University of Antwerp
Faculty of Social Sciences

Objective rating method: Entropy

Speech intelligibility estimation

Jose Rivera

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What are we going to talk about?

1. Preliminars

Research question

Research question

On two fronts:

1. Can comparative judgement (CJ) methods be used to assess speech intelligibility (SI)?,
   To investigate this wee need:
   - an objective measure of SI
2. where CJ stands versus absolute holistic judgement (HJ) methods?,
   In terms of:
   - validity
   - reliability
   - statistical efficiency
   - time efficiency

Objective measure of SI

the most objective measure of SI (we know of) comes from a transcription task:

1. transcribing children's utterances (made by multiple judges),
2. align transcriptions at the utterance level,
3. calculate an entropy measure (H), defined as

$$H = H(\mathbf{p}) = \frac{-\sum_{i=1}^{n} p_i \cdot \log_2(p_i)}{\log_2(N)}$$

4. characteristics of H [1, 2]
   - bounded in $[0, 1]$ space,
   - utterances with more agreement are more intelligible, and therefore $H \to 0$,
   - utterances with low agreement are less intelligible, and therefore $H \to 1$.

1. Preliminars

Research hypothesis production

A typical scientific lab[1]

What is needed?

1. Quality of theory
2. Quality of data
3. Reliable procedures and code
4. Quality of data analysis
5. Documentation
6. Reporting

What we will deal with:

1. Quality of theory
2. Quality of data
3. Reliable procedures and code
4. Quality of data analysis
5. Documentation
6. Reporting

[1] McElreath [5], lecture 20 and McElreath [6], chapter 17

Research hypothesis production[2]

Well known challenges

- Insufficient data
- Wrong population
- Measurement error
- Selection bias
- Confounding

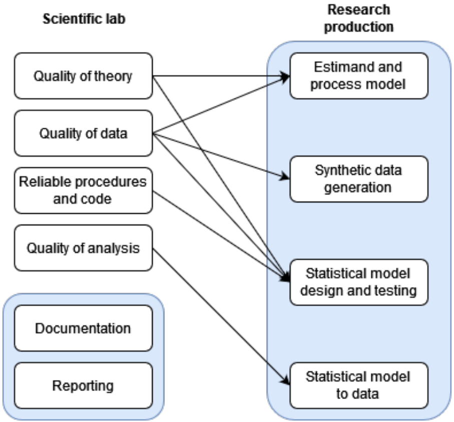
Known challenges in our research;

- Insufficient data (possibly)
- Wrong population
- Measurement error
- Selection bias
- Confounding

[2] Hernán [4], lesson 4

Research hypothesis schematics[3]

a. Estimand and process model
b. Synthetic data generation
c. Statistical model design and testing
d. Apply statistical model to data



[3] McElreath [6], lecture 20, Pearl [9]. Follow Fogarty et al. [3] on item (c).

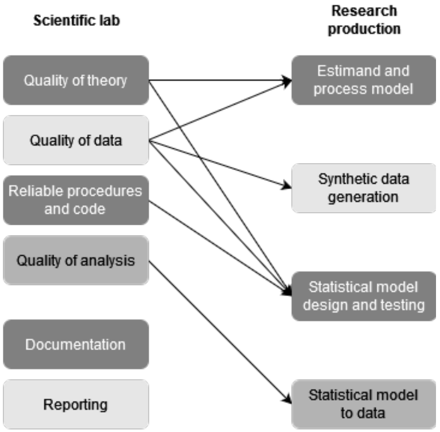
Why do we need to follow this?

Because the improvement of:

- A clear definition of the estimand and process model (assumptions).
- An improved the reliability of your procedures.
- As a documentation procedure.

leads to:

- A sound analysis, and sound results (even when we cannot answer our question).
- An improved planning to get data.

