

## Data Science II: Homework 4

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**QUESTION 1:** In this exercise, we will build tree-based models using the College data (see “College.csv” in Homework 2). The response variable is the out-of-state tuition (Outstate). Partition the dataset into two parts: training data (80%) and test data (20%).

```
# initial data steps--importing and partitioning
College = read.csv("College.csv")
head(College)
```

```
##              College Apps Accept Enroll Top10perc Top25perc
## 1 Abilene Christian University 1660   1232    721      23      52
## 2           Adelphi University 2186   1924    512      16      29
## 3           Adrian College 1428   1097    336      22      50
## 4           Agnes Scott College 417    349    137      60      89
## 5      Alaska Pacific University 193    146     55      16      44
## 6           Albertson College 587    479    158      38      62
##   F.Undergrad P.Undergrad Outstate Room.Board Books Personal PhD Terminal
## 1          2885          537    7440      3300   450    2200   70      78
## 2          2683         1227   12280      6450   750    1500   29      30
## 3          1036           99   11250      3750   400    1165   53      66
## 4           510           63   12960      5450   450     875   92      97
## 5           249          869    7560      4120   800    1500   76      72
## 6           678           41   13500      3335   500     675   67      73
##   S.F.Ratio perc.alumni Expend Grad.Rate
## 1         18.1         12   7041      60
## 2         12.2         16  10527      56
## 3         12.9         30   8735      54
## 4          7.7         37  19016      59
## 5         11.9          2  10922      15
## 6          9.4         11   9727      55
```

```
datSplit = initial_split(data = College, prop = 0.8)
trainData = training(datSplit)
testData = testing(datSplit)
head(trainData)
```

```
##              College Apps Accept Enroll Top10perc Top25perc F.Undergrad
## 1 Bellarmine College 807    707    308      39      63      1198
## 2          Barat College 261    192    111      15      36      453
## 3 Columbia College MO 314    158    132      10      28      690
## 4      Augsburg College 662    513    257      12      30     2074
## 5      Morehouse College 3708   1678    722      41      66     2852
```

```
set.seed(1)
tree1 = rpart(formula = Outstate ~ . - College,
               data = trainData,
               control = rpart.control(cp=0))
rpart.plot(tree1) #this gives the full tree, but we want a more complex and smaller tree
```

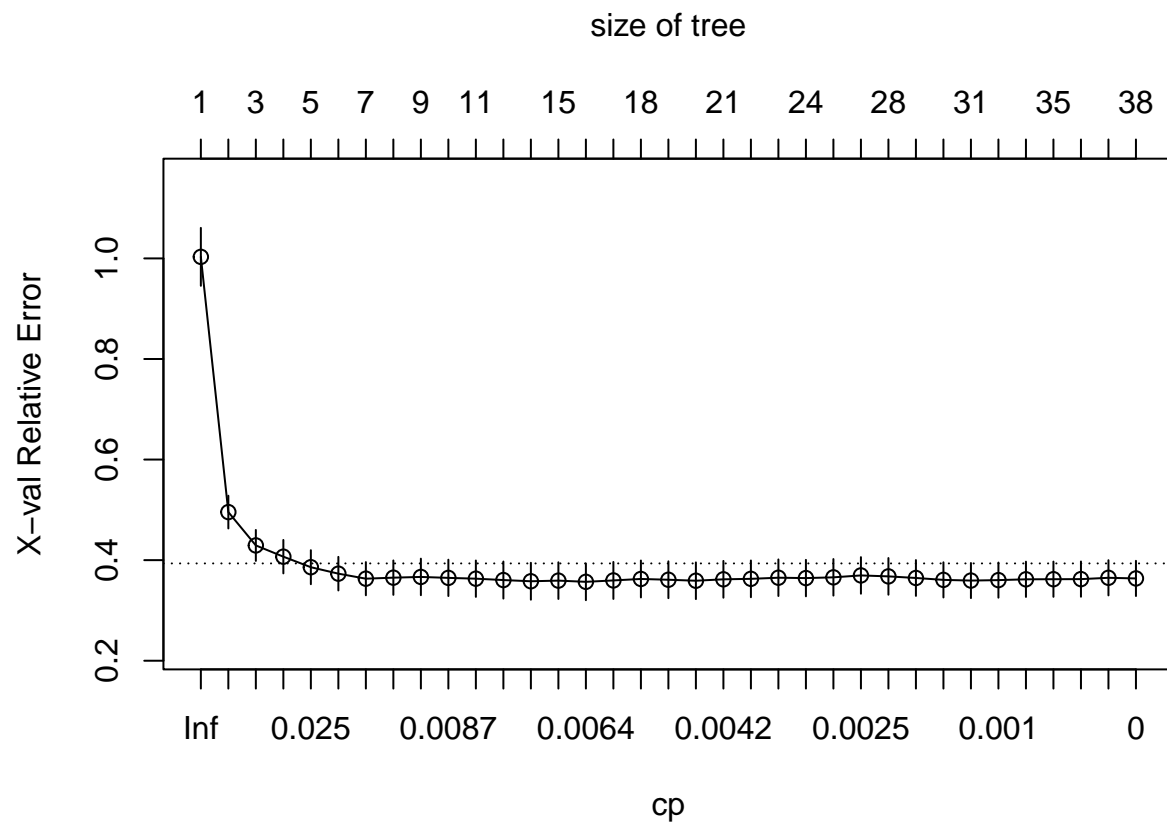
[illegible]

2

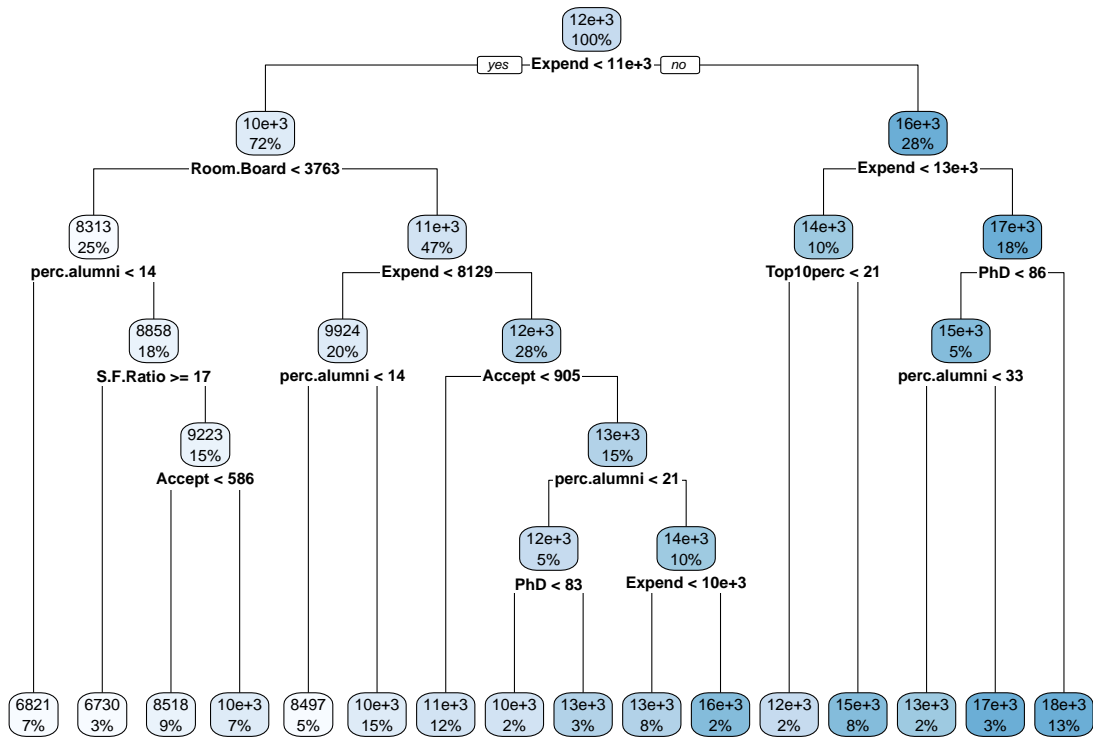
```
printcp(tree1)
```

```
