

Causes and effects in Dichotomous Comparative Judgments: an information-theoretical system of plausible mechanism

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Abstract

Dichotomous Comparative Judgment (DCJ) requires judges to compare pairs of stimuli to determine which one exhibits a higher degree of a specific trait. DCJ has proven effective and reliable across various fields (Pollitt, 2012b; Jones, 2015; van Daal et al., 2019; Bartholomew et al., 2018; Lesterhuis, 2018; Bartholomew and Williams, 2020; Marshall et al., 2020; Boonen et al., 2020). However, despite the method's widespread use, existing literature lacks a clear explanation of the complexities and assumptions underpinning the DCJ system, as well as the plausible mechanisms through which DCJ data could be generated. This study addresses these issues by representing DCJ within the framework of causal inference. Specifically, utilizing the structural approach, the study develops a scientific model to clarify plausible causal assumptions and mechanisms inherent in the DCJ system. The study then translates this model into a probabilistic statistical model to estimate statistical relationships and infer causal effects within the system. This research provides a robust probabilistic foundation for the statistical analysis of DCJ data, building upon Thurstone's law of comparative judgment (1927). Its findings offer valuable insights for researchers and analysts designing and implementing DCJ experiments.

Keywords: causal inference, probability, Thurstone, comparative judgement, directed acyclic graph, structural causal models, statistical modeling

1. Introduction

In contemporary contexts, Thurstone's law of comparative judgment (1927) primarily refers to the method of *dichotomous* comparative judgment (DCJ, Pollitt, 2012a,b). In DCJ, a judge assesses the relative manifestation of a *trait* within a pair of stimuli. This assessment results in a dichotomous value indicating which stimulus possesses a

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higher degree of the trait. After different judges perform multiple rounds of pairwise comparisons, an outcome vector is produced. This vector is modeled using the Bradley-Terry-Luce model (BTL, [Bradley and Terry, 1952](#); [Luce, 1959](#)), which creates a score that corresponds with the trait of interest. This score is then used to rank the stimuli from lowest to highest or to evaluate the influence of certain variables on the stimuli's positions in the ranking.

DCJ has proven effective in assessing competencies and traits predominantly within the educational realm, as demonstrated by [Pollitt \(2012b\)](#), [Jones \(2015\)](#), [van Daal et al. \(2019\)](#), [Bartholomew et al. \(2018\)](#), [Lesterhuis \(2018\)](#), [Bartholomew and Williams \(2020\)](#), and [Marshall et al. \(2020\)](#). However, its application transcends education, as exemplified by [Boonen et al. \(2020\)](#). The methodology has also evolved to include multiple, as opposed to pairwise comparisons ([Luce, 1959](#); [Plackett, 1975](#)), and to accommodate comparisons with ordinal outcomes ([Tutz, 1986](#); [Agresti, 1992](#)). Overall, research suggests that DCJ offers an alternative and efficient approach to measurement and evaluation, characterized by its reliability and validity ([Lesterhuis, 2018](#); [van Daal, 2020](#); [Marshall et al., 2020](#); [Bouwer et al., 2023](#)). Nevertheless, despite the method's widespread use, existing literature lacks a clear representation of the plausible mechanisms through which DCJ data could be generated. Particularly, there is no depiction of the complexity and the assumptions underpinning the DCJ system, nor how different assessment factors can potentially influence the observed DCJ outcome.

According to [Verhavert et al. \(2019\)](#) and [van Daal \(2020\)](#), several assessment factors interact and influence the method's outcome. These factors include the number and characteristics of the stimuli, their *proximity* in terms of the assessed trait, the number of comparison per stimulus, and the pairing algorithm used. Furthermore, since the method relies on judges' assessments, the number and characteristics of judges, their *discrimination* abilities, and the number of comparisons per judge also play pivotal roles. Moreover, when the stimuli represent sub-units of higher-levels units, factors such as the number and characteristics of these units, along with their *proximity* in terms of the assessed trait, can significantly influence the outcome. For instance, [van Daal et al. \(2019\)](#) assessed academic writing skills of university students (units) using multiple argumentative essays (sub-units).