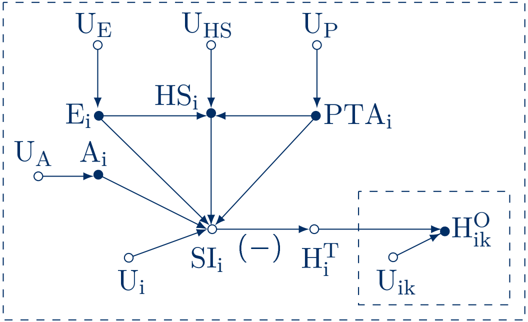


2. Estimand and Process model

The theory behind our research

- H_{ik} = (observed) entropy replicates
- H_i = (latent) child's entropy
- SI_i = (latent) child's SI score (inversely related to H_i^T)
- A_i = child's "hearing" age
- E_i = child's etiology of disease
- HS_i = child's hearing status
- PTA_i = child's pure tone average
- variables assumed independent, beyond the described relationships,

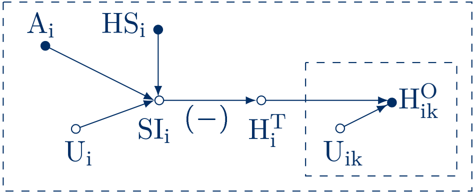
$$
\begin{aligned}
P(\mathbf{U}) &= P(U_{ik}, U_i, U_A, U_E, U_{HS}, U_P) \\
&= P(U_{ik})P(U_i)P(U_A)P(U_E)P(U_{HS})P(U_P)
\end{aligned}
$$



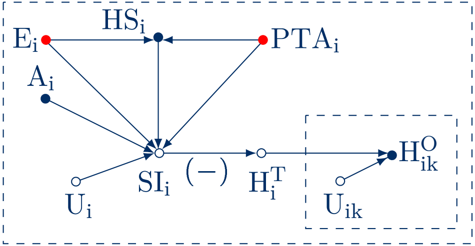
General causal diagram

Interested in two effects

1. total effects model inherits:
   - children's characteristics that lead to the fitting of specific apparatus,
   - the (convenience of) sample selection (fixed with post-stratification)
2. to do the last, we stratify for all variables that explain variability, ergo, use a direct effects model
3. We have two levels: replicates (k), child's level (i), denoted by squares
4. U_{ik} = replicates measurement error
   U_i = within child SI variability



(b) total effects



(a) direct effects

Causal and probabilistic model

$$
\begin{aligned}
H^O_{ik} &\sim \text{BetapProp}(H^T_i, df_{ik}) \\
H^T_i &= \text{inv\_logit}(-SI_i) \\
SI_i &\sim \text{Normal}(\mu_{SI}, \sigma_{Ui}) \\
&\quad \mu_{SI} = a_i + \alpha + \alpha_{HS[i]} + \alpha_{E[i]} \\
&\qquad + \beta_{A,HS[i]}(A_i - \bar{A}) + \beta_P PTA_i \\
HS_i &\sim \text{data} \\
A_i &\sim \text{data} \\
E_i &\sim \text{data} \\
PTA_i &\sim \text{data} \\
U &\sim \text{unobservable}
\end{aligned}
$$

(a) general probabilistic model

$$
\begin{aligned}
H^O_{ik} &\leftarrow f(H^T_i, U_{ik}) \\
H^T_i &\leftarrow f(SI_i) \\
SI_i &\leftarrow f(HS_i, A_i, E_i, PTA_i, U_i) \\
HS_i &\leftarrow f(U_{HS}) \\
A_i &\leftarrow f(U_A) \\
E_i &\leftarrow f(U_E) \\
PTA_i &\leftarrow f(U_P) \\
U &\sim P(\mathbf{U})
\end{aligned}
$$

(a) general structural model

3. Synthetic data generation

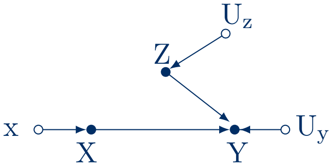
Intervention

- Purpose: to keep a control on all the factors responsible for the outcome's variation blue(understand the system).
- It is modeled by modifying the structural model (and causal diagram).
- remember: $\mathbf{V} = \{Z, X, Y\}$, $\mathbf{U} = \{U_z, U_x, U_y\}$, and $\mathbf{F} = \{f_z, f_x, f_y\}$.
- Intervention on X can be written in do-calculus[a] as: $P(\mathbf{V} \mid do(X = x))$.

[a] we are not delving into this (the usual suspects [7, 8, 10, 11])

$$M = \begin{cases} Z \leftarrow f_z(U_z) \\ X \leftarrow f_x(U_x) \\ Y \leftarrow f_y(X, Z, U_y) \\ U \sim P(\mathbf{U}) \end{cases}$$

(a) structural model



(b) causal diagram

4. References

4. References

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