##
## Regression tree:
## rpart(formula = Outstate ~ . - College, data = trainData, control = rpart.control(cp = 0))
##
## Variables actually used in tree construction:
## [1] Accept      Apps      Expend      F.Undergrad Grad.Rate  P.Undergrad
## [7] perc.alumni Personal  PhD        Room.Board  S.F.Ratio  Terminal
## [13] Top10perc
##
## Root node error: 6345327363/452 = 14038335
##
## n= 452
##
##      CP nsplit rel error  xerror   xstd
## 1  0.51835135    0  1.00000 1.00308 0.057594
## 2  0.09850360    1  0.48165 0.49558 0.032540
## 3  0.04087938    2  0.38315 0.42928 0.030790
## 4  0.03428521    3  0.34227 0.40693 0.033279
## 5  0.01863879    4  0.30798 0.38599 0.033861
## 6  0.01752037    5  0.28934 0.37314 0.033396
## 7  0.01436278    6  0.27182 0.36315 0.033017
## 8  0.01003387    7  0.25746 0.36520 0.034232
## 9  0.00882200    8  0.24742 0.36663 0.036351
## 10 0.00852605    9  0.23860 0.36478 0.036147
## 11 0.00834425   10  0.23008 0.36315 0.036175
## 12 0.00723941   12  0.21339 0.36041 0.036853
## 13 0.00690162   13  0.20615 0.35804 0.036713
## 14 0.00640576   14  0.19925 0.35930 0.036468
## 15 0.00639032   15  0.19284 0.35694 0.036539
## 16 0.00534616   16  0.18645 0.35966 0.036782
## 17 0.00513089   17  0.18110 0.36259 0.036738
## 18 0.00466995   18  0.17597 0.36105 0.036650
## 19 0.00437217   19  0.17130 0.35907 0.036494
## 20 0.00407089   20  0.16693 0.36190 0.036567
## 21 0.00339007   21  0.16286 0.36284 0.036564
## 22 0.00294261   22  0.15947 0.36508 0.036358
## 23 0.00282619   23  0.15653 0.36435 0.036260
## 24 0.00279247   24  0.15370 0.36584 0.036330
## 25 0.00215660   26  0.14812 0.36962 0.036417
## 26 0.00208123   27  0.14596 0.36772 0.036467
## 27 0.00156288   28  0.14388 0.36453 0.035635
## 28 0.00123992   29  0.14232 0.36076 0.034953
## 29 0.00106361   30  0.14108 0.35942 0.034906
## 30 0.00100411   31  0.14001 0.36031 0.034953
## 31 0.00095590   33  0.13800 0.36192 0.035074
## 32 0.00091077   34  0.13705 0.36211 0.035072
## 33 0.00080953   35  0.13614 0.36228 0.035069
## 34 0.00025201   36  0.13533 0.36492 0.035007
## 35 0.00000000   37  0.13508 0.36366 0.035014
```

```
cpTable = tree1$cptable
plotcp(tree1)
```



```
# Picking the cp that yields the minimum cross-validation error
minErr = which.min(cpTable[,4])
tree3 = rpart::prune(tree1, cp = cpTable[minErr,1])
rpart.plot(tree3)
```



```
plot(as.party(tree3)) #another visual
```



```

##          30          14          12          11          10          8
## Room.Board perc.alumni      Accept  S.F.Ratio      Enroll F.Undergrad
##          5          2          2          1          1          1
##   Grad.Rate P.Undergrad
##          1          1
##
## Node number 1: 452 observations,      complexity param=0.5183513
##   mean=11903.88, MSE=1.403833e+07
##   left son=2 (326 obs) right son=3 (126 obs)
##   Primary splits:
##       Expend      < 10939.5 to the left,  improve=0.5183513, (0 missing)
##       Terminal    < 84.5    to the left,  improve=0.3748716, (0 missing)
##       PhD         < 78.5    to the left,  improve=0.3667132, (0 missing)
##       Room.Board  < 3961    to the left,  improve=0.2904086, (0 missing)
##       Top10perc   < 35.5    to the left,  improve=0.2793795, (0 missing)
##   Surrogate splits:
##       Terminal    < 93.5    to the left,  agree=0.850, adj=0.460, (0 split)
##       PhD         < 89.5    to the left,  agree=0.836, adj=0.413, (0 split)
##       Top10perc   < 43.5    to the left,  agree=0.825, adj=0.373, (0 split)
##       Top25perc   < 74.5    to the