Although several studies have examined the individual impact of these factors on the method's reliability ([Bramley, 2015](#); [Pollitt, 2012b](#); [Bramley and Vitello, 2019](#); [Verhavert et al., 2019](#); [Crompvoets et al., 2022](#); [van Daal et al., 2017](#); [Gijzen et al., 2021](#); [Bouwer et al., 2023](#)), none, to the best of the authors' knowledge, have provided a transparent depiction of the DCJ system and the mechanisms generating the DCJ outcome. This study aims to fill this gap by representing DCJ within the framework of causal inference. Specifically, utilizing the structural approach, the study develops a scientific model to clarify plausible causal assumptions and mechanisms inherent in the DCJ system. The study then translates the scientific model into a probabilistic statistical model. This model aims to produce statistical estimates to draw inferences about plausible causal relationships within the DCJ system.

Ultimately, this study provides a robust causal and probabilistic foundation for the statistical analysis of DCJ data, building upon Thurstone's law of comparative judgment ([1927](#)). Consequently, its findings offer valuable insights for researchers and analysts

designing and implementing DCJ experiments.

2. Theoretical framework

This section introduces fundamental concepts in causal inference, such as directed acyclic graphs (DAGs), structural causal models (SCMs), and the flow of association and causation in graphs. The section is not a comprehensive description of causal inference methods. Readers interested in deeper exploration should consult introductory papers like [Pearl \(2010\)](#), [Rohrer \(2018\)](#), [Pearl \(2019\)](#), and [Cinelli et al. \(2020\)](#). They may also find introductory books such as [Pearl and Mackenzie \(2018\)](#), [Neal \(2020\)](#) and [McElreath \(2020\)](#) useful. For more advanced study, seminal intermediate papers like [Neyman \(1923\)](#), [Rubin \(1974\)](#), [Spirtes et al. \(1991\)](#), and [Sekhon \(2009\)](#), as well as books such as [Pearl \(2009\)](#), [Morgan and Winship \(2014\)](#) and [Hernán and Robins \(2020\)](#) are recommended.

2.1. The structural approach to causal inference

In statistics, *causal inference* refers to the process of identifying the causes of a phenomenon and estimating their effects using data ([Shaughnessy et al., 2010](#); [Neal, 2020](#)). Unlike classical statistical modeling, which focuses solely on summarizing data and inferring associations, causal inference provides a coherent mathematical notation for analyzing causes and counterfactuals ([Pearl, 2009](#)).

Counterfactuals represent scenarios *contrary to fact*, where alternative *potential* outcomes resulting from a cause are neither observed nor observable ([Neal, 2020](#); [Counterfactual, 2024](#)). According to [Pearl and Mackenzie \(2018\)](#), counterfactuals are the foundation of causal inference and occupy the highest level of cognitive abstraction in the ladder of causation, followed by intervention and association. Nevertheless, despite their abstract nature, counterfactuals enable the development of a *theory of the world* that explains why specific causes have specific effects and what occurs in their absence ([Pearl and Mackenzie, 2018](#)). They achieve this by translating causal statements into counterfactual statements, that is, statements about “what would have happened in the world under different circumstances.”

Several approaches to causal inference and counterfactuals exist, but two are particularly prominent: the potential outcomes approach, also known as the Neyman-Rubin causal model ([Neyman, 1923](#); [Rubin, 1974](#)), and the structural approach ([Pearl, 2009](#); [Pearl et al., 2016](#)). Both approaches employ rigorous mathematical notation to characterize causal inference, but they do so in different ways ([Neal, 2020](#)). The potential outcomes approach relies on counterfactual notation, whereas the structural approach employs the do-operator and structural causal models (SCM, [Pearl, 2009](#); [Pearl et al., 2016](#)). Despite these differences, both notations can be expressed in terms of the other, and both approaches provide methods for using experimental and observational data to estimate causal effects ([Pearl, 2010](#)).

However, the structural approach offers an additional key advantage over the potential outcomes approach: it enables the graphical representation of any system through directed acyclic graphs (DAG, [Gross et al., 2018](#); [Neal, 2020](#)). DAGs serve as heuristics, effectively conveying the assumed causal structure of a system ([Pearl et al., 2016](#)).

A heuristic is a strategy that simplifies information to make decisions more quickly, efficiently, and sometimes more accurately than complex methods (Chow, 2015). Consequently, DAGs do not represent detailed statistical models but allow researchers to deduce which statistical models can provide valid causal inferences, assuming the causal structure depicted in the DAGs are accurate (McElreath, 2020).

