Math 525: HPC Semester Project

Cuda GPU Accelerated: Support Vector Machine

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Introduction

Support Vector Machine (SVM) is a type of Machine Learning algorithm that is designed around finding the highest margin decision boundary (hyperplane) that classifies the data points. The intuition of using the highest margin hyperplane is that the further the data point is from the decision boundary, the more confident the classification of that data point is.

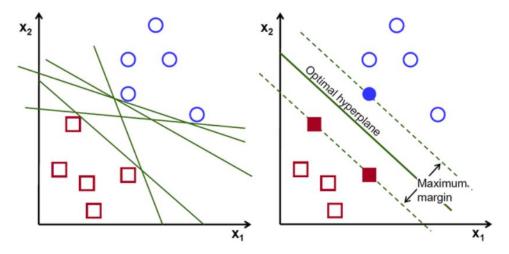


Figure 1: On the left are some possible hyperplanes while on the right is the optimal hyperplane with the maximum margin.

The input to the algorithm is a vector $[x_1, x_2, ...x_n] = x_i$ and a label y_i and the hyperplane is represented as a series of linear weights $[w_1, w_2, ...w_n] = w$. The prediction of the model is $sign(w^Tx)$. Since the purpose of SVM is to minimize the margin, the definition of margin needs to be defined. Margin (γ) is the distance from the decision boundary hyperplane which is $\gamma_i = \frac{y_i(w^Tx_i)}{||w||}$.

The problem now becomes how to minimize γ .

 γ can be minimized by setting up a lagrangian function where the $\alpha_i \geq 0$

$$\mathcal{L}(w, \alpha) = \frac{1}{2}w^T w + \sum_{i=1}^{N} \alpha_i (1 - y_i(w^T x_i))$$

To begin solving this function we must take the partial derivative with respect to w and set the result to 0.

$$\frac{\partial \mathcal{L}(w,\alpha)}{\partial w} = w + \sum_{i=1}^{N} \alpha_i(-y_i x_i) = 0$$

$$w = \sum_{i=1}^{N} \alpha_i y_i x_i$$

Then, substituting back into the original lagrangian, the resulting function is dubbed the "Dual Problem" where result is solely determined by α

$$\mathcal{L}(w,\alpha) = -\frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \alpha_i \alpha_j y_i y_j x_i^T x_j + \sum_{i=1}^{N} \alpha_i$$

If the weights are known, the α s are known and vice versa. The SVM algorithm initializes alphas to random numbers and that steps through the gradient to determine the resulting weights. If the data is linearly separable, SVM will find the highest margin hyperplane.

In order to use SVM in the non-separable cases, there are two modifications that can be employed. The first modification is using "soft" margin rather than hard margin. Soft margin additionally limits the α to be less than or equal to a parameter C. This prevents points that are grossly miss-classified from dominating the decision hyperplane. The second is to use a kernel function. The kernel trick can be used to map the data to a higher dimensional space using less computation. This is due to the fact that the SVM algorithm only relies on the inner product of the vectors which is computationally cheap. For the polynomial case to map 2 features to quadratic space (x_i, x_j) we must calculate $(1, x_i, x_j, x_i^2, x_j^2, x_i x_j)$ but using a kernel is only $(x_i^T x_j + 1)^2$.

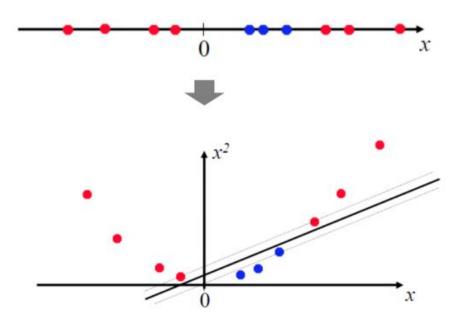


Figure 2: Mapping input vector to higher dimensional space to separate.

