Wed 30 Aug Reminders/Announcements

- · HWI due Thurs. Sept 7 (allows for Q's on Wed)
- · Recordings + Class Notes to appear in Canvas / Webpage

For \$1.1, narrow focus to immediate needs.

Think of this as a future resource

$$[EX]$$
 $A = \{a,b,c,d,e\}$, then $\{a,b,c\} \notin [A]^3$
 $[A]^3 = (5) = 5! = 10$ $\{a,b\} \notin [A]^3$

def: A graph
$$G = (V, E)$$
 is a pair of sets such that $E \subseteq [V]^2$ unordered all of elements in E are spairs of elements in V

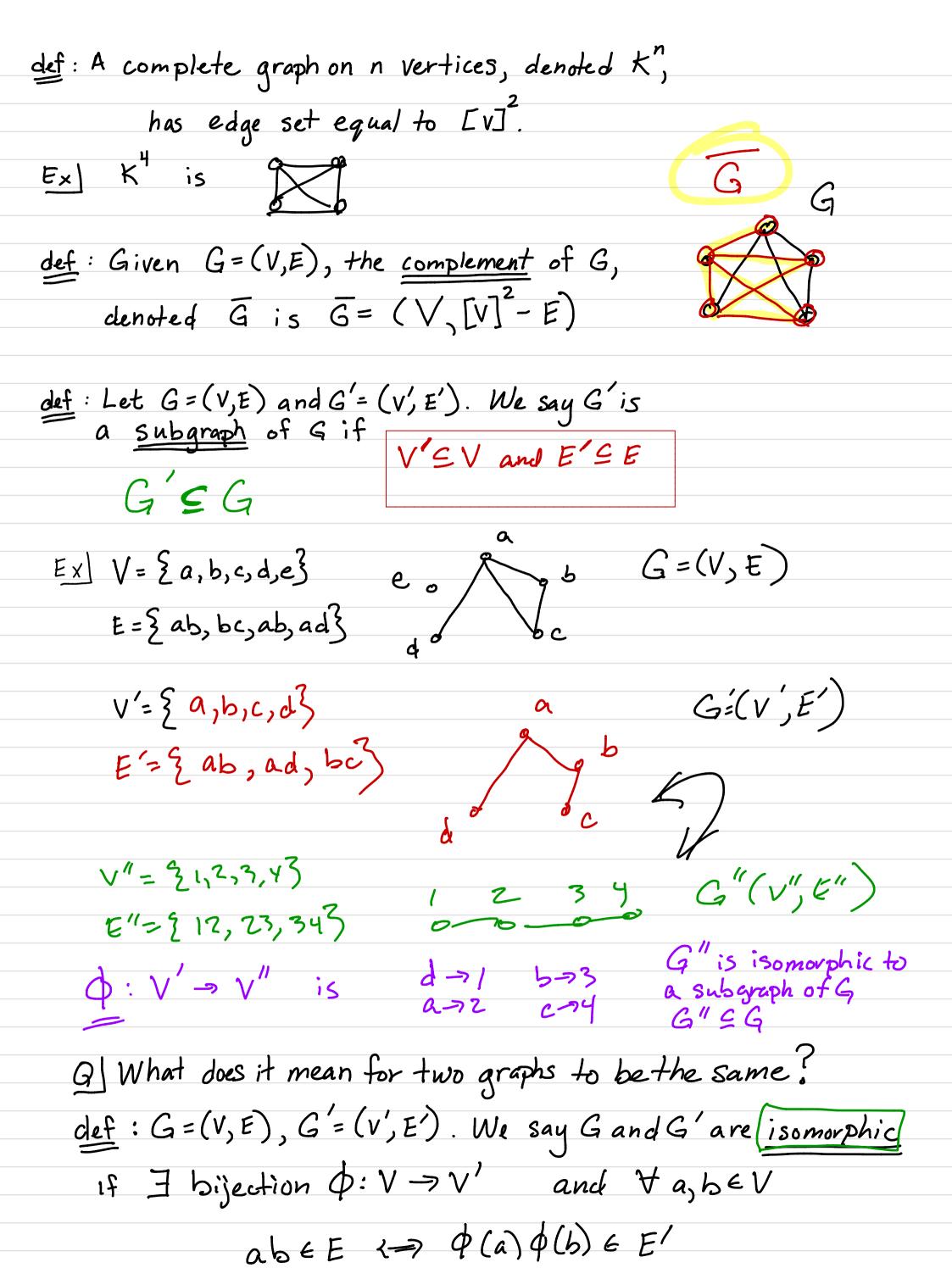
Ex Let
$$G = (V, E)$$
 be defined as $V = \{\{\{a,b\}, \{\{b,c\}\}, \{\{a,c\}\}, \{\{a,d\}\}\}\}$

