

§3.6: What to do about derivatives of functions like...

$$y = (x^2 + 1)^{10} \quad \text{or} \quad y = \sin(4x + 3)$$

What is this called when "inside" + "outside".

How can you know that

$$\frac{d}{dx} [f(g(x))] \neq f'(g'(x))$$

$$y = (x^2 + 1)^2 = x^4 + 2x^2 + 1$$

$$y' = 4x^3 + 4x \quad \checkmark$$

try our fantasy formula:

$$y' = 2(2x)' = 4x$$

Nope ☹

Extras:

$$y = (x \sin(x))^5$$

$$y = \left( \frac{x}{x + \sin x} \right)^5$$