The overall computational work for SVM is high since the alphas must be

individually recalculated based on the gradient and each cell of the kernel matrix does not depend on any other cells while being of dimension datapoints x datapoints. This leads to the SVM algorithm to be a prime candidate for the acceleration of a GPU in the CUDAFortran language. The dataset in use for the demonstrations of the algorithm is a set of 1560 images in gray scale values from -1 to 1 for 256 pixels. There is a corresponding label (1 or 5) that the algorithm will classify.

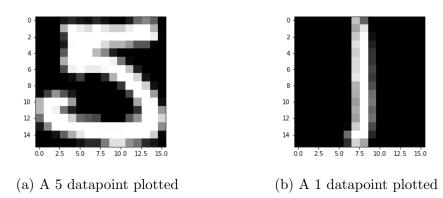


Figure 3: Example data from both classes

Data Distribution

The data distribution component when working in cuda fortran has a distinct problem when working with cuda threads and the host cpu thread. The latentcy of a data transfer from the host to the device and vice versa can be a bottle neck if there are frequent small transfers of data. Ideally, any data that is sent to the gpu is never needed again in the host thread until the processing is done. In the first draft of the gpu code prior to data optimizations, the loss of each training epoch was being calculated on the cpu side. This is a problem for the execution speed of the cuda kernel as there exists a data dependency every epoch that must be fulfilled. By either removing this line or calculating the loss on the kernel will and did increase the speed of this program significantly.

The Memory profiling results from nvprof showed this and the visual profiler was showing a lot of GPU page faults and memory thrashing which can clearly be seen by the green bar in the image.

```
==150107== Unified Memory profiling result:
```

Device "GeForce RTX 2070 SUPER (0)"

Count Avg Size Min Size Max Size Total Size Total Time Name
728004 27.323KB 4.0000KB 0.9961MB 18.97026GB 2.537655s Host To Device
131570 151.41KB 4.0000KB 0.9961MB 18.99832GB 1.650468s Device To Host
34283 - - - 6.111599s Gpu page fault

groups

164 4.0000KB 4.0000KB 4.0000KB 656.0000KB - Memory thrashes

Total CPU Page faults: 65627

------ 101

Total CPU thrashes: 164

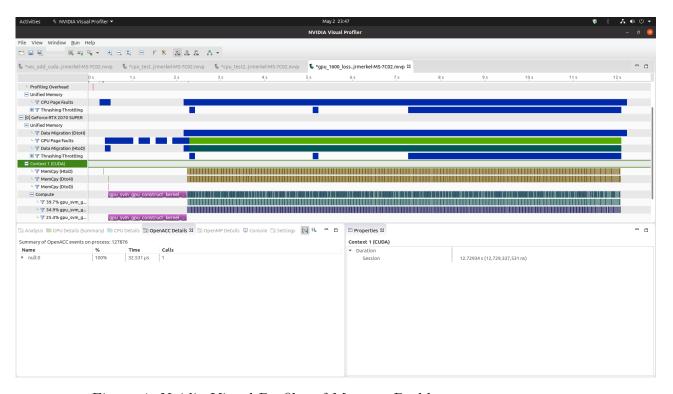


Figure 4: Nvidia Visual Profiler of Memory Problems

As we can see from the output, the amount of time that the program was spending transferring data was really high in comparison to the total execution time which was 12.729. Originally, I was very confused by such a high amount of transferred memory at almost 19GB. The dataset itself should only be a few MB so there had to be something. Eventually I noticed the loss calculation line was the only one that was not in a kernel. By removing that line the profiling results look like this instead.

