# Speech intelligibility measurement

# A latent variable approach on utterances' transcriptions

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## **Abstract**

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### 1. Introduction

Intelligible speech can be defined as the extent to which the elements in an speaker's acoustic signal, e.g. phonemes or words, can be correctly recovered by a listener [47, 73, 70, 36]. Because intelligible spoken language requires all core components of speech perception, cognitive processing, linguistic knowledge, and articulation to be mastered [36], its attainment carries an important societal value, as it is a milestone in children's language development, the ultimate checkpoint for the success of speech therapy, and has been qualified as the 'gold standard' for assessing the benefit of cochlear implantation [13].

The literature suggest two perspectives from which speech intelligibility can be assessed: the message and listener's perspective [4, 5]. The first, also known as acoustic studies, is focused on assessing separately particular characteristics of the speech samples, e.g. their pitch, duration or stress (supra segmental characteristics), or the articulation of vowels and consonants (segmental characteristics) [63]. Whereas the second, also known as perceptual studies, is centered on making holistic assessments of the speech stimuli, e.g. measure their perceived quality [4, 5]. On both instances, the stimuli (children's utterances) can be generated from reading at loud, contextualized utterances, or spontaneous speech tasks<sup>1</sup>.

Furthermore, perceptual studies can use multiple approaches to measure intelligibility, but they can be largely grouped into two: objective and subjective ratings [45]. In *objective rating* methods, listeners transcribe the children's utterances orthographically or phonetically, and use such information to construct a score. In that sense, in the transcription task, intelligibility can be inferred from the extent a set of transcribers can identify the word contained in an utterance [5]. In contrast, under *subjective rating* methods, listeners directly infer the utterance's intelligibility score through specific procedures, e.g. absolute holistic, analytic, or comparative judgments, among others.

It is easy to deduce that *objective rating* methods produce more valid<sup>2</sup> and reliable<sup>3</sup> scores than its *subjective* counterpart, and as a result, are usually used as an objective measure of intelligibility [5, 27].

Accompanying the intelligibility assessment methods, the literature supply a myriad of factors that are thought also contribute to the (under)development of intelligible spoken language [57, 6, 40, 28]. Among these are audiology related factors, such chronological age, age at implantation, the duration of device use, hearing age, bilateral or contralateral cochlear implantation, and the children's preoperative and postoperative hearing levels. On the other hand, there are also child related factors, such as the cause of the hearing impairment (genetic, infections), additional disabilities (mental retardation, speech motor problems), and gender. Finally, there are also environmental factors, such as communication modality.

Considering all of the above, this paper seeks to investigates the speech intelligibility levels of normal hearing (NH) versus hearing-impaired children with cochlear implants (HI/CI). For that purpose, ten utterances recordings, from thirty two NH and HI/CI children, were selected from a large corpus of *spontaneously spoken speech* collected by the CLiPS research center. Additionally, we set up an experiment, where one hundred language students transcribed each stimuli to the Qualtrics environment [77]. Finally, the transcriptions were transformed into an entropy measure per utterance, which served as our outcome variable.

We believe this paper make three specific contributions to the understanding of the factors that drive the intelligibility of spoken language. First, we develop a novel analysis using a latent variable approach [26]. More specifically, we model *speech intelligibility* as a latent variable that can be inferred from the entropy replicates. This method offers three specific benefits. On the one hand, the method 'constructs' an intelligibility score, which in turn, allow us to test different hypothesis and even make individual comparisons at the appropriate level. On the other hand, it allow us to control for different sources of variation. This is particularly important as, by failing to account for the appropriate hierarchies in the data, we could be 'manufacturing' false confidence in the parameter estimates, leading us to incorrect inferences [53]. Finally, the method also provides a 'criterion' on how reliable are the entropy replicates to measure speech intelligibility.

Second, we use Directed Acyclic Graph (DAG) [59, 17] to depict all the relevant variables though to influence speech intelligibility. We describe in detail our causal and non-causal hypothesis, and supplement our description with a causal diagram. The benefit of the method lies, not only, in that it makes the assumptions of our hypothesis more transparent, but also allow us to derive statistical procedures from the aforementioned causal assumptions [53, 79, 62].

 $<sup>^1\</sup>mathrm{ordered}$  on increasing level of ecological validity [32, 25]

<sup>&</sup>lt;sup>2</sup>the extent to which scores are appropriate for their intended interpretation and use [50, 68].

<sup>&</sup>lt;sup>3</sup>the extend to which a measure would give us the same result over and over again [68], i.e. measure something, free from error, in a consistent way.

Third and final, we wrap the analysis procedure under the Bayesian framework, providing the assumptions, and the steps required to reproduce the computational implementation of the models.

### 2. Materials and Methods

We set up an experiment where speech samples were transcribed by a group of listeners. The current section succinctly describes the participating children, the stimuli used, and the experimental setup, while also delve into the causal and statistical framework of analysis.

#### 2.1. Children

Thirty two children were selected using a large corpus of spontaneously spoken speech, collected by the Computational Linguistics, Psycholinguistics and Sociolinguistics research center (CLiPS). The selection followed a two step procedure [27]. First, a sample of sixteen hearing-impaired children (ten boys, six girls) were selected based on the quality of their registered stimuli. Second, an additional matched sample of sixteen hearing children was also selected (six boys, ten girls), and served as a comparison group.

For the first group, all the hearing-impaired children with cochlear implants (HI/CI) were native speakers of Belgian Dutch, living in Flanders, the Dutch speaking area of Belgiam. They were all raised orally using monolingual Dutch, with a limited support of signs. All of the children were screened by the Universal Neonatal Hearing Screening (UNHS), using an automated auditory brainstem response hearing tests for newborns, and all received the cochlear implantation before the age of two. Their medical and audiological records did not ascertain any additional health or developmental issues. Hence, no known additional comorbidities were though present. Finally, at the date of the measurement, they were all enrolled in the mainstream educational system.

For the second group, the sixteen normal hearing children (NH) were closely matched to the HI/CI group based on chronological age. All children were also native speakers of Belgian Dutch, and enrolled in the mainstream educational system. None reported hearing loss or additional disabilities, judged from the UNHS screening procedure and their respective parental report.

The characteristics of the selected children is detailed in Table 3, in the supplementary section A.1.

## 2.2. Stimuli

The stimuli consisted of children's utterances, i.e. sentences of similar length, recovered from previously mentioned CLiPS corpus. More specifically, we use a portion of the corpus that consisted of ten utterances recordings for each of the thirty two selected children, adding to a total of 320 stimuli.

The stimuli were documented when the child was telling a story cued by the picture book 'Frog, where are you' [52] to a caregiver 'who does not know the story'.

The recordings were orthographically transcribed with the CLAN editor in CHAT format [51]. The quality of the stimuli was ensured by selecting utterances with no syntactically ill-formed or incomplete sentences, any background noise, cross-talk, long hesitations, revisions or non-words [5]. The aforementioned transcriptions were used only in the selection process of the stimuli for the experiment.

### 2.3. Experimental setup

The experiment was setup to perform a transcription task in the Qualtrics environment [77]. One hundred language students from the University of Antwerp participated. The participants were native speakers of Belgian Dutch, without any particular experience with the speech of hearing-impaired children.

The participants and stimuli were divided into five groups, where each group of 20 students transcribed 64 stimuli on their series. The stimuli were presented to the listeners in a random order. As a result, the setup produced 20 transcriptions per utterance, adding to a total of 6400 transcriptions. The steps that comprised the task are detailed in the supplementary section A.2.1.

The data resulting from the transcription task was then processed and converted into one entropy measure per utterance (H), which served as our outcome variable.

The entropy measure is bounded in the unit interval [0,1], and it was used as a quantification of (dis)agreement between listeners' transcriptions: utterances yielding a high degree of agreement between transcribers were considered highly intelligible, and therefore, registered a lower entropy  $(H \to 0)$ . In

contrast, utterances yielding a low degree of agreement were considered as exhibiting low intelligibility, and therefore, registered a higher entropy  $(H \to 1)$  [5, 27]. The procedure followed to calculate the entropies is detailed in the supplementary section A.2.2.

### 2.4. Causal framework

The analysis was informed by a preliminary work aimed at describing the causal and non-causal factors influencing speech intelligibility. More specifically, the current research uses a Directed Acyclic Graph (DAG) [59, 17] to describe all the relevant variables though to influence intelligibility. A DAG is a type of *structural causal model* that can be represented, among other ways, by a *causal diagram*.

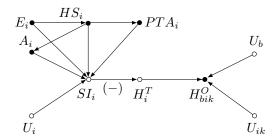


Figure 1: DAG: causal diagram describing the relationships among the analyzed variables. Open circles describe latent/unobserved variables, full circles describe observed variables.

Figure 1 shows the causal diagram for our research hypothesis. In the figure,  $H_{bik}^O$  denote the observed entropy replicates nested within children and experimental blocks, where  $k=1,\ldots,10$  utterances,  $i=1,\ldots,32$  children, and  $b=1,\ldots,5$  blocks. Moreover,  $H_i^T$  and  $SI_i$  denotes the child's true entropy and speech intelligibility scores, respectively. In addition,  $HS_i$  denotes the children's hearing status group,  $A_i$  their hearing age,  $PTA_i$  their unaided post-implant pure tone average, and  $E_i$  the etiology of the disease that led to the hearing impairment.

