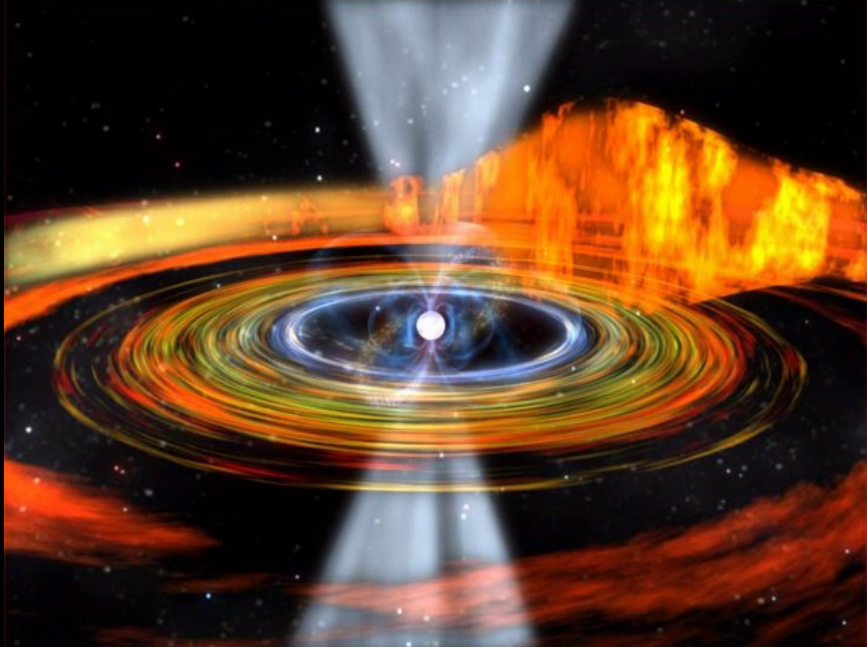
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# Structure of a Pulsar



- Strong magnetic fields focus outgoing radiation
- Results in a “lighthouse” effect
- Spins very fast due to conservation of angular momentum
- Rapid spinning causes these beams of radiation to sweep across us





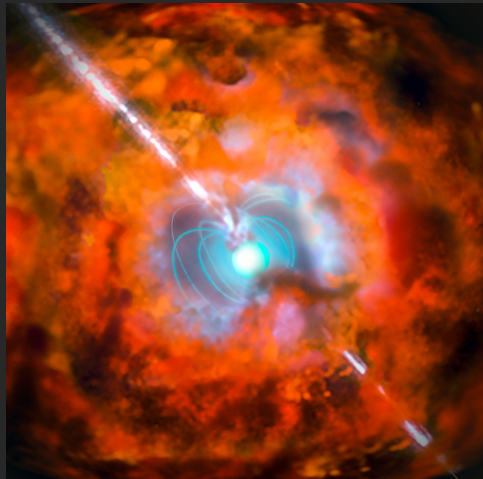


- Isolated pulsars will eventually slow as they lose angular momentum and energy to the outgoing gases
- Pulsars as part of binary systems may actually speed up
  - A steady diet of more mass lends more angular momentum
  - Can end up pulsing every few thousandths of a second
- There is a rotational speed limit
  - If you spin too fast, gravity can't keep everything contained
  - Is what tells us pulsars must be neutron stars and not white dwarfs

# Magnetars



- When spin, temperature, and magnetic field combine in the right combination
- Magnifies magnetic field: creates a dynamo
- Magnetic fields up to  $10^{11}$  teslas
  - Earth magnetic field:  $5 \times 10^{-5}$  T
  - We can't create more than maybe 100-1000 T without ripping apart our machines
- 1 in 10 supernova could create?





# The Power of the (Magnetic) Force



- Magnetic fields create forces on moving charges
  - Say, for instance, the protons and electrons in atoms
- Getting a moon distance away would wipe all your credit cards
- Getting within several thousand kilometers would render all your biochemistry useless
- Getting within 1000 kilometers and your molecular structure just kinda... dissolves!