⁼⁼¹⁵⁰²⁰²⁼⁼ Unified Memory profiling result:

Device "GeForce RTX 2070 SUPER (0)"

```
Count Avg Size Min Size Max Size Total Size Total Time Name

74 141.84KB 4.0000KB 0.9922MB 10.25000MB 934.7800us Host To Device

138 145.16KB 4.0000KB 0.9961MB 19.56250MB 1.812210ms Device To Host

114 - - - - 9.456863ms Gpu page fault

groups

Total CPU Page faults: 123
```

Since the data is not being sent back to the CPU every epoch, that allows us to avoid the large latentcy associated with the gpu memory transfer. This means sending all of the data and keeping it there for the full training is really the only way to distribute the data for performance and most datasets will not exceed the amount memory on the GPU. What this looks like in the actual code is that we have managed arrays that are associated with the module that the kernel subroutines will modify.

```
module gpu_svm
    use cudafor
    use cublas
    real, save, managed, dimension(:,:), allocatable ::
        kernel_matrix,orig_dataset
    integer,save, managed:: rows, features, max_iter,
        num_cudathreads, type, num_ex,num_blocks
    real,save, managed :: learning_rate, C
    real, save, dimension(:), managed, allocatable :: labels
```

Then the cuda compiler will optimize when the memory is used so that we

do not have to worry about the cuda memory functions.

Serial Optimization

The kernel construction function was originally implemented as a small subroutine that does depend on the loop index but is not many lines of code.

This means that the subroutine call can use inlining to find more optimization
opportunites. This is done by adding a compiler argument to the nvfortran
compiler of -Minline=gpu_kernel which will allow the compiler to optimize
out this call.

enddo

end subroutine

In the performance section, we can see that the gpu_kernel function does not show up which means that this function is correctly being optimized out of its own call and is being inlined. Another aspect of the serial optimization was to pre-calculate the number of executions that each gpu thread would have to use so that each time the kernel is called, the gpu thread does not have to determine that value which can take some cycles off for each kernel call. Since there are 4 kernel calls per epoch and 1000 epochs this adds up to a sizeable time change. There is still a possibility to create stride 1 that would require a large refactor by storing the matrices in a transposed matrix.

Load Balancing

Load balancing is another aspect of using cuda fortran that should be considered. Each gpu process should be doing the same amount of work to ensure that the exectution is as fast as possible. In order to do this, any time a GPU kernel is used, the number of executions is the same and is either implicitly done by the cuda compiler if you use !cuf directive or explicitly in kernel subroutines. For the explicit kernel subroutines, I used num_ex which was pre-calculated to increase the serial speed and is calculated by the number of

rows divided by the ceiling of the number of cuda threads. Then to determine which iteration the thread should be doing, we use (i-1)*num_cudathreads)+ threadidx%x + (blockidx%x - 1) *num_blocks to spread out the load evenly and still completing every iteration. Since cuda takes care of most of the load balancing this was not a significant amount of the project yet from the Nvidia Visual Profiler we can still see that all of the threads we are allocating are doing the same work.

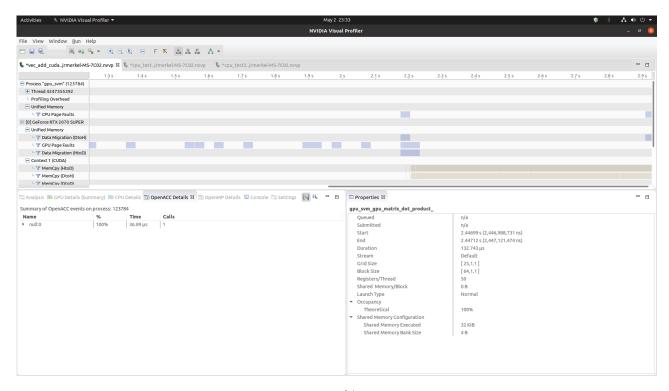


Figure 5: Nvidia Visual Profiler of 100% usage of threads

From this figure we can see that the 25 blocks of 64 threads are being executed with 100% occupancy of the threads.