Three main features can be emphasized from the figure. First, the children's speech intelligibility and true entropy scores are thought to be latent/unobservable variables [26] (drawn with open circles, see supplementary section A.3 about the appropriate interpretations of the scores). The figure also shows the scores are thought to be inferable from the observed entropy replicates. More specifically, we are asserting the observed entropy replicates  $H_{bik}^O$  represent multiple realizations of a child's true entropy  $H_i^T$ . Finally, as expected from our the theory, we assume the intelligibility score  $SI_i$  is inversely/negatively related to the true entropy  $H_i^T$ , i.e. the lower the intelligibility the higher the entropy, and vice versa.

Second, the figure reflects the expected multilevel structure of variability present in our data. This is particularly important as, by failing to account for the appropriate dependencies in the data, we could be 'manufacturing' false confidence in the parameter's estimates, leading us to incorrect inferences [53].

Based on the experimental setup described in section 2.3, we anticipated the ten utterances, originated from each of the thirty two children, were also observed within a group of transcribers (series) assigned to the observation, i.e. our data has a hierarchy with children, replicates and block levels ( $U_i$ ,  $U_{ik}$  and  $U_b$ , respectively).

Considering the latter, we expect that if the experiment was 'set up right', the block random effects would explain a small amount of variability in the data, and its inclusion/exclusion in the model would not change the parameter estimates. Moreover, we expect a larger variability between children's *speech* intelligibility, at least larger than the block random effects. Several evidence suggest this is particularly true among HI/CI children [80, 60, 54, 11, 78, 58, 36]. Finally, we did not had any comparable expectation for the variability in the replicates, as this feature has not been investigated before.

Third, the figure shows the assumed relationship among the relevant variables [57, 6, 40, 28], and how these influence the children's intelligibility of speech. Furthermore, it also reveals we assume the variables are independent, beyond the described relationships. Here follows a description of our causal hypothesis for the relevant variables.

For *hearing status*  $(HS_i)$ , it is clear that its inclusion directly corresponds with the main purpose of the current research endeavor. i.e. compare the *speech intelligibility* among NH and HI/CI children. Yet, we do not have a clear expectation about the levels among the groups. In terms of intelligibility, previous literature suggest that some HI/CI children manage to 'catch up' with their NH counterparts

[74, 42, 7, 37, 9, 21, 75], implying the two group attain similar levels. However, other studies also indicate HI/CI children never reach their NH analogues [56, 11, 14, 38, 36, 24, 41], therefore implying different levels of *intelligibility* among the groups.

For *Hearing age*  $(A_i)$ , we expect the variable to be one of the main responsible for the increase in children's *speech intelligibility*, no mater the children's hearing status [5]. Several studies provide evidence that *intelligibility* increases with age [15, 16, 32, 33, 2, 8, 45], and the intuition of its effects can be easily asserted from Flexer [31]: "the more delayed the age of acquisition of a skill, the farther behind children are in the amount of cumulative practice they have had to perfect that skill. The same concept holds true for cumulative auditory practice".

In that sense, *Hearing age* is a composite variable constructed by combining the *chronological age* for the NH group, and the *device length of use* for the HI/CI group [27] (see table 3 in supplementary section A.1). The variable tries to approximate the amount of time a child has been actively hearing and developing his(her) language. However, no short of evidence has been presented in favor of using others surrogate measures, like *chronological age* [34, 42, 41] or *age at implantation* [57, 6, 9, 21]. We argue that the feasibility of using any other proxy measure, largely depends on the assumed reliability of the surrogate, to approximate the variable of interest. In that sense, although we recognize *hearing age* is not a 'perfect' proxy [27], we argue it is the most appropriate to test our hypothesis, based on the relevant literature and its assumed reliability to capture children's language development (although the latter has not been tested). Furthermore, we believe the variable serve two additional purposes: (i) control for sampling bias (expanded in supplementary section A.4), and (ii) de-confound the parameter estimates of *hearing status* [17].

Lastly it is important to highlight that, for modeling purposes, using more than one of the aforementioned proxies in tandem is not recommended. It is apparent from the previous description, the three surrogate measures share high similarities in their data construction. This in turn, could cause problems in the modeling procedure, as including variables that provide 'similar information' might lead to a statistical problem known as multicollinearity, in which our estimates get biased and less precise [29], leading us to incorrect inferences and conclusions.

For pure tone average  $(PTA_i)$ , we expect it to have a small or null effect on speech intelligibility, as the empirical evidence seem to suggest [5]. Pure tone average is the child's subjective hearing sensitivity, aided or unaided, by their hearing apparatus.

However, beyond the empirical evidence, the variable was included for two additional reasons. First, given that previous modeling efforts did not capture the full data hierarchy, it is possible that the effects of PTA on *speech intelligibility* has been largely overlooked. Although evidence seem to suggest the variable has no effect, it is also sensible to think that HI/CI children with severe hearing loss, as accounted by the variable, might develop their language at a slower rate. This is especially true, if we consider the signal provided by the cochlear implant is still degraded compared to normal hearing scenarios [22]. Lastly, the second reason for its inclusion lies in the possibility that the variable might be useful to de-confound the parameter estimates of *hearing status* [17], a purpose shared with the *hearing age* variable.

In the case of the **Etiology** of the disease that led to the hearing impairment  $(E_i)$ , we expect it to have a differential effect on *speech intelligibility*, within the HI/CI group. However, since the severity of the etiology cannot be easily ascertain nor ordered, we cannot foresee the direction of such effects, i.e. genetic factors not necessarily lead to worse levels of language development and intelligibility, than factors related to infections.

The previous assumption does not have a correspondence with the empirical evidence, were the variable was deemed unimportant [5]. However, we argue that it is possible its effects have also been largely overlooked, due to the lack of statistical control on the data variability hierarchy, similar to the PTA case. Moreover, as with its predecessors, the variable might also be useful to de-confound the parameter estimates of *hearing status* [17], assuming our DAG is appropriate.

Finally, it is important to highlight the reason for the absence of other variables, deemed relevant by the literature, in our causal hypothesis.

For the *type of cochlear implantation*, i.e. bilateral or contralateral, the variable was not included because we did not expect it to be related to other variables in the DAG, i.e. the decision on receiving one or the other is solely based on the intelligibility outcome, no matter how the latter is measured. This in turn means that its inclusion/exclusion would not confound our estimates. Additionally, given that most of the children underwent through sequential bilateral implantation (eleven in total), we anticipated the effect of variable already permeates the HI/CI sample.

For the case of *additional disabilities*, e.g. mental retardation or speech motor problems, given that the children did not reported any additional comorbidities, the variable was deemed unnecessary.

In the case of *environmental factors*, such as communication modality, the variable was also deemed unnecessary, given that HI/CI children were raised orally using monolingual Dutch with a limited support of signs, a scenario similar to the NH group (see section 2.1).

Last but not least, **gender** was not included in our hypothesis, as no theoretical nor empirical evidence have been found on its effects [5].

As expected, it is possible that other unobserved confounding variables are not accounted by our assumptions, and therefore, our causal diagram. This is true for any type of social, behavioral and educational research. However, we argue that the additional transparency of our approach, and its ability to derive statistical procedures from causal assumptions, is its main strength [53, 79, 62].

### 2.5. Statistical analysis

Using the DAG, described in the previous section, we describe the algebraic formalism for our multiple Bayesian probabilistic models [46]. Each model targeted a different manner in which our research hypothesis could be investigated.

In general terms, every model was composed of two parts: a latent measurement model [26] and a structural equation model [44]. For the former, we represented the child's *speech intelligibility* as a latent variable, inversely related to the child's latent *true* entropy. Moreover, we modeled the latter as a variable that can be inferred from the observed entropy replicates in the following way:

$$H_{bik}^{O} \sim \text{BetaProp}\left(\bar{H}_{bi}, M_{i}\right)$$
 (1)

$$\bar{H}_{bi} = \text{logit}^{-1}(a_b - SI_i) \tag{2}$$

$$H_i^T = \text{logit}^{-1}(-SI_i) \tag{3}$$

where BetaProp( $\mu$ ,  $\theta$ ) defines the beta-proportion distribution with parameters  $\mu$  and  $\theta$  [30, 48]; with  $\mu \in [0,1]$  and  $\theta > 0$ . Furthermore,  $\bar{H}_{bi}$  represented the average entropy measure nested within blocks and children (b = 1, ..., 5 and i = 1, ..., 32, respectively), while  $M_i$  denotes the 'sample size' of the distribution, possibly nested within children. Furthermore,  $H_{bik}^O$ ,  $H_i^T$  and  $SI_i$  denotes the children's entropy replicates, true entropy and speech intelligibility score, respectively. Finally,  $a_b$  represents the block random effects, and  $\log i T^{-1}(x) = \exp(x)/(1 + \exp(x))$  the inverse-logit transformation.

From the previous algebraic structure we can notice. First, we modeled the average entropy of the replicates with  $\mu = \bar{H}_{bi}$ , which is a non-linear transformation of the block random effects and the children's speech intelligibility. Second, the children's true entropy  $H_i^T$  is inversely and non-linearly related to the speech intelligibility  $SI_i$ . Third and last, we captured the variability of the entropy replicates using  $\theta = M_i$ . See supplementary section A.5.1 for a detailed overview of the implications of using this approach.

For the second component we used a structural model [44]. In this portion, different iterations of our research hypothesis were proposed. Hereby we present the general representation, from which the others can be derived:

$$SI_i = a_i + \alpha + \alpha_{E[i],HS[i]} + \beta_{A,HS[i]}(A_i - \bar{A}) + \beta_{P,HS[i]}sPTA_i \tag{4}$$

where  $E_i$  and  $HS_i$  are defined as in the previous section,  $A_i$  is the hearing age in years, while  $sPTA_i$  is the standardized version of the unaided post-implant pure tone average  $PTA_i$ . Moreover,  $a_i$  denoted the children's random intercepts, and  $\alpha$  the fixed intercept. On the other hand,  $\alpha_{E[i],HS[i]}$  denoted the intelligibility levels per etiology and hearing status group, while  $\beta_{A,HS[i]}$  denoted the evolution of intelligibility per unit of hearing age, for each hearing status group. Finally,  $\beta_{P,HS[i]}$  described the evolution of intelligibility per unit of the standardized pure tone average, for each hearing status group.