left,  agree=0.810, adj=0.317, (0 split)
##       Apps        < 2647.5 to the left,  agree=0.794, adj=0.262, (0 split)
##
## Node number 2: 326 observations,      complexity param=0.0985036
##   mean=10226.83, MSE=6554930
##   left son=4 (112 obs) right son=5 (214 obs)
##   Primary splits:
##       Room.Board  < 3762.5 to the left,  improve=0.2924964, (0 missing)
##       Expend      < 8132    to the left,  improve=0.2810090, (0 missing)
##       Terminal    < 80.5    to the left,  improve=0.1938974, (0 missing)
##       Grad.Rate   < 61.5    to the left,  improve=0.1721348, (0 missing)
##       PhD         < 77.5    to the left,  improve=0.1621505, (0 missing)
##   Surrogate splits:
##       Expend      < 7115.5 to the left,  agree=0.718, adj=0.179, (0 split)
##       Terminal    < 63.5    to the left,  agree=0.709, adj=0.152, (0 split)
##       P.Undergrad < 66.5    to the left,  agree=0.702, adj=0.134, (0 split)
##       Grad.Rate   < 50.5    to the left,  agree=0.681, adj=0.071, (0 split)
##       Accept      < 184.5   to the left,  agree=0.669, adj=0.036, (0 split)
##
## Node number 3: 126 observations,      complexity param=0.03428521
##   mean=16242.92, MSE=7296120
##   left son=6 (44 obs) right son=7 (82 obs)
##   Primary splits:
##       Expend      < 13158   to the left,  improve=0.2366455, (0 missing)
##       Room.Board  < 5557.5   to the left,  improve=0.2232844, (0 missing)
##       Top25perc   < 74.5    to the left,  improve=0.2225995, (0 missing)
##       PhD         < 85.5    to the left,  improve=0.2130894, (0 missing)
##       Terminal    < 91.5    to the left,  improve=0.1909604, (0 missing)
##   Surrogate splits:
##       Top25perc   < 64.5    to the left,  agree=0.762, adj=0.318, (0 split)
##       Top10perc   < 36.5    to the left,  agree=0.754, adj=0.295, (0 split)
##       Books       < 462.5    to the left,  agree=0.722, adj=0.205, (0 split)
##       Terminal    < 89.5    to the left,  agree=0.722, adj=0.205, (0 split)
##       S.F.Ratio   < 13.25   to the right, agree=0.722, adj=0.205, (0 split)
##

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## Node number 4: 112 observations,      complexity param=0.01436278
##   mean=8312.83, MSE=4930922
##   left son=8 (30 obs) right son=9 (82 obs)
##   Primary splits:
##       perc.alumni < 13.5      to the left,  improve=0.1650237, (0 missing)
##       Expend      < 6215.5    to the left,  improve=0.1359266, (0 missing)
##       S.F.Ratio   < 15.05     to the right, improve=0.1348840, (0 missing)
##       Grad.Rate   < 44.5      to the left,  improve=0.1156903, (0 missing)
##       Room.Board  < 3050      to the left,  improve=0.1096671, (0 missing)
##   Surrogate splits:
##       Top25perc   < 28.5      to the left,  agree=0.750, adj=0.067, (0 split)
##       Room.Board  < 2536      to the left,  agree=0.750, adj=0.067, (0 split)
##       Apps        < 4254.5    to the right, agree=0.741, adj=0.033, (0 split)
##       Accept      < 170       to the left,  agree=0.741, adj=0.033, (0 split)
##       Enroll      < 1198.5    to the right, agree=0.741, adj=0.033, (0 split)
##
## Node number 5: 214 