2.2. DAGs and SCMs

Graph theory is a branch of mathematics focused on the study of graphs. Graphs are mathematical structures modeling pairwise relations between objects. They can represent physical relations, such as electrical circuits and roadways, and less tangible structures, such as ecosystems and sociological relations. Graphs have proven useful in various fields, including computer science, operations research, and the natural and social sciences (Gross et al., 2018).

In statistics, one application incorporating concepts from graph theory is causal inference. Specifically, the structural approach to causal inference uses directed acyclic graphs (DAG) to provide a graphical and formal representation of the causal structure of a system (Neal, 2020). In this context, a *graph* denotes a collection of nodes connected by edges, where nodes represent random variables. The term *directed* indicates the edges of the graph extend from one node to another, with arrows showing the direction of causal influence. Moreover, the term *acyclic* indicates the causal influences do not form a loop, meaning the influences do not cycle back on themselves (McElreath, 2020). Several examples of DAGs can be found in Figure 1.

DAGs offer two key advantages for modeling causal structures. Firstly, they represent causal relations in a nonparametric and fully interactive manner. This feature allows for feasible causal analysis strategies without needing the specification of the type of data or the nature of the functional dependence among variables (Morgan and Winship, 2014). Secondly, regardless of complexity, DAGs can represent various causal structures using only five fundamental building blocks (Neal, 2020; McElreath, 2020). This feature enables the decomposition of complex structures into basic building blocks, facilitating the analysis of these structures by focusing on the causal assumptions associated with each building block individually (McElreath, 2020). These building blocks can be represented in three ways: the magnified representation, the standard representation, and the structural causal model form (SCM, Morgan and Winship, 2014).

The left panels of Figure 1 illustrate the *magnified* representation. These graphs depict the *endogenous* variables $V = \{X, Z, Y\}$ alongside the *exogenous* variables $E = \{e_X, e_Z, e_Y\}$. Endogenous variables are those whose causal mechanisms the investigator chooses to model (Neal, 2020). In contrast, exogenous variables represent *errors* or *disturbances* arising from omitted factors that the investigator chooses not to model explicitly (Pearl, 2009, 27,68). The graphs show endogenous variables as solid black circles to signify that they are observed random variables, while endogenous variables are depicted as open circles to signify their unobserved (latent) nature. Lastly, the arrows in the graphs reflect the expected direction of causal influences among these variables.

Often, DAGs omit the exogenous variables for simplicity, resulting in the *standard* representation. However, including exogenous variables in a graph can be beneficial