In the previous algebraic structure it is important to highlight, all parameters are estimated in the logit scale and centered at  $sPTA_i=0$  and  $\bar{A}=5$ , the latter denoting the minimum hearing age in the sample. This is done to facilitate the interpretation of the parameters.

Thirteen statistical models were derived from the previous general description. Each model expressed one specific way in which our research hypothesis could be investigated. Table 1 provides an overview of the parameterization for the full set of proposed models. The models were characterized by two aspects: (i) the use of interactions and the selection of interacting variables, and (ii) the 'sample size' set to capture

the replicates variability. For the former, the options were: intercept only (model 1), and multivariate regression with no interactions (models 2 to 4), with age and hearing status interaction only (models 5, 8, and 11), with etiology and hearing status interaction only (models 6, 9, and 12), and a full interaction model comprising the previous two (models 7, 10 and 13). In a similar fashion, for the latter the options were: one fixed 'sample size' (models 1, 2, 5, 6, and 7), one estimated 'sample size' (models 3, 8, 9, and 10), and finally, one 'sample size' per child (models 4, 11, 12, and 13), which we dubbed *robust* models (see supplementary section A.5.2, where we expand about the need for *robust* models).

Notice all proposals used block and children's random effects ( $a_b$  and  $a_i$ , respectively), as well as the fixed effect intercept ( $\alpha$ ). Moreover, the models with one fixed 'sample size' used a value of ten, corresponding to number of utterances per child (see supplementary section A.5.1 on its implications). Finally, all models contemplated the interaction of the standardized pure tone average and the hearing status. The latter was imposed, because the collection of data did not contemplated the measurement of the pure tone average for the NH group. Therefore, the only interpretable parameter is the one estimated for the HI/CI children.

It is important to highlight that for all model implementations, the visual inspection of trace, trace-rank and autocorrelation plots was performed. Additionally, we also evaluated the Gelman-Rubin diagnostic and effective number of samples [39]. In all cases, the plots and statistics indicated the parameters achieved convergence, good mixing and lack of serial autocorrelation, all necessary requirements to be able to interpret the model estimates [53].

Additional details concerning the Bayesian implementation of the models, such as the representation of variability in a beta-proportion distribution, the parameters' priors and hyper-priors, the estimation procedure, the data pre-processing phase, and simulation studies are expanded in the supplementary section A.5.

						Parameters	3	
Model	Name	$M_i$	$a_b$	$a_i$	$\alpha$	$\alpha_{E[i],HS[i]}$	$\beta_{A,HS[i]}$	$\beta_{P,HS[i]}$
1	Intercept only (fixed 'size')	10	$a_b$	$a_i$	$\alpha$	_	-	-
2	No interaction (fixed 'size')	10	$a_b$	$a_i$	$\alpha$	$\alpha_{HS[i]}$	$\beta_A$	$\beta_{P,HS[i]}$
3	No interaction (one 'size')	M	$a_b$	$a_i$	$\alpha$	$\alpha_{HS[i]}$	$\beta_A$	$\beta_{P,HS[i]}$
4	No interaction (robust)	$M_i$	$a_b$	$a_i$	$\alpha$	$\alpha_{HS[i]}$	$\beta_A$	$\beta_{P,HS[i]}$
5	Age interaction (fixed 'size')	10	$a_b$	$a_i$	$\alpha$	$\alpha_{HS[i]}$	$\beta_{A,HS[i]}$	$\beta_{P,HS[i]}$
6	Etiology interaction (fixed 'size')	10	$a_b$	$a_i$	$\alpha$	$\alpha_{E[i],HS[i]}$	$\beta_A$	$\beta_{P,HS[i]}$
7	Full interaction (fixed 'size')	10	$a_b$	$a_i$	$\alpha$	$\alpha_{E[i],HS[i]}$	$\beta_{A,HS[i]}$	$\beta_{P,HS[i]}$
8	Age interaction (one 'size')	M	$a_b$	$a_i$	$\alpha$	$\alpha_{HS[i]}$	$\beta_{A,HS[i]}$	$\beta_{P,HS[i]}$
9	Etiology interaction (one 'size')	M	$a_b$	$a_i$	$\alpha$	$\alpha_{E[i],HS[i]}$	$\beta_A$	$\beta_{P,HS[i]}$
10	Full interaction (one 'size')	M	$a_b$	$a_i$	$\alpha$	$\alpha_{E[i],HS[i]}$	$\beta_{A,HS[i]}$	$\beta_{P,HS[i]}$
11	Age interaction (robust)	$M_i$	$a_b$	$a_i$	$\alpha$	$\alpha_{HS[i]}$	$\beta_{A,HS[i]}$	$\beta_{P,HS[i]}$
12	Etiology interaction (robust)	$M_i$	$a_b$	$a_i$	$\alpha$	$\alpha_{E[i],HS[i]}$	$\beta_A$	$\beta_{P,HS[i]}$
13	Full interaction (robust)	$M_i$	$a_b$	$a_i$	$\alpha$	$\alpha_{E[i],HS[i]}$	$\beta_{A,HS[i]}$	$\beta_{P,HS[i]}$

Table 1: Proposed statistical models. Parameterizations.

### 3. Results

### 3.1. About the variability of the data

As expected, our data registered three levels of variability: between blocks and children variability, and finally, the entropy replicates variability.

Evidence from the posterior estimates reveal the block random effects explained a small amount of variability in the data ( $\sigma_b = 0.26$ , top panel of figure 2), and its inclusion/exclusion in the model did not change the parameter estimates. The previous implied the experiment was correctly 'set up', as the series in which the utterances were transcribed did not explain a significant amount of variation, nor its exclusion biased the parameter estimates.

On the contrary, we observe a significantly larger variability between children. More precisely, the speech intelligibility variability between children was more than three times the block effects variability

( $\sigma_i = 0.74$ , middle panel of figure 2). The result corroborates previous evidence on the matter [80, 60, 54, 11, 78, 58, 36, 5].

Lastly, for the entropy replicates variability, the posterior estimates reveal a reasonable finding: the amount of variability at the replicates level is even larger than the one observed at the children level (M = 6, bottom panel of figure 2). The latter implies there is significant error in measuring speech intelligibility using the entropy replicates, i.e. there is considerable measurement error [10].

The last two results have important consequences for our future inferences. What the results imply is that given the large amount of variability between children and the considerable presence of measurement error, the statistical models might have a harder time producing unequivocal inferences, in respect to the intelligibility levels of the *hearing status* groups, or other parameters of interest. This is particularly important, as simulation studies revealed this behavior was expected even with more reasonable levels of variability ( $\sigma_i = 0.5$  and M = 10, see supplementary section A.5.5).

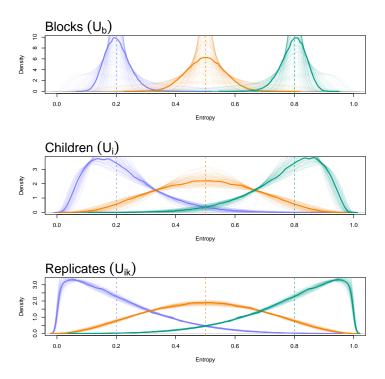


Figure 2: Model 10, posterior predictive: variability present in the data. Distributions are plotted on the entropy replicates scale, considering three different averages:  $\mu = 0.2$ ,  $\mu = 0.5$ , and  $\mu = 0.8$  (discontinuous lines). Thick solid lines represent the marginal distribution, thin solid lines depict 100 random posterior samples.

### 3.2. About our hypothesis

The current research used the Information-Theoretic Approach [1, 12] for model selection and inference. The application of the approach required: (i) the expression of the research hypothesis into statistical models, (ii) the selection of the most plausible models, and (iii) to produce inferences based on one or multiple selected models. The first requirement of the approach is covered in sections 2.4 and 2.5, and expanded in supplementary section A.5. Here we use the results of the second requirement, detailed in the supplementary section A.5.6, to produce the final inferences.

As detailed in the supplementary section, the final conclusions of our research will be drawn from the comparisons of two models: (i) a no interaction model, with one estimated 'sample size' (model 3), and (ii) a full interaction model, with one estimated 'sample size' (model 10). The former is selected because it is the model with highest probabilistic support. The latter is considered because it encompasses the remaining highest supported models. Furthermore, no *robust* models are inspected, as we prefer a more parsimonious depiction of our hypothesis. Table 2 summarizes the parameters posterior estimates and contrasts of interest.