observations,      complexity param=0.04087938
##   mean=11228.55, MSE=4484142
##   left son=10 (89 obs) right son=11 (125 obs)
##   Primary splits:
##       Expend      < 8128.5    to the left,  improve=0.2703119, (0 missing)
##       Terminal    < 85.5      to the left,  improve=0.1910113, (0 missing)
##       Accept      < 932.5     to the left,  improve=0.1864649, (0 missing)
##       Apps        < 1181      to the left,  improve=0.1850094, (0 missing)
##       Grad.Rate   < 55.5      to the left,  improve=0.1783875, (0 missing)
##   Surrogate splits:
##       PhD         < 70.5      to the left,  agree=0.715, adj=0.315, (0 split)
##       Terminal    < 73.5      to the left,  agree=0.696, adj=0.270, (0 split)
##       S.F.Ratio   < 14.05     to the right, agree=0.673, adj=0.213, (0 split)
##       Top10perc   < 22.5      to the left,  agree=0.654, adj=0.169, (0 split)
##       Top25perc   < 43.5      to the left,  agree=0.654, adj=0.169, (0 split)
##
## Node number 6: 44 observations,      complexity param=0.007239407
##   mean=14449.11, MSE=5024178
##   left son=12 (7 obs) right son=13 (37 obs)
##   Primary splits:
##       Top10perc   < 20.5      to the left,  improve=0.2077970, (0 missing)
##       F.Undergrad < 1206      to the left,  improve=0.1726283, (0 missing)
##       Apps        < 1282      to the left,  improve=0.1672279, (0 missing)
##       Accept      < 917.5     to the left,  improve=0.1672279, (0 missing)
##       P.Undergrad < 346.5     to the right, improve=0.1283876, (0 missing)
##   Surrogate splits:
##       Top25perc   < 44        to the left,  agree=0.955, adj=0.714, (0 split)
##       Apps        < 433.5     to the left,  agree=0.886, adj=0.286, (0 split)
##       Accept      < 396       to the left,  agree=0.886, adj=0.286, (0 split)
##       Enroll      < 146       to the left,  agree=0.886, adj=0.286, (0 split)
##       F.Undergrad < 612       to the left,  agree=0.886, adj=0.286, (0 split)
##
## Node number 7: 82 observations,      complexity param=0.01863879
##   mean=17205.45, MSE=5862151
##   left son=14 (23 obs) right son=15 (59 obs)
##   Primary splits:
##       PhD         < 85.5      to the left,  improve=0.2460372, (0 missing)
##       Room.Board  < 5557.5    to the left,  improve=0.1810750, (0 missing)

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##      Grad.Rate < 67.5      to the left,  improve=0.1810398, (0 missing)
##      Terminal  < 91.5      to the left,  improve=0.1701871, (0 missing)
##      Apps      < 3335.5    to the left,  improve=0.1657770, (0 missing)
##      Surrogate splits:
##      Terminal  < 91.5      to the left,  agree=0.902, adj=0.652, (0 split)
##      Top10perc < 30.5      to the left,  agree=0.805, adj=0.304, (0 split)
##      Grad.Rate < 64.5      to the left,  agree=0.805, adj=0.304, (0 split)
##      Top25perc < 67.5      to the left,  agree=0.793, adj=0.261, (0 split)
##      Apps      < 827.5     to the left,  agree=0.780, adj=0.217, (0 split)
##
## Node number 8: 30 observations
##      mean=6821.467, MSE=2964807
##
## Node number 9: 82 observations,      complexity param=0.01003387
##      