- Crust of magnetar and the magnetic field are locked together
  - Changing one changes the other. . .
- Crust is under huge pressure from gravity, rotation, and the magnetic field
- A tiny slip, even just a centimeter, releases an insane amount of energy
  - Force the magnetic field to “slip” as well
  - Equivalent to a solar flare, just far, far, far more energetic
- Swift: 2004
  - Designed to look at high energy x-ray sources
  - Wasn't even looking in the direction of the magnetar flare
  - The amount of radiation swamped and oversaturated all its sensors
  - Compressed the Earth's magnetic field and ionized upper atmosphere
  - All from 50,000 light-years away. . .
- Thankfully, these are rare



# The Great Escape



- Let's talk the speed required to escape an gravitational mass
- Should depend on the mass of the object and our initial distance away from it
- If we want to barely escape, then we need our final velocity to be 0

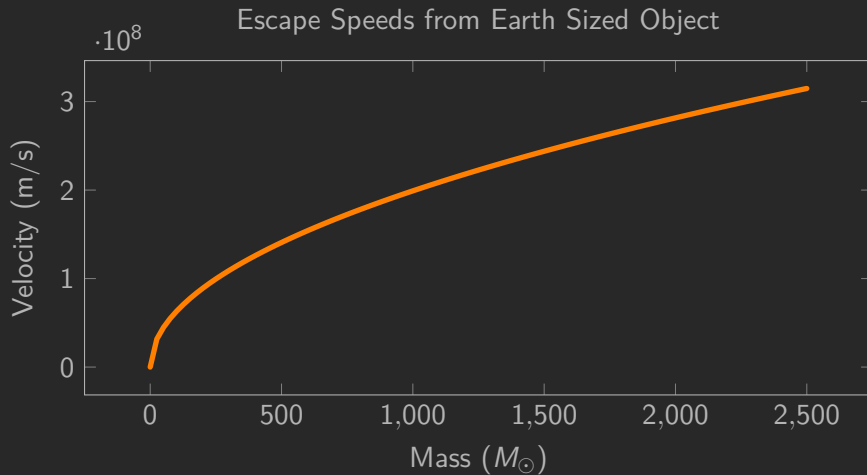


- Let's talk the speed required to escape an gravitational mass
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- This requires that:

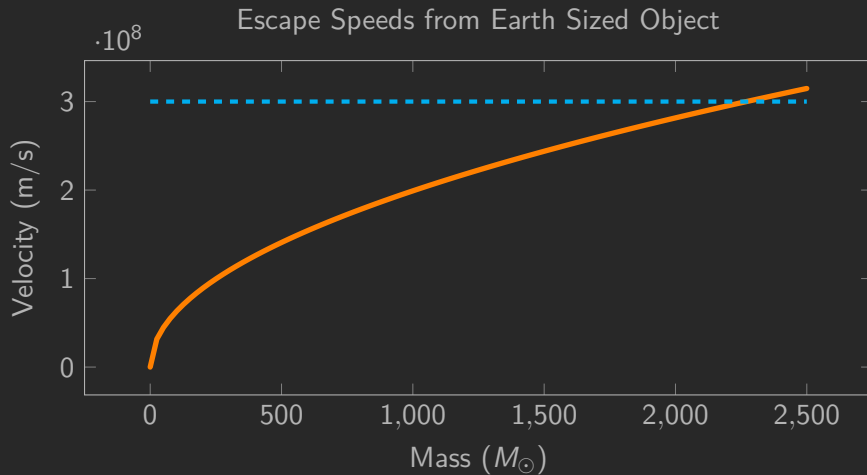
## Escape Speed

$$v = \sqrt{\frac{2GM}{R}}$$

# Making the Escape



# Making the Escape



# The Point of No Escape



- Since nothing can go faster than light, for any mass there exists a radius from whence nothing could escape!
- Rewriting our escape velocity:

$$c^2 = \frac{2GM}{R}$$
$$R = \frac{2GM}{c^2}$$

- This radius is called the Schwarzschild radius
- Even light couldn't escape from within this radius
- Makes it "Black"
- And thus we have a theoretical "Black Hole"
- In actuality, created when collapsing stars mass great enough to overcome neutron degeneracy



# Some Examples



## Example

What is the Schwarzschild radius for our Sun? ( $M_{\odot} = 2 \times 10^{30} \text{ kg}$ )

## Example

What is the Schwarzschild radius of YOU? ( $M = 70 \text{ kg}$ )