			CI		HP	DI		
Parameter	Mean	SD	-2.5%	97.5%	-2.5%	97.5%	n eff.	Rhat
Model 3: No interact	tion (on	e 'size')						
parameters:								
a	0.179	0.189	-0.197	0.554	-0.198	0.552	3'677.705	1.001
bP[2]	-0.117	0.166	-0.439	0.207	-0.440	0.202	1'738.855	1.000
bA	0.432	0.141	0.154	0.715	0.170	0.723	1'815.243	1.001
aHS[1]	0.284	0.235	-0.178	0.761	-0.203	0.728	2'719.833	1.000
aHS[2]	0.116	0.217	-0.303	0.537	-0.304	0.537	2'646.671	1.000
constrast:								
aHS[2]-aHS[1]	-0.168	0.246	-0.661	0.371	-0.650	0.324	n.a.	n.a.
Model 10: Full intera	action (e	one 'size'	)					
parameters:								
a	0.217	0.179	-0.142	0.562	-0.118	0.580	3'902.629	0.999
bP[2]	-0.122	0.173	-0.457	0.220	-0.460	0.216	1'659.639	1.002
bAHS[1]	0.435	0.157	0.127	0.745	0.123	0.741	1'477.460	1.000
bAHS[2]	0.237	0.177	-0.119	0.596	-0.089	0.615	1'844.785	1.001
aEHS[1,1]	0.183	0.278	-0.358	0.726	-0.349	0.729	2'524.451	1.000
aEHS[2,2]	0.212	0.241	-0.259	0.684	-0.259	0.684	2'418.275	0.999
aEHS[3,2]	0.077	0.245	-0.402	0.547	-0.383	0.561	3'015.559	0.999
aEHS[4,2]	0.007	0.269	-0.522	0.530	-0.547	0.499	3'268.043	1.000
contrast:								
bAHS[2]-bAHS[1]	-0.197	0.208	-0.600	0.213	-0.590	0.223	n.a.	n.a.
aEHS[2,2]-aEHS[1,1]	0.029	0.352	-0.673	0.723	-0.714	0.682	n.a.	n.a.
aEHS[3,2]-aEHS[1,1]	-0.106	0.365	-0.823	0.607	-0.822	0.609	n.a.	n.a.
aEHS[4,2]-aEHS[1,1]	-0.176	0.380	-0.906	0.568	-0.928	0.535	n.a.	n.a.
aEHS[3,2]-aEHS[2,2]	-0.135	0.299	-0.719	0.453	-0.730	0.439	n.a.	n.a.
aEHS[4,2]-aEHS[2,2]	-0.205	0.344	-0.888	0.453	-0.902	0.430	n.a.	n.a.
aEHS[4,2]-aEHS[3,2]	-0.070	0.344	-0.744	0.612	-0.735	0.617	n.a.	n.a.

CI = compatibility interval

HDPI = highest posterior density interval

 $n \ eff. = effective number samples$ 

Rhat = Gelman-Rubin diagnostic

n.a. = not available / not applicable

[1] = NH children, [2] = HI/CI children

 $[1,\!\mathrm{i}]=\mathrm{NH}$ children,  $[2,\!\mathrm{i}]=\mathrm{genetic},\,[3,\!\mathrm{i}]=\mathrm{CMV}$ infection,  $[4,\!\mathrm{i}]=\mathrm{unknown}$ etiology

Table 2: Selected statistical models: results.

Before providing any parameter interpretation, it is important to highlight an statistical issue that will permeate all of our inferences. As it is detailed in section 3.1, with our current data size and given the large amount of variability registered at the children and replicates levels, the models are not able to produce unequivocal null hypothesis rejections for most of the parameters estimates, at a confidence level of 95%, i.e. the CI and HPDI will almost always include the zero value. This is particularly important, as rejecting the null hypothesis of certain parameters and contrast of interest provides unambiguous evidence for the current research hypothesis.

However, we consider that even when particular null hypothesis cannot be rejected, the models are still able show some preliminary evidence of effects and their direction. Given that parameter estimation under the Bayesian framework does not return parameters' point estimates, but rather the posterior distribution of possible values, we can still evaluate the amount of evidence towards a specific effect and its direction. In a complementary way, supplementary section A.5.5 reveal that our models are also able to affirm the estimate values with at least 60% power, depending on the estimates magnitudes, i.e. the models can correctly estimate values different from zero, when such alternative hypothesis is true.

In that sense, we will continue interpreting the parameters, providing evidence on the directionality of

the effects. Nevertheless, the reader should be cautious into understanding the CI and HPDI indicate that our data size might still not be enough, to ultimately define the direction of some effects with a certain level of confidence (usually 95%), and further observations at the children level might still be needed.

Considering the previous, for *hearing status*, model three reveals that HI/CI children have a modest lower level of *speech intelligibility*, compared to their NH counterparts (aHS[2]-aHS[1]). Notice the CI and HPDI include the value of zero, and therefore, null hypothesis rejections at a 95% confidence level cannot be made. However, the posterior distribution of the contrast reveal that 76.8% of the estimates are unequivocally below zero (aHS[2]-aHS[1] < 0). In this sense, the result seem to mildly support previous evidence on the matter [56, 11, 14, 38, 36, 24, 41].

Nevertheless, model ten paints a more nuanced story considering the *etiology* of the disease. The contrasts of the model reveal that HI/CI children with genetic etiology manage to reach similar levels of *intelligibility* as NH children (aehs[2,2]-aehs[1,1]). However, the same cannot be said when the hearing impairment is caused either by CMV infection (aehs[3,2]-aehs[1,1]) or other unknown causes (aehs[4,2]-aehs[1,1]). The posterior distribution of the aforementioned contrasts show the estimates are distinctly below zero with a probability of 62.4% and 68%, respectively.

About the former result, we theorize a intuitive explanation. Since hearing loss is a brain issue, rather than ear issue [31], as children with genetic causes grow developing their language using the hearing apparatus, they grow constructing effective auditory neural pathways that benefit from the new hearing input from the start, even when that input is slightly degraded [22]. However, the same cannot be said for other etiology status. What is hinted is that, a child with other etiology might need to 're-wire' his(her) auditory neural connections in order to fully take advantage of the new hearing signal. This is particularly important, if we consider these children are trying to achieve this 're-wiring' process, during an important maturing stage of the brain cortex (first twelve months) [31].

In relation to *hearing age*, model three reveals what we initially expected: the factor is one of the main determinants for the increase in children's *speech intelligibility*, showing statistically significant moderate effects (bA) [18, 64]. However, model ten offers preliminary evidence contrary to what was previously found [5], indicating there is a difference in the evolution of *intelligibility* between HI/CI and NH children (bAHS[2]-bAHS[1]). The posterior distribution of the contrast show 83.1% of the estimates are unequivocally below zero. We intuit the latter result have two possible complementary explanations, either: (i) the children develop their language differently at different stages of their (*hearing*) age [31], or (ii) given that the hearing signal provided by the apparatus is degraded [22], HI/CI children might take longer to achieve similar levels of *intelligibility* than their NH counterparts.

Finally, for *pure tone average*, we see both models support our initial hypothesis: HI/CI children with severe hearing loss, as accounted by the variable, develop their language at a slower rate than their NH counterparts (bP[2]). Notice again that 95% confidence null hypothesis rejections cannot be made. However, the posterior distribution of the parameter reveal the estimates are unequivocally below zero with approximately 76% probability (bP[2] < 0). Therefore, from perspective of effect sizes [18, 64], the estimates can be considered small in magnitude, but present nonetheless.

More interestingly still is that this results couple rather well with the second explanation for the effects of *hearing age*, i.e. the more degraded the signal a child receives, either because of the apparatus or the severity of their hearing-impairment, the slower the *speech intelligibility* evolves.

### 3.3. The speech intelligibility scale

As previously stated, one of the main benefits of the current methodology is that we can 'construct' an *intelligibility* score of the sampled children, which in turn, allow us to test different hypothesis and even make individual comparisons at the appropriate level. See supplementary section A.3 for the appropriate interpretation of the scores.

Figure 3 depicts the estimated *true* entropy and *speech intelligibility* scores per child. Three points can be highlighted from the figure. First, from the horizontal discontinuous lines, we can clearly assess that on average NH children have a modest higher level of intelligibility (lower entropy) than the HI/CI counterparts. However, given the children's variability, we cannot reject the hypothesis that HI/CI have similar levels than the NH children, as one can notice from the overlapping shaded areas of both groups.

Second, the figure reveals there is some inherited uncertainty on the score estimates, resulting from using entropy replicates as a tool for measuring *speech intelligibility*. The latter can be observed from the vertical lines, describing the highest posterior density intervals for the *intelligibility* of each child. We

argue this last trait is one of the main strengths of the method, as it allow us to not only make individual comparisons, but also consider the inherited (un)certainty of the comparison.

Third and final, the non-linear relationship between *speech intelligibility* and the *true* entropy scale is clearly noticed in the HPD intervals, where lowest/highest entropy values are paired with narrower intervals. Clear examples of this can be observed at the top panel of figure 3, where children 20 and 25 show narrower intervals at the lowest part of the scale, while child 6 shows the analogous at the highest end of the same. The previous behavior is expected under non-linear statistical models. Nevertheless, this particular trait has an intuitive interpretation under our specific application, i.e. we can be more certain of the children's *true* entropy values at the extreme of the hypothetical construct (either zero or one), rather than in the middle part of the scale.

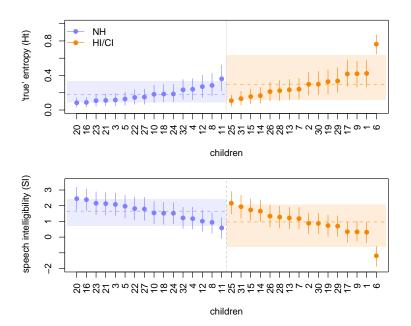


Figure 3: Model 10, posterior predictive: true entropy and speech intelligibility scales. Colored circles represent mean values per hearing status group. Thin vertical continuous lines depict 95% highest posterior density intervals (HDPI). Thin horizontal discontinuous lines represent the marginal average for the hearing status group. Shaded area represent the marginal averages 95% confidence interval.