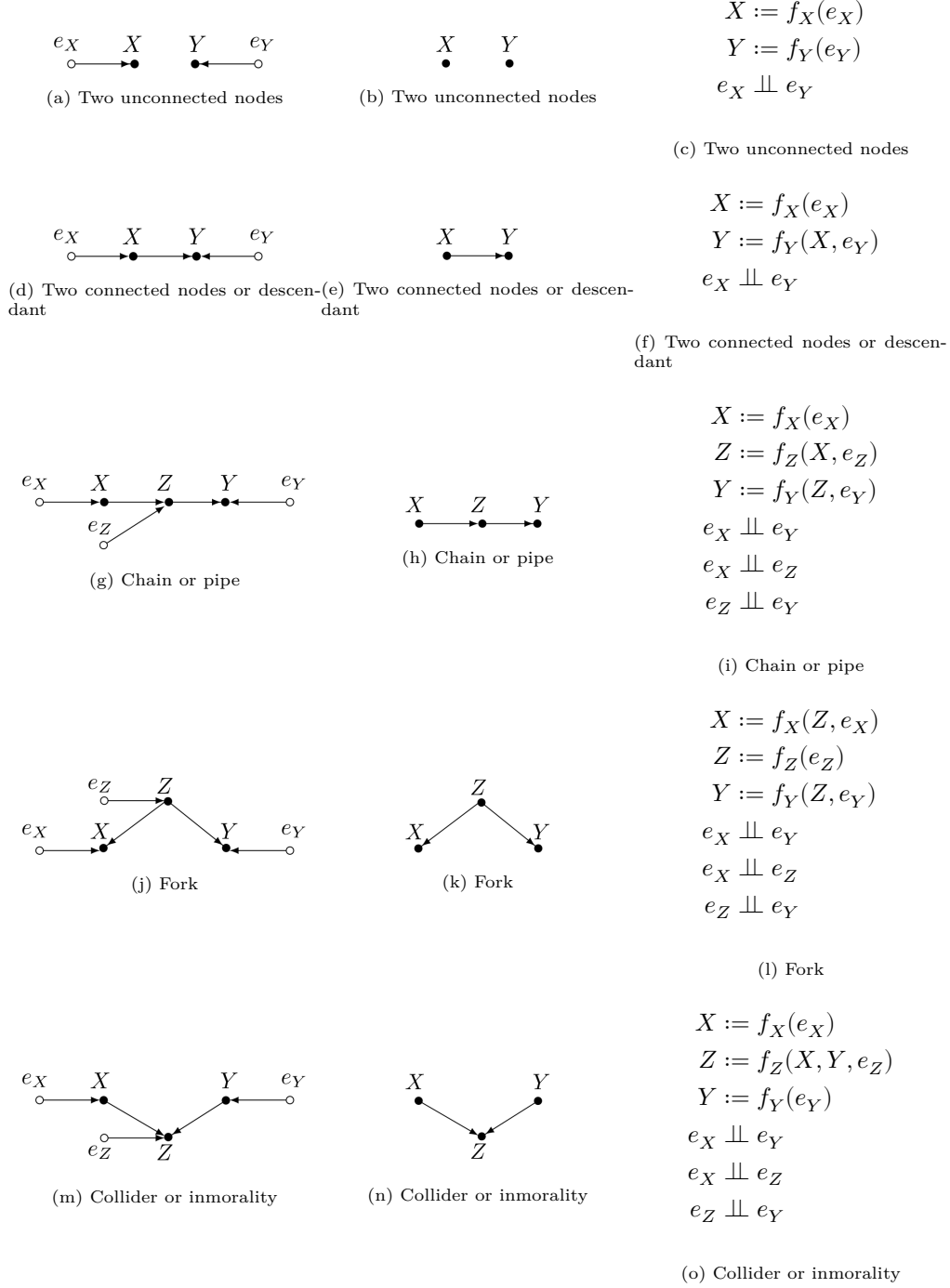


Figure 1: The five fundamental building blocks of DAGs. **Note:** left panels show the magnified representation, middle panels show the standard representation, and the right panels show their corresponding SCM form.

in some scenarios, as their presence can reveal potential issues related to conditioning and confounding (Cinelli et al., 2020), concepts explored in the following section. The standard representation is illustrated in the middle panels of Figure 1.

Lastly, the right panels of Figure 1 depict the SCM form of the fundamental building blocks. SCMs are formal mathematical models defined by a set of endogenous variables V , a set of exogenous variables E , and a set of functions $F = \{f_X, f_Z, f_Y\}$ (Pearl, 2009; Neal, 2020). These functions, referred to as structural equations, specify each endogenous variable as nonparametric functions of other variables. Moreover, SCMs use the symbol ‘:=’ to indicate the variables’ asymmetrical causal dependence and the symbol ‘ $\perp\!\!\!\perp$ ’ to represent *d-separation*, which roughly equates to the concept of variable independence. The concepts of d-separation and causal (in)dependence are explored in the following section.

A careful examination of Figure 1 highlights the assumptions underlying these building blocks. Figures 1a, 1b, and SCM 1c depict two unconnected nodes, representing a scenario where variables X and Y are not causally related. Figures 1d, 1e, and SCM 1f illustrate two connected nodes, showing a scenario where a *parent* node X exerts a causal influence on a *child* node Y . Consequently, Y is considered a *descendant* of X . Figures 1g, 1h, and SCM 1i depict a *chain* or *pipe*, where X influences Z , and Z influences Y . In this configuration, X is a parent node of Z , and Z is a parent node of Y . This creates a *directed path* between X and Y . Consequently, X is an *ancestor* of Y , and Z fully *mediates* the relationship between the two. Figures 1j, 1k, and SCM 1l illustrate a *fork*, where variables X and Y are both influenced by Z . Here, Z is a parent node of X and Y . Finally, Figures 1m, 1n, SCM 1o depict a *collider*, also known as *immorality*, where variables X and Y are concurrent causes of Z . In this configuration, X and Y are not causally related to each other but both influence Z . Additionally, in all SCMs, the errors are assumed to be mutually independent of each other and of all other variables in the graph, as evidenced by the pairwise relations $e_X \perp\!\!\!\perp e_Y$, $e_X \perp\!\!\!\perp e_Z$, and $e_Z \perp\!\!\!\perp e_Y$.