mean=8858.451, MSE=4538812
##      left son=18 (12 obs) right son=19 (70 obs)
##      Primary splits:
##      S.F.Ratio < 16.8      to the right, improve=0.17106710, (0 missing)
##      Grad.Rate < 44.5      to the left,  improve=0.12521090, (0 missing)
##      Books      < 680      to the right, improve=0.10664180, (0 missing)
##      Expend      < 8128.5   to the left, improve=0.08251206, (0 missing)
##      Terminal  < 82.5      to the left,  improve=0.08062386, (0 missing)
##      Surrogate splits:
##      Expend      < 5015     to the left, agree=0.915, adj=0.417, (0 split)
##      P.Undergrad < 1073     to the right, agree=0.890, adj=0.250, (0 split)
##      Apps      < 2081     to the right, agree=0.878, adj=0.167, (0 split)
##      Enroll      < 645.5    to the right, agree=0.878, adj=0.167, (0 split)
##      F.Undergrad < 2744.5   to the right, agree=0.878, adj=0.167, (0 split)
##
## Node number 10: 89 observations,      complexity param=0.008822004
##      mean=9923.787, MSE=2773243
##      left son=20 (21 obs) right son=21 (68 obs)
##      Primary splits:
##      perc.alumni < 13.5     to the left, improve=0.2268001, (0 missing)
##      Expend      < 7069.5   to the left, improve=0.1982358, (0 missing)
##      Grad.Rate < 57         to the left, improve=0.1705047, (0 missing)
##      Top10perc < 18.5      to the left, improve=0.1342929, (0 missing)
##      Apps      < 1438      to the left, improve=0.1302637, (0 missing)
##      Surrogate splits:
##      Grad.Rate < 50.5       to the left, agree=0.809, adj=0.190, (0 split)
##      S.F.Ratio < 21.75      to the right, agree=0.798, adj=0.143, (0 split)
##      Apps      < 250        to the left, agree=0.787, adj=0.095, (0 split)
##      Accept     < 226.5     to the left, agree=0.787, adj=0.095, (0 split)
##      Personal   < 1700      to the right, agree=0.787, adj=0.095, (0 split)
##
## Node number 11: 125 observations,      complexity param=0.01752037
##      mean=12157.54, MSE=3627158
##      left son=22 (55 obs) right son=23 (70 obs)
##      Primary splits:
##      Accept     < 905       to the left, improve=0.2452003, (0 missing)
##      Apps      < 1096       to the left, improve=0.2382105, (0 missing)
##      Terminal   < 82.5      to the left, improve=0.1962363, (0 missing)
##      Enroll     < 299       to the left, improve=0.1940069, (0 missing)
##      F.Undergrad < 1064.5   to the left, improve=0.1840590, (0 missing)

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## Surrogate splits:
## Apps < 1096 to the left, agree=0.968, adj=0.927, (0 split)
## Enroll < 299 to the left, agree=0.920, adj=0.818, (0 split)
## F.Undergrad < 1064.5 to the left, agree=0.872, adj=0.709, (0 split)
## PhD < 76.5 to the left, agree=0.728, adj=0.382, (0 split)
## Top25perc < 53.5 to the left, agree=0.720, adj=0.364, (0 split)
##
## Node number 12: 7 observations
## mean=12100, MSE=3566024
##
## Node number 13: 37 observations
## mean=14893.54, MSE=4058520
##
## Node number 14: 23 observations, complexity param=0.008526053
## mean=15281.96, MSE=9558413
## left son=28 (9 obs) right son=29 (14 obs)
## Primary splits:
## perc.alumni < 32.5 to the left, improve=0.24608690, (0 missing)
## Top25perc < 76.5 to the left, improve=0.21677310, (0 missing)
## P.Undergrad < 140 to the right, improve=0.21246950, (0 missing)
## Books < 632.5 to the right, improve=0.09221313, (0 missing)
## Top10perc < 44.5 to the left, improve=0.06921854, (0 missing)
## Surrogate splits:
## F.Undergrad < 2774 to the right, agree=0.870, adj=0.667, (0 split)
## P.Undergrad < 171 to the right, agree=0.870, adj=0.667, (0 split)
## Accept < 2801.5 to the right, agree=0.826, adj=0.556, (0 split)
## Enroll < 777 to the right, agree=0.826, adj=0.556, (0 split)
## Grad.Rate < 68 to the left, agree=0.826, adj=0.556, (0 split)
##
## Node number 15: 59 observations
## mean=17955.29, MSE=2416673
##
## Node number 18: 12 observations
## mean=6730.25, MSE=6174270
##
## Node number 19: 70 observations, complexity param=0.006901616
## mean=9223.286, MSE=3348902
## left son=38 (39 obs) right son=39 (31 obs)
## Primary splits:
## Accept < 585.5 to the left, improve=0.1868118, (0 missing)
## Apps < 924.5 to the left, improve=0.1622362, (0 missing)
## Enroll < 376.5 to the left, improve=0.1535067, (0 missing)
## Top10perc < 28.5 to the left, improve=0.1399150, (0 missing)
## Top25perc < 57.5 to the left, improve=0.1333957, (0 missing)
## Surrogate splits:
## Apps < 667.5 to the left, agree=0.943, adj=0.871, (0 split)
## Enroll < 234.5 to the left, agree=0.857, adj=0.677, (0 split)
## F.Undergrad < 1124 to the left, agree=0.829, adj=0.613, (0 split)
## Top25perc < 55.5 to the left, agree=0.757, adj=0.452, (0 split)
## Grad.Rate < 66.5 to the left, agree=0.729, adj=0.387, (0 split)
##
## Node number 20: 21 observations
## mean=8496.667, MSE=1463384
##

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## Node number 21: 68 observations
##   mean=10364.51, MSE=2354545
##
## Node number 22: 55 observations
##   mean=11093.62, MSE=1595111
##
## Node number 23: 70 observations,   complexity param=0.008344251
##   mean=12993.49, MSE=3635587
##   left son=46 (23 obs) right son=47 (47 obs)
##   Primary splits:
##       perc.alumni < 21      to the left,   improve=0.1868718, (0 missing)
##       Expend       < 10712  to the left,   improve=0.1594021, (0 missing)
##       Personal     < 740    to the right,  improve=0.1570990, (0 missing)
##       Terminal     < 85.5   to the left,   improve=0.1122604, (0 missing)
##       F.Undergrad < 1607.5  to the right, improve=0.0908322, (0 missing)
##   Surrogate splits:
##       Books        < 608.5  to the right, agree=0.800, adj=0.391, (0 split)
##       Personal     < 1269    to the right, agree=0.786, adj=0.348, (0 split)
##       Grad.Rate    < 66.5    to the left,  agree=0.771, adj=0.304, (0 split)
##       P.Undergrad < 1167    to the right, agree=0.757, adj=0.261, (0 split)
##       F.Undergrad < 2611    to the right, agree=0.743, adj=0.217, (0 split)
##
## Node number 28: 9 observations
##   mean=13369.11, MSE=9777604
##
## Node number 29: 14 observations
##   mean=16511.64, MSE=5553176
##
## Node number 38: 39 observations
##   mean=8518.103, MSE=2547846
##
## Node number 39: 31 observations