#### 3.4. Posterior predictive

The posterior predictive results give us with a tool to assess how good our models were to reconstruct the observed data. Figure 4 shows our full interaction model managed to 'recreate' our data, while also provided the (un)certainty around the entropy replicates. The latter was shown in two ways: (i) through the point estimates and HPD intervals for the *true* entropy scale (red points and horizontal lines), and (ii) though the expected estimated marginal and sampled distributions for the entropy replicates (thick and thin solid distribution lines, respectively).

### 3.5. Influential observations

Finally, implementing the statistical models under the Bayesian framework provide us with one last advantage: we were able to identify influential observations that might sway our estimates, under our model framework [53]. We argue this method is preferable, as the identification of influential observations through preliminary or univariate procedures might lead to erroneous exclusion of information, ultimately damaging our research inferences. See supplementary section A.5.2 for more details.

Figure 5 provides an overview of the identified high-leverage observations (pair child, utterance). Model ten reveals some observations for children 8, 10, and 15 can be deemed prominent. The first two were NH children, while the last was an HI/CI analogue.

After a careful inspection, the only similitude between these observations was that all of them registered the lowest replicate values observed in the sample (0.007 for child 8, and zero for the remaining two). Therefore, it makes sense our model found these points 'surprising', as they are mostly out of the expected range for the outcome. The latter is particularly true for child 15, as it is not expected that an HI/CI child have traits of perfect *intelligibility*, as the replicate seem to indicate.

However, notice additionally that even with their presence, no further evidence was found in favor of *robust* models over other more parsimonious iterations of our research hypothesis (see supplementary section A.5.6). As a result, none of these observation were excluded from the analysis, but they were identified and can be further investigated.

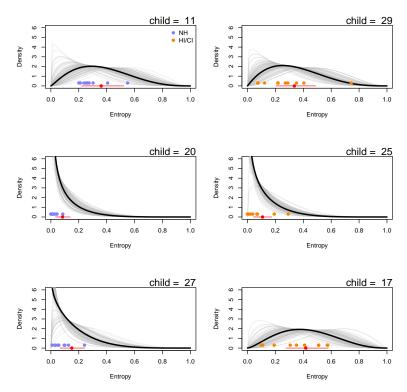


Figure 4: Model 10, posterior predictive: entropy replicates, true entropy, and distributions. Colored points represent the entropy replicates per hearing status group. Red points with lines represent the mean true entropy with 95% highest posterior density interval (HPDI). Thick solid line represents the marginal distribution, thin solid lines depicts 100 random posterior samples for the distributions.

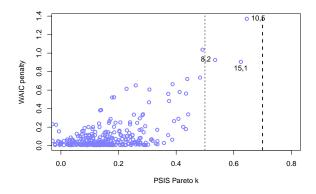


Figure 5: Model 10, influential observations. Pairs child, utterance are reported for specific observations. Thin and thick discontinuous lines indicate the minimum and extreme recommended threshold of identification (0.5 and 0.7, respectively).

### 4. Discussion

As stated in previous paragraphs, the main focus of the present research was to investigate the speech intelligibility levels of normal hearing (NH) versus hearing-impaired children with cochlear implants (HI/CI). For that purpose, we set up an experiment where ten utterances, from thirty two children, were transcribed and transformed into entropy measures, which served as our outcome variable.

Rather than use the common multilevel approach, the current research proposed a statistical method novel to the field of linguistics. First, we modeled the *speech intelligibility* as a latent variable that can be inferred from the entropy replicates [26, 44]. The previous not only allow us to 'construct' an *intelligibility* score, but also to control for all the variability assumed present in our data. We argue the former was important as it allowed us to make comparisons at appropriate levels, while the latter was important to not 'manufacture' false confidence in our parameter estimates, ultimately leading us to incorrect inferences [53]. Second, we used Directed Acyclic Graphs (DAG) [59, 17] to describe our causal and non-causal hypothesis about the *intelligibility* of speech, and determine which variables were relevant for its development. Finally, we implemented the method under the Bayesian framework, where we provided the steps and code for its implementation.

The statistical results highlighted two specific points. First, and most important, considering the large variability registered at the children and replicates levels, we were not able to produce unequivocal null hypothesis rejections, at a 95% confidence level. As a result, in some way, we were impeded to clearly delimit the magnitude and direction of some effects. Furthermore, simulation studies revealed the need for larger sample sizes in order to produce such decisive results.

Nevertheless, as a second point, we have shown that by using the posterior distribution of the estimates, we were able to provide 'preliminary' evidence on some of our causal hypothesis. On the one hand, we found there was mild evidence towards a difference in *intelligibility* between *hearing status* groups, in favor of NH children. However, the evidence also revealed the difference was mostly observed between NH and HI/CI children with etiologies other than genetic. In that sense, we further hypothesized that since hearing loss is a brain issue, rather than ear issue [31], these children might be 're-wiring' their auditory neural pathways during an important maturing stage of the brain cortex (first twelve months) [31], and that is what causes the delay in language development. It is fair to say then, the researchers believe it would be interesting to further inspect this hypothesis, with the support of Magnetic Resonance Imaging (MRI).

On the other hand, our analysis clearly identified hearing age as one of the main determinant in the evolution of speech intelligibility. However, the story produced by our models was more nuanced, as they also indicated there might be a different evolution in intelligibility between NH and HI/CI children. The last result gave evidence contrary to what was previously found [5]. Furthermore, as in the case of hearing status, we hypothesized this outcome have two possible complementary explanations, either: (i) the children develop their language differently, at different stages of their (hearing) age [31], or (ii) given that the hearing signal provided by the apparatus is degraded [22], HI/CI children might take longer to achieve similar levels of intelligibility than their NH counterparts. Therefore, the researchers believe it would be interesting to assess the latter hypothesis, and for that purpose, further collection of data would be required, i.e we would need to identify the hearing signal degradation for the cochlear implants.

Furthermore, our analysis provided 'mild' evidence that HI/CI children with more severe hearing loss, as accounted by the *pure tone average*, develop their language at slower rate than their NH analogues. We further noticed, the previous result couples rather well with the second hypothesis proposed to explain the effects of *hearing age*, i.e. the more degraded the hearing signal, either because of the apparatus or the severity of the hearing-impairment, the slower the *intelligibility* evolves.

As perspectives for future research and further critiques, two finals points can be highlighted. First, the procedure for calculating the entropy replicates weighted equally any differences in the transcriptions. This implied the entropy values were equally increased by fairly small deviances, e.g. kikker 'frog' versus kikkers 'frogs', than with considerable ones, e.g. mismatches as in jongen 'boy' versus hond 'dog'. In that sense, the researchers also share the believe of Boonen et al. [5], that a further refinement of the entropy calculation can be made, in which the linguistic distance of the transcriptions can be considered.

Second and last, although we used a DAG to state our causal and non-causal hypothesis, it is clear, the benefits of the tool shine when it is also used to plan the data collection. As stated in the document, the tool not only helps to make our hypothesis more transparent, but also allow us to derive statistical procedures from such assumptions. Scenarios like the lack of power to test specific effects, and the need for larger samples could have been easily foresaw during this part of the experimental planning [53, 35].

# 5. Acknowledgments

A special thanks to Richard McElreath, for timely response and help. Further gratitude is expressed to Tine van Daal, Marijn Gijsen, Lies Appels, and Silvana Romero for giving feedback to preliminary versions of this document.

### 6. Author contributions

All authors contributed to the development of the causal hypothesis. Jose Rivera performed the statistical analysis, Sven de Maeyer supervised the production of the documents and statistical results, and Steven Gillis collected the data.

# 7. Financial support

The project was financed by the Flemish Government through the University Research Fund (BOF).

### 8. Conflicts of interest

The authors declare they have no conflict of interest.

# 9. Research transparency and reproducibility

The model simulation procedures and testing that support the findings of this study are openly available at https://github.com/jriveraespejo/PhD\_UA\_paper1.

Due to the privacy and confidentiality of subjects, the data set in which the model was implemented cannot be put online.

# A. Supplementary

### A.1. Children characteristics

Table 3 shows the detailed information of the sampled children. The referred table includes the variable used for the matching procedure, i.e. chronological age, while also additional variables thought to be relevant for our hypothesis. No other variables are included as no known additional comorbidities, beside their hearing impairment, are suspected. Additionally, notice the pure tone average (PTA) data was not collected for the NH children.