2.3. The flow of association and causation in graphs

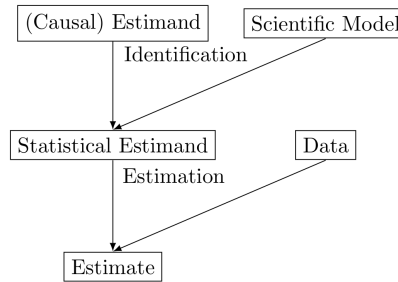


Figure 2: Identification-Estimation flowchart. Extracted from Neal (2020, 32)

2.4. A motivating example

Given the heuristic nature of DAGs, a motivating example can help clarify how to use the five fundamental building blocks to construct the causal structure of a system. Consider a research problem where the causal effect of a variable T on an outcome Y

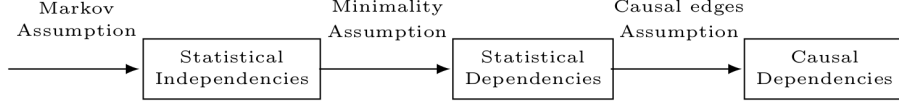


Figure 3: The flow of association and causation in graphs. Extracted from [Neal \(2020, 31\)](#)

needs investigation. The problem suggests that a variable X potentially influences both T and Y . Beyond these relationships, the problem does not specify any further variables of interest. Such scenarios are not hard to imagine. For instance, T might represent different treatments that could affect the recovery from cancer Y , while X could denote the patient's age. Similarly, in the context of a DCJ study like the one described by [Boonen et al. \(2020\)](#), T could represent the duration of a child's cochlear implant use, which might influence the child's overall speech quality Y , with X indicating the child's hearing status. (not a bad example, but I prefer one using writing skills)

Figure 4 illustrates the plausible causal structure of the motivating example. A detailed examination of Figures 4a, 4b, and SCM 4c reveals the presence of at least four of the five fundamental building blocks. The figures display multiple descendants, as indicated by pairwise relations such as $X \rightarrow T$, $X \rightarrow Y$, and $T \rightarrow Y$. Additionally, the figures features multiple pairs of unconnected nodes, evident from the relations $e_T \perp\!\!\!\perp e_X$, $e_T \perp\!\!\!\perp e_Y$, and $e_X \perp\!\!\!\perp e_Y$. Finally, the figures illustrate the fork $X \rightarrow \{T, Y\}$, and two colliders with $\{X, e_T\} \rightarrow T$ and $\{X, T, e_Y\} \rightarrow Y$.

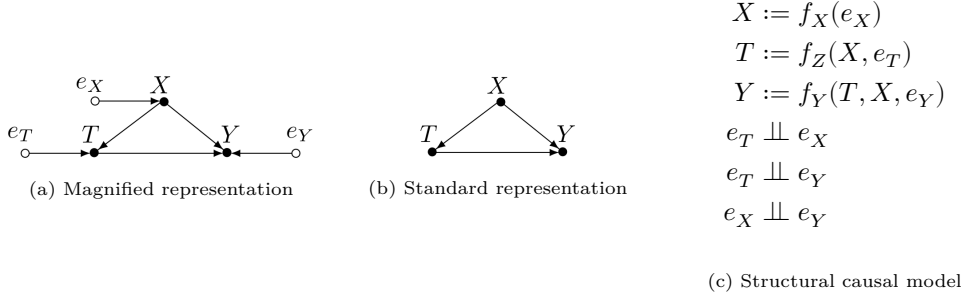


Figure 4: DAGs for a plausible causal structure in a system.

