

1. For every  $a, b, c \in \mathbb{N}$ ,  $\text{lcm}(ca, cb) = c \cdot \text{lcm}(a, b)$ .

2. Every multiple of 4 can be written in the form  $1 + (-1)^n(2n - 1)$ .

3. For every integer  $n$ ,  $n^2 + 3n + 3$  is odd.

4. Let  $a, b \in \mathbb{N}$ . If  $\gcd(a, b) > 1$ , then  $b \mid a$  or  $b$  is not prime.  
(First, think about your logical **strategy**.)