Child         age (y;m)         of use (y;m)         age (y;m)         unaided aided           HI/CI children           1         female         05;07         05;00         05;00         Genetic         120         19           2         male         06;04         05;09         05;09         CMV         106         23           3         male         06;07         05;10         05;10         Genetic         114         35           4         female         06;10         06;03         06;03         CMV         115         25           5         female         07;00         06;08         06;08         Genetic         93         32           7         female         07;00         06;08         06;08         Genetic         117         17           8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;01         05;05         05;05         Uknown         112         42           9         male         07;01         05;05         05;05         CMV         120         15           10         female         07;01 <th></th> <th>Gender</th> <th>Chronological</th> <th>Device length</th> <th>Hearing</th> <th>Etiology</th> <th>PTA (</th> <th>dB.)</th>		Gender	Chronological	Device length	Hearing	Etiology	PTA (	dB.)
1         female         05;07         05;00         05;00         Genetic         120         19           2         male         06;04         05;09         05;09         CMV         106         23           3         male         06;07         05;10         05;10         Genetic         114         35           4         female         06;10         06;00         06;00         Unknown         120         20           5         female         07;00         06;08         06;08         Genetic         93         32           6         male         07;00         05;08         06;08         Genetic         117         17           8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           10         female         07;01         05;	Child		age $(y;m)$	of use (y;m)	age $(y;m)$		unaided	aided
2         male         06;04         05;09         05;09         CMV         106         23           3         male         06;07         05;10         05;10         Genetic         114         35           4         female         06;07         06;00         06;00         Unknown         120         20           5         female         07;00         06;03         06;03         CMV         115         25           6         male         07;00         05;08         05;08         Genetic         93         32           7         female         07;00         06;08         06;08         Genetic         117         17           8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           10         female         07;01         05;05         05;05         CMV         120         35           11         male         07;01         05;07		HI/CI	children					
2         male         06;04         05;09         05;09         CMV         106         23           3         male         06;07         05;10         05;10         Genetic         114         35           4         female         06;07         06;00         06;00         Unknown         120         20           5         female         07;00         06;08         06;08         Genetic         93         32           6         male         07;00         06;08         06;08         Genetic         93         32           7         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         CMV         120         15           10         female         07;01         05;07         05;07         Genetic         120         35           11         male         07;02         06;05 <td>1</td> <td></td> <td></td> <td>05;00</td> <td>05;00</td> <td>Genetic</td> <td>120</td> <td>19</td>	1			05;00	05;00	Genetic	120	19
4         female         06;10         06;00         06;00         Unknown         120         20           5         female         07;00         06;03         06;03         CMV         115         25           6         male         07;00         05;08         05;08         Genetic         93         32           7         female         07;00         06;08         06;08         Genetic         117         17           8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         CMV         120         15           10         female         07;01         05;07         05;07         Genetic         120         35           11         male         07;01         05;07         05;07         Genetic         120         37           12         male         07;02         06;05         06;05         Genetic         120         37           13         male         07;08         06;1		male	06;04	05;09	05;09	CMV	106	23
5         female         07;00         06;03         06;03         CMV         115         25           6         male         07;00         05;08         05;08         Genetic         93         32           7         female         07;00         06;08         06;08         Genetic         117         17           8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         CMV         120         15           10         female         07;01         05;11         05;11         Genetic         120         35           11         male         07;01         05;07         05;07         Genetic         113         42           12         male         07;02         06;05         06;05         Genetic         120         37           13         male         07;08         06;10         06;10         CMV         114         27           14         male         07;09         06;02         06;02         CMV         120         35           15         male         08;07         07;10	3	male	06;07	05;10	05;10	Genetic	114	35
6         male         07;00         05;08         05;08         Genetic         93         32           7         female         07;00         06;08         06;08         Genetic         117         17           8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;01         05;05         05;05         CMV         120         15           10         female         07;01         05;07         05;07         Genetic         120         35           11         male         07;01         05;07         05;07         Genetic         120         35           12         male         07;02         06;05         06;05         Genetic         120         37           13         male         07;08         06;10         CMV         114         27           14         male         07;09         06;02         06;02         CMV         120         35           15         male         08;07         07;10         07;10         CMV         120         33           16         male         08;08         09;09         09;09	4	female	06;10	06;00	06;00	Unknown	120	20
7         female         07;00         06;08         06;08         Genetic         117         17           8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         CMV         120         15           10         female         07;01         05;07         05;07         Genetic         120         35           11         male         07;02         06;05         06;05         Genetic         120         37           13         male         07;08         06;10         06;10         CMV         114         27           14         male         07;09         06;02         06;02         CMV         120         35           15         male         08;07         07;10         07;10         CMV         120         33           16         male         08;08         09;09         09;09         Genetic         95         27           NH children           17         female         06;05         n.a.         n.a.         n.a.         n.a.           18         female	5	female	07;00	06;03	06;03	CMV	115	25
8         female         07;00         05;05         05;05         Unknown         112         42           9         male         07;00         05;05         05;05         CMV         120         15           10         female         07;01         05;11         05;11         Genetic         120         35           11         male         07;01         05;07         05;07         Genetic         120         37           12         male         07;02         06;05         06;05         Genetic         120         37           13         male         07;08         06;10         06;10         CMV         114         27           14         male         07;09         06;02         06;02         CMV         120         35           15         male         08;07         07;10         07;10         CMV         120         33           16         male         08;07         07;10         07;10         CMV         120         33           16         male         08;08         09;09         09;09         Genetic         95         27           NH children           17         fe	6	male	07;00	05;08	05;08	Genetic	93	32
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7	female		06;08	06;08	Genetic	117	17
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	8	female	07;00	05;05	05;05	Unknown	112	42
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	9	male	07;00	05;05	05;05	CMV	120	15
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	10	female	07;01	05;11	05;11	Genetic	120	35
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	male	07;01	05;07	05;07		113	42
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	12	male		06;05	06;05	Genetic	120	37
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	13	male	,	,	,	CMV	114	
16         male         08;08         09;09         09;09         Genetic         95         27           NH children           17         female         06;05         n.a.         06;05         n.a.         n.a. </td <td>14</td> <td>male</td> <td></td> <td>06;02</td> <td>06;02</td> <td>CMV</td> <td>120</td> <td>35</td>	14	male		06;02	06;02	CMV	120	35
16         male         08;08         09;09         09;09         Genetic         95         27           NH children           17         female         06;05         n.a.         06;05         n.a.         n.a. </td <td>15</td> <td>male</td> <td>08;07</td> <td>07;10</td> <td>07;10</td> <td>CMV</td> <td>120</td> <td>33</td>	15	male	08;07	07;10	07;10	CMV	120	33
17       female       06;05       n.a.       06;05       n.a.	16	male				Genetic	95	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		NH chi	ldren	·	·			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	17	female	06;05	n.a.	06;05	n.a.	n.a.	n.a.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	18	female	06;06	n.a.	06;06	n.a.	n.a.	n.a.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	19	female	06;07	n.a.	06;07	n.a.	n.a.	n.a.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	20	female	06;09	n.a.	06;09	n.a.	n.a.	n.a.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	21	female	06;09	n.a.	06;09	n.a.	n.a.	n.a.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	22	male	06;09	n.a.	06;09	n.a.	n.a.	n.a.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	23	male	06;09	n.a.	06;09	n.a.	n.a.	n.a.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	24	male	06;10	n.a.	06;10	n.a.	n.a.	n.a.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	25	female	07;01	n.a.	07;01	n.a.	n.a.	n.a.
28     female     07;08     n.a.     07;08     n.a.     n.a.     n.a.       29     male     07;08     n.a.     07;08     n.a.     n.a.     n.a.     n.a.       30     female     07;09     n.a.     07;09     n.a.     n.a.     n.a.     n.a.       31     female     08;00     n.a.     08;00     n.a.     n.a.     n.a.	26	male	07;01	n.a.	07;01	n.a.	n.a.	n.a.
29     male     07;08     n.a.     07;08     n.a.     n.a.     n.a.       30     female     07;09     n.a.     07;09     n.a.     n.a.     n.a.       31     female     08;00     n.a.     08;00     n.a.     n.a.     n.a.	27	male	07;04	n.a.	07;04	n.a.	n.a.	n.a.
30       female       07;09       n.a.       07;09       n.a.       n.a.       n.a.         31       female       08;00       n.a.       08;00       n.a.       n.a.       n.a.	28	female	07;08	n.a.	07;08	n.a.	n.a.	n.a.
31 female 08;00 n.a. 08;00 n.a. n.a. n.a.	29	male	07;08	n.a.	07;08	n.a.	n.a.	n.a.
, ,	30	female	07;09	n.a.	07;09	n.a.	n.a.	n.a.
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	31	female	08;00	n.a.	08;00	n.a.	n.a.	n.a.
	32	female	08;01	n.a.	08;01	n.a.	n.a.	n.a.

(y;m) = (years;months)

n.a. = not applicable / not available

Table 3: Characteristics of selected children.

### A.2. Experiment details

#### A.2.1. Transcription task

The setting for the transcription task comprised the following steps [4, 5]:

- 1. the listener took a seat in front of a computer screen, located at the campus' computer laboratory.
- 2. the listener opened Qualtrics [77] and select the transcription task.
- 3. the listener read two set of instructions presented on the computer screen about:
  - a) how to perform the task,
  - b) the aspects not considered for the task.
- 4. the listener hear the stimuli through high quality headphones, set at a comfortable volume.
- 5. the listener wrote the orthographic transcriptions of the utterances, in a free text field in the software environment.

#### A.2.2. Entropy calculation

The outcome from the transcription task was obtained following a two step procedure [5]. First, we aligned the participant's orthographic transcriptions, at the utterance level, in a column-like grid structure similar to the one presented in Table 4. This step was repeated for every one of the 6400 transcriptions. Lastly, we computed the entropy measure of the aligned transcriptions as in Shannon [65]:

$$H = H(\mathbf{p}) = \frac{-\sum_{i=1}^{n} p_i \cdot \log_2(p_i)}{\log_2(N)}$$

$$(5)$$

where H is bounded in the unit interval [0,1], n denotes the number of word occurrences within each utterance,  $p_i$  the probability of such word occurrence, and N the total number of aligned transcriptions per utterance.

Transcription	Utterance							
number	1	2	3	4	5			
1	de	jongen	ziet	een	kikker			
	the	boy	see	a	frog			
2	de	jongen	ziet	de	[X]			
	the	boy	sees	the	[X]			
3	de	jongen	zag	[B]	kokkin			
	the	boy	saw	[B]	$\operatorname{cook}$			
4	de	jongen	zag	geen	kikkers			
	the	boy	saw	no	frogs			
5	de	hond	zoekt	een	[X]			
	the	dog	searches	a	[X]			
Entropy	0	0.3109	0.6555	0.8277	1			

 $[B] = blank \; space, \, [X] = unidentifiable \; word$ 

Table 4: Alignment and entropy calculation. Extracted from Boonen et al. [5], and slightly modified with illustrative purposes.