## Example

What is the Schwarzschild radius for our Sun? ( $M_{\odot} = 2 \times 10^{30}$  kg)

$$R = \frac{2(6.67 \times 10^{-11})(2 \times 10^{30})}{(3 \times 10^8)^2} = 2964 \text{ m}$$

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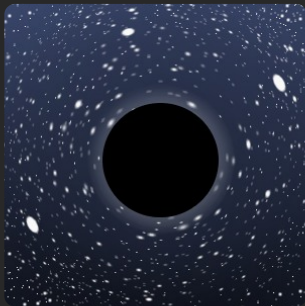
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## Example

What is the Schwarzschild radius of YOU? ( $M = 70$  kg)

$$R = \frac{2(6.67 \times 10^{-11})(70)}{(3 \times 10^8)^2} = 1 \times 10^{-25} \text{ m}$$

# The Event Horizon



- Since no light can escape, it is impossible for us to see any events that happen within the Schwarzschild radius
- It is as if they were “beyond the horizon”
- Another name for the Schwarzschild radius is the **Event Horizon**
- Both describe the point at which light can no longer escape
- Commonly imagined as the “edge” of the black hole



You know that the event horizon of a particular black hole has a radius of 30 km. How massive is the black hole (in solar masses)?

( $G = 6.67 \times 10^{-11}$ ,  $M_{\odot} = 2 \times 10^{30}$ ,  $c = 3 \times 10^8$ )

- A.  $(3.4 \times 10^{-8})M_{\odot}$
- B.  $0.01M_{\odot}$
- C.  $10M_{\odot}$
- D.  $(2 \times 10^{31})M_{\odot}$



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  - Utterly, utterly false. Our Sun has nowhere near the mass needed to push past both the electron and neutron degeneracy pressures to form a black hole.
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- Black Holes are the universe's vacuum cleaners, sucking in all their surroundings
  - Nope! Black holes have a lot of mass and gravity, but if you are far away that's all you see. We could happily keep orbiting the Sun even if it were to pop into a black hole this instant!



- Stellar Mass Black Holes
  - Generally several solar masses to a dozen or so
  - Results in fairly small event horizons
- Supermassive Black Holes
  - Many times larger than the Sun
  - Anchor the center of many galaxies
  - The one at the center of the Milky Way is estimated at  $4,300,000 M_{\odot}$ !!
  - May actually be crucial to galaxy formation



So what happens as you fall into a black hole?



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YOU DIE!



So what happens as you fall into a black hole?

**YOU DIE!**

But what about in the meanwhile? What would happen?

# Tidal Spaghetti



- Recall that the gravity of Jupiter exerts tidal forces on Io
  - Squeeze and stretch the moon
- Black holes have MUCH more gravity
  - And thus MUCH stronger tidal forces!
- Your feet would feel a force thousands of times more than your head!
  - Get stretched!
- Process known as:

# Tidal Spaghetti

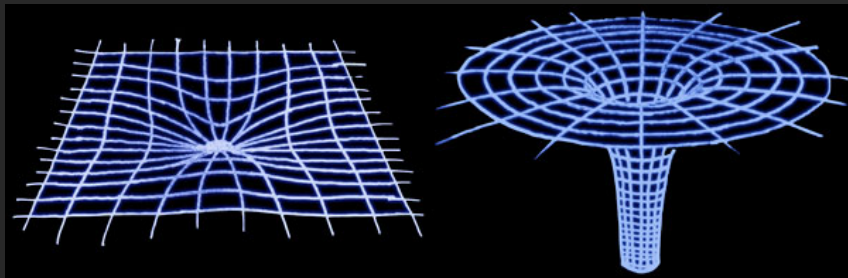


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## Spaghettification!



- Einstein showed that space and time are both related
- Can envision as a two dimensional rubber sheet
- Large masses cause indentations in the sheet and bend the trajectories of objects near them
- Since space and time are related, the more space you cross, the slower time ticks







- As you approach a black hole, the curvature of space-time becomes extreme
- As viewed from the outside your time slows down!
  - Can also envision as the light emitted each second takes longer and longer to reach the observer.
  - YOUR time, as far as you are concerned, does not change
- Outsider observer never sees someone cross the event horizon
- The traveler sees the opposite
  - Looking outward, time appears accelerated
  - Would see the entire future of the universe before crossing the event horizon