$$= \{ab, bc, ac, ad\}$$

$$\frac{def}{|G|} : G = (V, E)$$

$$|G| = |V| \quad \text{the order of } G$$

$$|G|| = |E| \quad \text{the index of } G$$





<u>defs</u>: G=(V, E) s.t. |V| >0; v EV

min { d(v) ; ve V 5

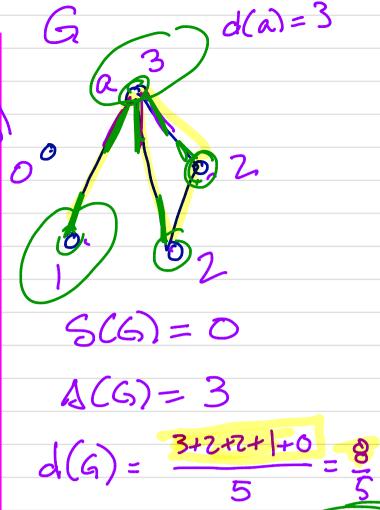
- A graph is K-regular if
$$d(v)=K$$
 $\forall v\in G$.

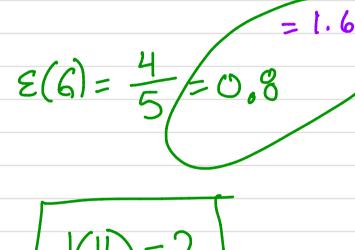
$$E(G) = \frac{|E|}{|V|} = \frac{1}{2} \sum_{x} d(x)$$
 $= \frac{1}{2} d(G)$
 $S(G) = \frac{1}{2} \sum_{x} d(x)$

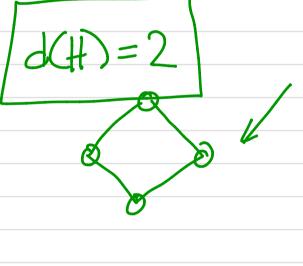
$$S = \frac{|V| \cdot S}{|V|} = \frac{Z}{V} \frac{S(G)}{|V|} = \frac{Z}{V} \frac{d(G)}{|V|} \leq \frac{Z}{V} \frac{d(G)}{V} \leq \frac{Z}{V} \frac{d(G)}{$$

· How to relate | E | and vertex degrees?

$$|E| = \left(\frac{1}{2}\right) \sum_{v \in V} d(v)$$







* Prop 1.2.1 In any graph G, the number of vertices of odd degree is EVEN Pf: | E | = 1 \(\sum_{10} \) | \(\text{Since} \) | \(E \) | \(\text{and} \) \(\sum_{10} \) \(\text{are} \) Integres, then Zd(v) is even. But Zd(v) is a sum of integres that is even, so it must have an even # of odd entries. Prop 1.2.2 For G=(V, E) s.t. | E| >0, 3 H = G s.t. S(H) > E(H) = E(G) OR S(H) > = d(H) = = d(G). Build a graph such that E(G) 76 and S(G)=2. In addition, G has 10 vertices w/d(v)=2. = d(G) = E(G) ≥ 6 ← d(G) ≥ 12 20+20.3 = 80 24 d(v)=9K10 W/ 10 860722/

10.9