Entropy was used as a quantification of (dis)agreement between listeners' transcriptions, i.e. utterances yielding a high degree of agreement between transcribers were considered highly intelligible, and therefore registered a lower entropy  $(H \to 0)$ . In contrast, utterances yielding a low degree of agreement were considered as exhibiting low intelligibility, and therefore registered a higher entropy  $(H \to 1)$  [5, 27].

To exemplify relevant scenarios for the procedure, we generate the entropy for utterances 2, 4 and 5 present in Table 4. To make the example easy to calculate, we assume our data consisted only of five transcriptions in total (N = 5).

For the second utterance, we observe that four transcriptions identify it with the word *jongen*, while the last with the word *hond*. Therefore, we registered two word occurrences (n = 2), with probabilities  $\mathbf{p} = (p_1, p_2) = (4/5, 1/5)$ , and entropy measure equal to:

$$H = \frac{-\sum_{i=1}^{2} p_i \cdot \log_2(p_i)}{\log_2(5)}$$
$$= \frac{-[0.8 \log_2(0.8) + 0.2 \log_2(0.2)]}{\log_2(5)}$$
$$\approx 0.3109$$

For the fourth utterance, we observe that two transcriptions identify it with the word *een*, one with *de*, one with *geen*, and one with a blank space [B]. Notice the blank space was not expected in such position, therefore, it was considered as a different word occurrence. As a result, the scenario had four word occurrences (n = 4), with probabilities  $\mathbf{p} = (p_1, p_2, p_3, p_4) = (2/5, 1/5, 1/5, 1/5)$ , and entropy measure equal to:

$$H = \frac{-\sum_{i=1}^{4} p_i \cdot \log_2(p_i)}{\log_2(5)}$$
$$= \frac{-\left[0.4 \log_2(0.4) + 3 \cdot 0.2 \log_2(0.2)\right]}{\log_2(5)}$$
$$\approx 0.8277$$

Finally, for the fifth utterance, we observe that all transcriptions identify it with different words. Notice that when a transcriber did not managed to identify (part of) the complete utterance, (s)he was instructed to write [X] to replace it. However, if more than one transcriber used [X] for an unidentifiable word, each was considered as being different from one another. The latter is done to avoid the artificial reduction of the entropy measure, as [X] values already indicate the lack of intelligibility of the word. Therefore, for the fifth utterance we registered five word occurrences (n = 5), with probabilities  $\mathbf{p} = (p_1, \dots, p_5) = (1/5, \dots, 1/5)$ , and entropy measure equal to:

$$H = \frac{-\sum_{i=1}^{5} p_i \cdot \log_2(p_i)}{\log_2(5)}$$
$$= \frac{-5 \cdot 0.2 \log_2(0.2)}{\log_2(5)}$$
$$= 1$$

### A.3. About speech intelligibility

As described in the introduction, intelligible speech can be defined as the extent to which the elements in an speaker's acoustic signal, e.g. phonemes or words, can be correctly recovered by a listener [47, 73, 70, 36]. More specifically, in the context of the transcription task, speech intelligibility can be inferred from the extent a set of transcribers can identify the word contained in an utterance [5].

Therefore in this paper, through the implementation of our proposed model, speech intelligibility is interpreted as a latent trait of individuals (hypothetical construct), which underlies the probability of observing a set of entropy replicates; that in turns, describes the ability of transcribers to identify the words in an utterance. Henceforth, statements such 'speech intelligibility is influenced by' can be read as 'the probability of observing a set of entropy replicates for each individual in the sample is influenced by'. Similar interpretation can be extended to the (latent) true entropy measures.

Despite this practical approach, we emphasize we did our best to ensure the construct validity of our study: (i) by ensuring the transcription task was well understood, and appropriately performed by the transcribers, and (ii) by using children's utterances coming from spontaneous speech, a task with the highest level of ecological validity [32, 25].

We then expect speech intelligibility, as measured by our model, to reflect the (general) *intelligibility* of speech possessed by individuals, but do not deal with general epistemological considerations on the connection between the two.

### A.4. Sampling bias

As it happens in most observational, and some experimental studies, ours can also be a potential victim of sampling bias. While stratifying on the selection variables can help to balance the samples, and even 'correct' the estimates [17, 20], as we do here by controlling for hearing age. Given the sample's selection and matching procedures, we cannot ensure the HI/CI nor the NH groups are representative of their respective populations.

Nevertheless, we argue that by controlling for other relevant confounders, the qualitative results presented in this study holds. However, we cannot discard the presence of unobservable variables that could bias our results, and in that sense, inferences beyond this particular set of children must be taken with care.

### A.5. Model details

#### A.5.1. Variability in the beta-proportion distribution

Figure 6 shows the implications of different 'sample sizes'  $(M_i)$  on the dispersion of the beta-proportion distribution [48]. The panels show different average entropies: the middle panel assumes  $\mu = 0.5$ , the left  $\mu = 0.2$ , and the right  $\mu = 0.8$  (as shown by the discontinuous lines).

In all three panels we notice two prevalent pattern: (i) the higher the 'sample size', the less dispersed is the distribution, and (ii) as expected from non-linear models, the behavior of the dispersion depends on the location of the distribution, i.e. their average value.

Concerning the first patterns, we expect that if the posterior estimates for  $M_i$  reach lower values, it would imply the entropy replicates  $H_{bik}^O$  had high dispersion. In contrast, higher  $M_i$  estimates would imply a lower dispersion in the replicates. In this particular case, a good comparison point is the number of utterances/replicates. If  $M_i < 10$ , it would imply that our effective 'sample size' (measuring points) is less than the actual number of replicates, and therefore, we would need more replicates to provide an accurate measure of the (latent) true entropy. In contrast,  $M_i > 10$  would imply the opposite.

As a final point, it is important to highlight that as the approach uses the 'sample size' parameter to model the replicates' heterogeneity, we are effectively estimating a measurement error model [10] on entropy values.

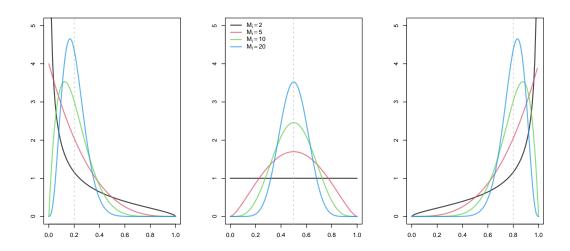


Figure 6: Variability in a beta-proportional distribution. Discontinuous lines describe the average value for the distribution ( $\mu$ ), solid lines describe the distribution assuming different  $\theta = M_i$ .

#### A.5.2. Data pre-processing

Besides the exclusion of corrupted observations, e.g. no available transcription, no other information was excluded before the modeling process. This decision departs from what has been done in previous research

[4, 69, 5]. The reason is that we believe the identification of influential observations, through preliminary or univariate procedures, might lead to erroneous exclusion of information, ultimately biasing our results. We believe the identification of *outliers* should not be done outside the context of a full modeling effort [53], as what can behave as an *outlier* based on a univariate analysis, might behave as expected under the appropriate model.

Considering the previous, instead of eliminating information based on preliminary analysis, we proposed a set of models that can be qualified as *robust* against influential observations. Considering the flexibility of the Bayesian framework, the proposal of such models was a trivial task (see Table 1).

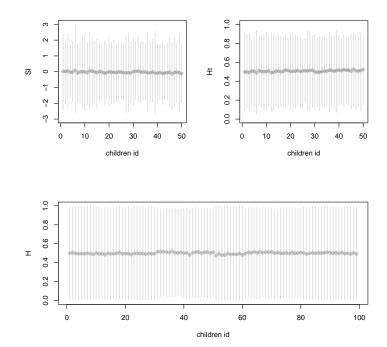


Figure 7: Prior distribution implications: speech intelligibility, *true* entropy and observed entropy scales. Circles represent mean values, lines depict the 95% compatibility intervals.

### A.5.3. Priors and hyper-priors

For all models, the selection of priors and hyper-priors was done through prior predictive simulation [53]. The selected priors were considered mildly informative and regularizing.

Figure 7 shows the implication of our assumptions on the three outcome scales of interest: the *speech* intelligibility, the true entropy, and the observed entropy replicates. Notice, no undesirable assumption has crept in any of the scales. Consequently, the estimates are free to visit a wide range of results, while also establishing a low probability of reaching impossible outcomes.

Hereby follows a description of the priors for the parameters already defined in section 2.5:

$$M_i \sim \text{Log-Normal}(\mu_M, \sigma_M)$$
 (6)

$$a_b \sim \text{Normal}(\mu_b, \sigma_b)$$
 (7)

$$a_i \sim \text{Normal}(\mu_i, \sigma_i)$$
 (8)

$$\alpha \sim \text{Normal}(0, 0.2)$$
 (9)

$$\alpha_{E[i],HS[i]} \sim \text{Normal}(0,0.3)$$
 (10)

$$\beta_{A.HS[i]} \sim \text{Normal}(0, 0.3)$$
 (11)

$$\beta_{P,HS[i]} \sim \text{Normal}(0, 0.3)$$
 (12)

while the hyper-priors were defined as follows:

$$\mu_M \sim \text{Normal}(0, 0.5)$$
 (13)

$$\sigma_M \sim \text{Exponential}(1)$$
 (14)

$$\mu_b \sim \text{Normal}(0, 0.2)$$
 (15)

$$\sigma_b \sim \text{Exponential}(1)$$
 (16)

$$\mu_i \sim \text{Normal}(0, 0.2)$$
 (17)

$$\sigma_i \sim \text{Exponential}(1)$$
 (18)

where  $\mu_M$  represent the average 'sample size' and  $\sigma_M$  the variability of such average. Moreover,  $\mu_b$  and  $\mu_i$  represent the average block and children random effect, respectively. Finally, in a similar manner,  $\sigma_b$  and  $\sigma_i$  represent the variability present at the blocks and children, respectively (see section 3.1).

