- 1. Determine the number of edges in a complete graph on n vertices.
- 2. Let $d \in \mathbb{N}$ and $V = \{0,1\}^d$. That is, V is the set of all binary sequences of length d. Define a graph on V in which two sequences form an edge if and only if they differ in exactly one position. (This graph is called the **d-dimensional cube**.)
 - (a) Draw and label the vertices of the 1-, 2-, and 3-dimensional cube.
 - (b) Determine the average degree, number of edges, diameter, girth and circumference of the *d*-dimensional cube.
- 3. Let G be a graph containing a cycle C, and assume that G contains a path of length at least k between two vertices of C. Show that G contains a cycle of length at least \sqrt{k} .
- 4. Proposition 1.3.2 states that . Is this bound best possible? Prove your answer is correct.
- 5. Show that for every graph G, $rad(G) \leq diam(G) \leq 2rad(G)$.