Performance/Scalability

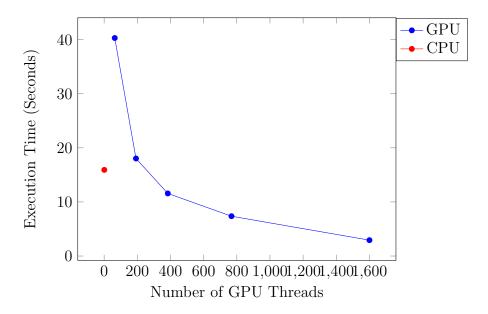


Figure 6: Execution Time by GPU Threads

GPU Threads	Execution time
64	40.31
192	18.026
384	11.569
768	7.36
1600	2.93

Figure 7: Table of GPU Execution Time

In terms of the GPU threads, the performance graph looks exactly how you would expect a highly parallel process to look. As we double the amount of GPU processes, the Execution time nearly halves. This is because nearly every aspect of the computation for the GPU version of the SVM algorithm is all in the various kernels. Of course as we increase the number of processes significantly, there still exists some time that gets wasted by overhead. The more threads you allocate, the more amount of overhead is added, along with the serial portions that cannot be optimized.

One thing that was done to improve the scalability is that all of the code for each epoch is done in the gpu kernel and the number of calls to the gpu kernel is minimized. Originally this snippet of code looked like the following.

```
!$cuf kernel do <<<num_cudathreads/num_blocks, 64>>>
do j = 1, rows
              gradient(j) = 1.d0 - y_x_alpha(j)
              alpha_arr(j) = alpha_arr(j) + learning_rate *
                  gradient(j)
enddo
istat = cudaDeviceSynchronize()
!For soft margin limit alpha by C
!$cuf kernel do <<<num_cudathreads/num_blocks, 64>>>
          do j = 1, rows
                  if(alpha_arr(j) > C) then
                      alpha_arr(j) = C
                  else if (alpha_arr(j) < 0) then
                      alpha_arr(j) = 0
                  endif
               enddo
```

One of the kernel calls can be removed by instead replacing it with this.