##   mean=10110.45, MSE=2944004
##
## Node number 46: 23 observations,   complexity param=0.006405762
##   mean=11815.22, MSE=3929265
##   left son=92 (11 obs) right son=93 (12 obs)
##   Primary splits:
##       PhD          < 82.5    to the left,   improve=0.4497651, (0 missing)
##       Terminal     < 82      to the left,   improve=0.3800468, (0 missing)
##       Room.Board   < 5924    to the left,   improve=0.2331664, (0 missing)
##       P.Undergrad < 225     to the left,   improve=0.2155932, (0 missing)
##       Grad.Rate    < 65.5    to the left,   improve=0.2081110, (0 missing)
##   Surrogate splits:
##       Terminal     < 84.5    to the left,   agree=0.870, adj=0.727, (0 split)
##       Personal     < 1125    to the left,   agree=0.739, adj=0.455, (0 split)
##       Grad.Rate    < 65.5    to the left,   agree=0.739, adj=0.455, (0 split)
##       Apps         < 2106    to the left,   agree=0.696, adj=0.364, (0 split)
##       Top10perc    < 27      to the left,   agree=0.696, adj=0.364, (0 split)
##
## Node number 47: 47 observations,   complexity param=0.008344251
##   mean=13570.09, MSE=2480017
##   left son=94 (38 obs) right son=95 (9 obs)
##   Primary splits:

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##      Expend      < 10323.5 to the left,  improve=0.5004839, (0 missing)
##      Personal    < 860      to the right, improve=0.3234696, (0 missing)
##      perc.alumni < 36.5     to the left,  improve=0.1378371, (0 missing)
##      Top25perc   < 51.5     to the left,  improve=0.1265320, (0 missing)
##      S.F.Ratio   < 13.25    to the right, improve=0.1241689, (0 missing)
##  Surrogate splits:
##      Personal    < 350      to the right, agree=0.851, adj=0.222, (0 split)
##      Top10perc   < 48.5     to the left,  agree=0.830, adj=0.111, (0 split)
##      Top25perc   < 74       to the left,  agree=0.830, adj=0.111, (0 split)
##      Terminal    < 93.5     to the left,  agree=0.830, adj=0.111, (0 split)
##      S.F.Ratio   < 11.35    to the right, agree=0.830, adj=0.111, (0 split)
##
## Node number 92: 11 observations
##   mean=10426.73, MSE=4073306
##
## Node number 93: 12 observations
##   mean=13088, MSE=410005.3
##
## Node number 94: 38 observations
##   mean=13027.89, MSE=1436389
##
## Node number 95: 9 observations
##   mean=15859.33, MSE=404578.9

```

**1.B: Perform random forest on the training data (10pts). Report the variable importance (5pts) and the test error (5pts). Variable importance Test error**

**1.C: Perform boosting on the training data (10pts). Report the variable importance (5pts) and the test error (5pts).**

**QUESTION 2: This problem is based on the data “auto.csv” in Homework 3. Split the dataset into two parts: training data (70%) and test data (30%).**

**2.A: Build a classification tree using the training data, with mpg cat as the response (10pts). Which tree size corresponds to the lowest cross-validation error? Is this the same as the tree size obtained using the 1 SE rule (10pts)?**

**2.B: Perform boosting on the training data and report the variable importance (10pts). Report the test data performance (10pts).**