### A.5.4. Estimation procedure

The proposed models in Table 1 were estimated under the Bayesian framework. More specifically, we used the No-U-Turn Hamiltonian Monte Carlo algorithm (No-U-Turn HMC) [3, 23, 43, 55] implemented in Stan [67]. We used four chains of 2000 iterations each, from which the first 1000 were discarded as a warm-up required by the software, leaving 1000 effective iterations.

Additionally, all procedures were performed in R 4.1.2 [61] and its integration packages [66], in a 64-bit system with a MINGW 32-bit cross-compiler (x86\_64-w64-mingw32/x64).

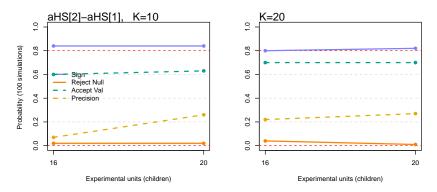


Figure 8: Group contrasts: power on small hearing group differences ( $\approx 0.15$ )

#### A.5.5. Simulation

Prior to fitting real data, all the proposed models were tested on simulated data. The simulation was done with two purposes: (i) to test the models' ability to recover the 'real' parameter values [35], and (ii) to test the power of our data size and assumed hypothesis [48]. On both instances, we used the *equivalent* prior sampling method [76], using an idealized data informed by the appropriate children population [19].

The results of our simulations highlight two key points. First, regarding the models ability to recover the 'real' estimate values, the probabilistic implementations work as intended, i.e. the statistical models manage to recover the 'real' values, if enough sample size is available.

Second, regarding the power of our data to affirm parameter estimates, reject null hypothesis, or provide enough precision for our inferences, three additional points can be made. On the one hand, assuming a small difference among the hearing status groups (approximately 0.15), sixteen children per group are enough to provide at least 60% certainty that our estimates affirm the predicted value, i.e. our model can correctly estimate values different from zero, when such alternative hypothesis is true (see green discontinuous line in figure 8). Moreover, the previous power threshold surpasses 80% if we assume medium group differences (approximately 0.4, not shown). Furthermore, in the case of other parameters of interest, even if the assumptions involve small effects (e.g. bA = 0.15 or bP = 0.1), our results always show the specific assumed value is tenable with power above 80%.

In contrast, the power analysis also reveal that with sufficient amount of variability at the children and replicates levels ( $\sigma_i = 0.5$  and  $M_i = 10$ ), the models do not have enough power to produce unequivocal null hypothesis rejections (see orange continuous lines in figure 8), i.e. the compatibility and highest posterior density intervals contain the value of zero, in almost all simulations. The latter implies that with reasonable expectations about the variability between children and the presence of measurement error (multiple replicates to measure one latent value), the statistical models require a data size significantly larger than sixteen children per group. Further model testing indicate that such unequivocal inferences can be accomplished, if we have a sample size similar to the full population size (70 children per group).

Lastly, and complementary to the previous result, the statistical precision of our estimates do not achieve power levels above the 80% threshold with our current data size (see yellow discontinuous line in figure 8). The latter implies that with sixteen children per group, the standard error of our estimates will not allow us to produce definite conclusions, e.g. we will not be certain if the two *hearing status* groups are not different because they are truly not statistically different or because the sample size is not enough to produce unequivocal inferences. This result is also related to the assumptions regarding the variability between children and the presence of measurement error. Similar to the previous case, sufficient levels of precision power can be reached, if we have a sample size similar to the full population size.

For more details on the assumed effects and the simulation code, refer to the GitHub repository: https://github.com/jriveraespejo/PhD\_UA\_paper1

#### A.5.6. Model selection

As stated in previous sections, the current research used the Information-Theoretic Approach [1, 12] for model selection. The application of the approach required: (i) the expression of the research hypothesis into statistical models, (ii) the selection of the most plausible models, and (iii) to produce inferences based on one or multiple selected models. Since the first step is covered in sections 2.4 and 2.5, and expanded in supplementary section A.5, here we proceed with the intermediate step.

We used the widely applicable information criterion (WAIC) [72], and the Pareto-smoothed importance sampling cross-validation (PSIS) [71] as the criteria to select among competing models. Two reasons justify our decision. First, both criteria allow us to use all the information of our Bayesian models, i.e. the posterior distribution of the parameters. Last, and more important, both criteria provide us with the best approximations for the out-of-sample (cross-validated) deviance [53]. The deviance is the best approximation for the Kullback-Liebler (KL) divergence [49], i.e. a measure of how far a model is from describing the *true* distribution of our data. In that sense, by comparing the deviance between competing models, we can measure which model is the farthest from 'perfect predictive accuracy' for our data [53].

Table 5 and 6 report the criteria for all the proposed models, sorted by the appropriate statistic. Three patterns are visible from the tables. First, we notice that around 63% of the evidence (WE) support two types of models: (a) no interaction and one estimated 'sample size', and (b) three (similar) interaction models with one estimated 'sample size'. Furthermore, 35% of the evidence is condensed in the diverse types of *robust* models, while the remaining 2% is negligible dispersed in the remaining ones.

Second, comparing the differences in WAIC/PSIS from the 'best' model (dWAIC and dPSIS, respectively), we arrive at the same conclusion as the previous paragraph, i.e. the model with no interaction and one estimated 'sample size' is the best model, followed by the interaction models with one 'sample size', and a bit further away, by the *robust* models. One important point to highlight is that, even when there seem to be a hierarchy of fit among the models, effectively, all of these are indistinguishable from each other, as it can be inferred from their precision estimate (dSE). However, we can also observe, a more precise support for models with any type of interaction and one estimated 'sample size', than for the *robust* models.

Third, we observe a greater over-fitting penalty (pWAIC and pPSIS, respectively) for models with a fixed 'sample size' than any other model. This is quite particular, as one would expect that a model with less parameters would over-fit less the data. However in this case, it implies the complexity of the data requires more parameters, especially considering there might be some highly influential observations that might sway the estimates of the less parameterized models (see section 3.5).

Model	Name	WAIC	SE	dWAIC	dSE	pWAIC	WE		
3	No interaction (one 'size')	-621.0	42.99	0.0	_	31.1	0.18		
10	Full interaction (one 'size')	-621.0	42.98	0.1	0.78	31.2	0.18		
9	Etiology interaction (one 'size')	-620.7	43.07	0.4	0.48	31.2	0.15		
8	Age interaction (one 'size')	-620.2	42.91	0.8	0.76	32.1	0.12		
11	Age interaction (robust)	-620.1	42.70	0.9	2.21	34.2	0.12		
12	Etiology interaction (robust)	-619.9	42.77	1.1	2.06	34.4	0.10		
4	No interaction (robust)	-619.2	42.81	1.8	2.18	34.8	0.07		
13	Full interaction (robust)	-618.8	42.65	2.2	2.17	35.0	0.06		
5	Age interaction (fixed 'size')	-578.2	52.51	42.8	16.85	50.7	0.00		
6	Etiology interaction (fixed 'size')	-578.2	52.63	42.8	16.95	50.7	0.00		
2	No interaction (fixed 'size')	-577.6	52.59	43.5	16.97	51.0	0.00		
1	Intercept only (fixed 'size')	-576.8	52.98	44.3	17.40	51.8	0.00		
7	Full interaction (fixed 'size')	-575.8	52.58	45.3	16.96	52.1	0.00		
SE	WAIC approximate standard error	WAIC approximate standard error							
dWAIC	difference in WAIC from the best model								
dSE	standard error for the difference in WAIC from the best model								
pWAIC	WAIC over fitting penalty								
WE	weight of evidence								

Table 5: Fit of statistical models: WAIC.

Model	Name	PSIS	SE	dPSIS	dSE	pPSIS	WE	
3	No interaction (one 'size')	-619.8	42.98	0.0	_	31.8	0.22	
10	Full interaction (one 'size')	-619.7	42.97	0.0	0.82	31.8	0.22	
9	Etiology interaction (one 'size')	-619.2	43.05	0.5	0.51	32.0	0.17	
8	Age interaction (one 'size')	-619.0	42.89	0.7	0.81	31.8	0.15	
11	Age interaction (robust)	-617.8	42.70	2.0	2.19	35.4	0.08	
12	Etiology interaction (robust)	-617.7	42.77	2.1	2.07	35.5	0.08	
4	No interaction (robust)	-616.5	42.81	3.3	2.19	36.1	0.04	
13	Full interaction (robust)	-616.3	42.64	3.4	2.13	36.2	0.04	
6	Etiology interaction (fixed 'size')	-576.0	52.63	43.7	17.00	51.7	0.00	
5	Age interaction (fixed 'size')	-575.9	52.54	43.9	16.94	51.9	0.00	
2	No interaction (fixed 'size')	-575.3	52.59	44.4	17.03	52.1	0.00	
1	Intercept only (fixed 'size')	-574.6	52.97	45.1	17.44	52.9	0.00	
7	Full interaction (fixed 'size')	-573.8	52.61	46.0	17.01	53.1	0.00	
SE	WAIC approximate standard error							
dPSIS	difference in PSIS from the best model							
dSE	standard error for the difference in PSIS from the best model							
pPSIS	PSIS over fitting penalty							
WE	weight of evidence							

Table 6: Fit of statistical models: PSIS.

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