This removes 1 overhead call to device synchronize and the setup of the kernel in general which will improve performance over the 1000 epochs that the program is ran. From the profiling report by nvprof, the time spent in the GPU activities and specifically in the subroutines that I created which are the gpu_matrix_dot_product, gpu_vec_to_matrix, and gpu_construct_kernel_matrix.

```
==150107== Profiling application: ./gpu_svm
==150107== Profiling result:
          Type Time(\%)
                            Time
                                    Calls
                                                        Min
                                                                 Max Name
                                               Avg
GPU activities: 41.41\% 2.89805s
                                     1000 2.8981ms 2.1803ms 6.9813ms
     gpu_svm_gpu_matrix_dot_product_
                 34.55\% 2.41756s
                                     1001 2.4151ms 1.1209ms 5.8735ms
                     gpu_svm_gpu_vec_to_matrix_
                 23.85\% 1.66932s
                                        1 1.66932s 1.66932s 1.66932s
                     gpu_svm_gpu_construct_kernel_matrix_
                 0.09\% 6.0573ms
                                     3002 2.0170us 1.1200us 5.7610us [CUDA memcpy DtoH]
                 0.06\% 4.0054ms
                                     5014
                                             798ns
                                                      736ns 2.6560us [CUDA memcpy HtoD]
                 0.04\% 2.4738ms
                                     1000 2.4730us 2.2400us 3.5520us
                      gpu_svm_fit_svm_191_gpu
                 0.01\% 799.29us
                                        2 399.64us 341.48us 457.81us [CUDA memcpy DtoD]
     API calls: 74.04\% 5.58224s
                                     5003 1.1158ms 1.6500us 220.01ms cudaFree
                 22.50\% 1.69667s
                                     3002 565.18us 1.1600us 1.66932s cudaDeviceSynchronize
                 0.70\% 52.625ms
                                     5004 10.516us 3.2100us 2.4818ms cudaMemcpy
                 0.59\% 44.629ms
                                     1000 44.628us 27.199us 78.148us cudaMemcpyAsync
                 0.55\% 41.327ms
                                     1000 41.327us 5.4100us 383.19us cudaStreamSynchronize
                 0.54\% 41.087ms
                                     2002 20.522us 10.890us 55.850us cudaMemcpyFromSymbol
                 0.38\% 28.821ms
                                     5003 5.7600us 2.1200us 181.54us cudaMalloc
                 0.35\% 26.260ms
                                     3002 8.7470us 4.3400us 233.09us cudaLaunchKernel
                  0.27\% 20.268ms
                                        1 20.268ms 20.268ms 20.268ms cuMemAllocManaged
                 0.02\% 1.7507ms
                                     2000
                                             875ns
                                                       280ns 2.8900us
                      {\tt cudaDeviceGetAttribute}
                 0.02\% 1.3691ms
                                     1001 1.3670us
                                                      570ns 2.7100us cudaGetDevice
                 0.01\% 797.89us
                                        1 797.89us 797.89us 797.89us cuMemHostAlloc
                                        3 261.56us 175.09us 390.27us cuDeviceTotalMem
                 0.01\% 784.67us
                 0.00\% 241.72us
                                      103 2.3460us
                                                      270ns 99.348us cuDeviceGetAttribute
                 0.00\% 183.38us
                                       12 15.281us 6.3500us 68.859us cudaMemcpyToSymbol
                 0.00\% 35.429us
                                       1 35.429us 35.429us 35.429us cuDeviceGetName
                 0.00\% 20.170us
                                        1 20.170us 20.170us 20.170us cudaStreamCreate
                 0.00\% 5.8800us
                                        1 5.8800us 5.8800us 5.8800us cudaSetDevice
                 0.00\% 5.2600us
                                        1 5.2600us 5.2600us 5.2600us cuDeviceGetPCIBusId
```

```
0.00\% 3.6700us
                                         1 3.6700us 3.6700us 3.6700us cudaDeviceSetLimit
                 0.00\% 2.5400us
                                                        370ns 1.1400us cuDeviceGetCount
                                               635ns
                 0.00\% 2.0700us
                                           2.0700us 2.0700us 2.0700us cudaGetFuncBySymbol
                 0.00\% 1.6900us
                                           1.6900us 1.6900us 1.6900us cudaGetDeviceCount
                 0.00\% 1.5100us
                                              5100us 1.5100us 1.5100us cuInit
                 0.00\% 1.3700us
                                               456ns
                                                        280ns
                                                                 710ns cuCtxSetCurrent
                 0.00\% 1.2700us
                                         3
                                               423ns
                                                        310ns
                                                                 600ns cuDeviceGet
                 0.00\%
                            750ns
                                         1
                                              750ns
                                                        750ns
                                                                 750ns cuFuncGetModule
                 0.00\%
                            650ns
                                         1
                                               650ns
                                                        650ns
                                                                 650ns cudaGetSymbolAddress
                 0.00\%
                            630ns
                                         2
                                               315ns
                                                        200ns
                                                                 430ns cudaRuntimeGetVersion
                 0.00\%
                            610ns
                                         1
                                               610ns
                                                        610ns
                                                                 610ns cuCtxGetDevice
                 0.00\%
                            570ns
                                         1
                                                                 570ns cuCtxGetCurrent
                                               570ns
                                                        570ns
                 0.00\%
                                                        470ns
                            470ns
                                         1
                                               470ns
                                                                 470ns
                      cuDeviceComputeCapability
                 0.00\%
                            450ns
                                               450ns
                                                        450ns
                                                                 450ns cuDeviceGetUuid
                                         1
                 0.00\%
                            350ns
                                         1
                                               350ns
                                                        350ns
                                                                 350ns cuDriverGetVersion
                 0.00\%
                            220ns
                                               220ns
                                                        220ns
                                                                 220ns cudaDriverGetVersion
OpenACC (excl): 100.00\% 32.740us
                                           32.740us 32.740us 32.740us acc_device_init
```

Since the GPU is spending most of its time in the highly parallel subroutines that I created, this project is highly scalable and in fact would see
greater performance gains if the dataset was bigger and used more features.

The amount of threads is almost overkill since from this snippet of the nvidia
visual profiler we can see that the average call to the subroutines I wrote are
less than a millisecond each and the cuf directive kernel is blindingly fast
at 2.622 microseconds. If the dataset was instead much larger than the
around 1600 samples in the training data, the setup for those kernels would
be roughly the same but the durations would be much longer. This longer
duration would mean more time is spent actually computing instead of going

from kernel to kernel.

