

1. Determine the number of edges in a complete graph on n vertices.
2. Let $d \in \mathbb{N}$ and $V = \{0, 1\}^d$. That is, V is the set of all binary sequences of length d . Define a graph on V in which two sequences form an edge if and only if they differ in exactly one position. (This graph is called the **d -dimensional cube**.)
 - (a) Draw and label the vertices of the 1-, 2-, and 3-dimensional cube.
 - (b) Determine the average degree, number of edges, diameter, girth and circumference of the d -dimensional cube.
3. Let G be a graph containing a cycle C , and assume that G contains a path of length at least k between two vertices of C . Show that G contains a cycle of length at least \sqrt{k} .
4. Proposition 1.3.2 states that every graph G containing a cycle satisfies $g(G) \leq \text{diam}(G) + 1$. Is this bound best possible? Prove your answer is correct.
5. Show that for every graph G , $\text{rad}(G) \leq \text{diam}(G) \leq 2\text{rad}(G)$.