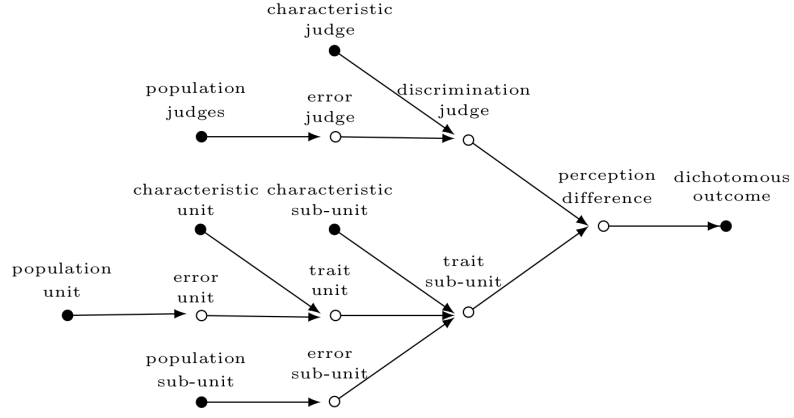


Figure 5: DCJ causal diagram, simplified description

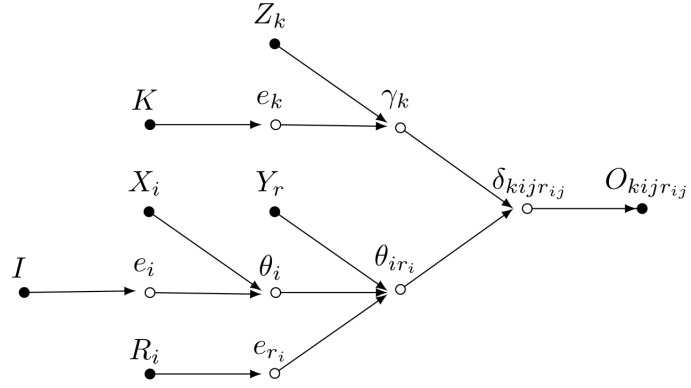


Figure 6: DCJ causal diagram, simplified mathematical description

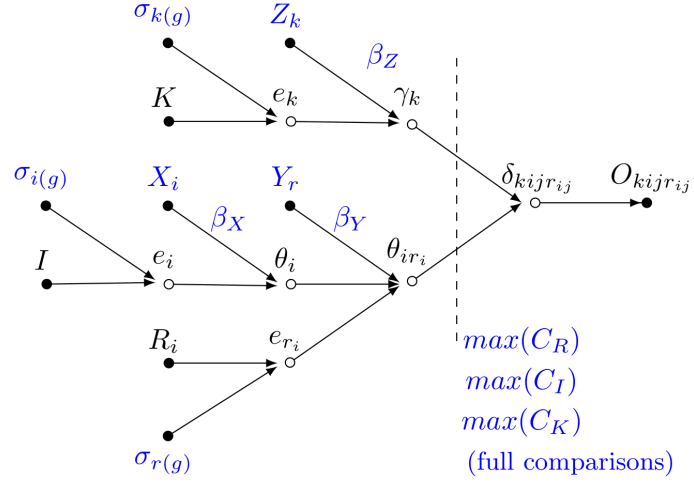


Figure 7: DCJ causal diagram, population mathematical description

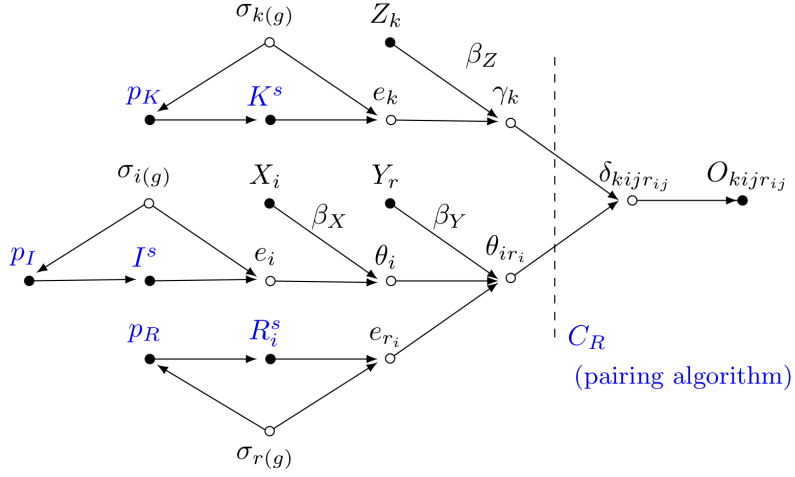


Figure 8: DCJ causal diagram, sample with comparisons mathematical description

3. Theory

3.1. A scientific model for the DCJ

3.2. Probabilistic assumptions of the scientific model

3.3. From the scientific to statistical model

3.4. Let's talk about Thurstone

4. Discussion

4.1. Findings

4.2. Limitations and further research

5. Conclusion

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6. Appendix

- 6.1. Why do we need to estimate judges' abilities?*
- 6.2. Latent variables as a mean of imputation*
- 6.3. Other comparative scenarios*

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