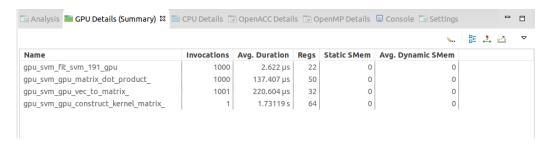


Figure 8: Average Kernel Execution Time

The last thing I'll touch on in this section is that the SVM algorithm was very efficient at classifying the datapoints after modifying the learning rate so that our gradient descent did not overfit the training data. This resulted in a prediction of 98.58% accuracy in classifying between the 5 and 1 image inputs.

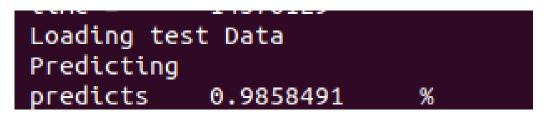


Figure 9: Code Output

Conclusion

Overall, the project was successful at implementing the SVM algorithm using cuda fortran and actually was able to classify the dataset with 98.58% accuracy. There are still more optimizations that could be made in the code that I did not have time to attempt. I think the efficacy of using a GPU as a hardware accelerator were clearly shown since the cpu speed was improved by a factor of 5.5x speed. This would likely be exacerbated by a larger dataset with more features. If I had more time I would refactor the code to use the transpose of the kernel matrix as well as implementing more kernel types other than just the linear kernel and polynomial kernel. A multivariate SVM would be one additional thing to increase the use cases of the algorithm in general.

References

- The dataset was taken from the COMS 573 HW on SVM and lecture notes from that class were also used.
- The implementation of SVM used help from http://www.adeveloperdiary.com/datascience/machine-learning/support-vector-machines-for-beginners-kernelsvm/
- Images from https://towardsdatascience.com/support-vector-machine-introduction-to-machine-learning-algorithms-934a444fca47

Code

CPU SVM

```
module svm
   contains
   subroutine kernel(x_i, x_j, type, transform)
       integer, intent(in):: type
       real, dimension(:) , intent(in):: x_i, x_j
       real, intent(out) :: transform
       real :: temp
       select case (type)
          !linear kernel x_i^T * x_j
          case(0)
              transform = dot_product(x_i,x_j)
          ! polynomial kernel (x_i^T * x_j)^2
          case(1)
              temp = (dot_product(x_i,x_j) + 1)
              transform = temp * temp * temp
           ! rbf kernel
          case(2)
          case default
              ! print*, "ERROR: NOT SUPPORTED KERNEL TYPE"
              ! call exit(0)
       end select
       return
   end subroutine
   subroutine construct_kernel_matrix_prediction(datasetA, datasetB, result, rows,
        features, type, result_dim)
       integer, intent(in) :: rows, features, type, result_dim
       real, dimension(:,:), intent(in) :: datasetA, datasetB
```

```
real, dimension(:,:), intent(out) :: result
   ! Perhaps there is a efficiency here either in dataset access or loop iters
   do i=1, result_dim
       do j=1, rows
          ! call kernel(dataset(i,1:features), dataset(j,1:features), type,
               kernel_matrix(i,j))
          call kernel(datasetA(j, :), datasetB(i, :), type, result(i,j))
       enddo
   enddo
end subroutine
subroutine cpu_construct_kernel_matrix(dataset, kernel_matrix, rows, features, type)
   integer, intent(in) :: rows, features, type
   real, dimension(:,:), intent(in) :: dataset
   real, dimension(:,:), intent(out) :: kernel_matrix
   ! call syncthreads()
   ! Perhaps there is a efficiency here either in dataset access or loop iters
   do i=1, rows
       do j=1, rows
          ! call kernel(dataset(i,1:features), dataset(j,1:features), type,
               kernel_matrix(i,j))
          call kernel(dataset(i,:), dataset(j,:), type, kernel_matrix(i,j))
       enddo
   enddo
end subroutine
subroutine vec_to_matrix(matrix, vector, n)
   integer, intent(in) :: n
   real, dimension (:), intent(in) :: vector
   real, dimension (:,:), intent(out) :: matrix
   integer :: i
   do i = 1, n
       do j = 1, n
```

```
matrix(i,j) = vector(i) * vector(j)
       enddo
   enddo
end subroutine
subroutine matrix_dot_product(matrixA, VecB, n, outVector)
   real, dimension(:,:), intent(in) :: matrixA
   real, dimension(:), intent(in) :: VecB
   integer, intent(in) :: n
   real, dimension(:), intent(out) :: outVector
   real :: acc
   integer :: i
   do i = 1, n
       acc = 0.d0
       do j = 1,n
          acc = acc + (matrixA(i,j) * VecB(j))
       enddo
       outVector(i) = acc
   enddo
end subroutine
subroutine fit_svm(kernel_matrix, labels, rows, features, max_iter, learning_rate,
    alpha_arr, loss, bias)
   !Inputs
   integer, intent(in) :: rows, features, max_iter
   real, intent(in) :: learning_rate
   real, dimension(:), intent(in) :: labels
   real, dimension(:,:), intent(in) :: kernel_matrix
   real, dimension(:,:), allocatable :: labels_matrix
   integer :: i, j
   real :: C
   real, dimension(:,:), allocatable :: y, alpha_matrix
```

```
real, dimension(:), allocatable :: bias_arr, y_x_alpha, gradient
! Inout since alphas change
real, dimension(:), intent(out) :: alpha_arr
real, intent(inout) :: bias
! Outputs
real, dimension(:), intent(out) :: loss
print*, "Init alphas"
C = 1.d0
! Randomize initial alphas
call random_number(alpha_arr(1:rows))
print*, "Allocating"
! Init bias, ones, and gradient
allocate(gradient(rows))
bias = 0.d0
allocate(bias_arr(rows))
bias_arr(1:rows) = 0.d0
allocate(y(rows, rows))
allocate(labels_matrix(rows,rows))
allocate(alpha_matrix(rows,rows))
!Temp vars
allocate(y_x_alpha(rows))
! calculate matrix form of labels
call vec_to_matrix(labels_matrix, labels, rows)
y(1:rows, 1:rows) = labels_matrix(1:rows, 1:rows) * kernel_matrix(1:rows, 1:rows)
! Training
do i = 1, max_iter
   print*, "Epoch = ", i
   ! Calculate gradient and update alpha
   call matrix_dot_product(y, alpha_arr, rows, y_x_alpha))
   gradient = 1.d0 - y_x_alpha
   alpha_arr= alpha_arr+ learning_rate * gradient
   !For soft margin limit alpha by C
```

```
do j = 1, rows
          if(alpha_arr(j) > C) then
             alpha_arr(j) = C
          else if (alpha_arr(j) < 0) then</pre>
             alpha_arr(j) = 0
          endif
      enddo
       ! Loss = sum alpha - 1/2 sum_i sum_j alphasij yij K Not doing to keep
           consistent with GPU
      !call vec_to_matrix(alpha_matrix, alpha_arr, rows)
      !loss(i) = sum(alpha_arr) - 0.5 * sum(alpha_matrix * y)
   enddo
   !Calc bias = avg if alpha within range, yi - aiyiK
   y_x_alpha(1:rows) = alpha_arr(1:rows) * labels(1:rows)
   ! call matrix_dot_product(kernel_matrix, alpha_x_y, rows, alpha_x_y_dot_kernel)
   do j = 1, rows
      if(alpha_arr(j) > 0 .and. alpha_arr(j) < C) then
          bias_arr(j) = labels(j) - dot_product(y_x_alpha, kernel_matrix(:, j))
      endif
   enddo
   bias = sum(bias_arr) / rows
end subroutine
!yhat = sign(sum alphai yi kernel(xi)T kernel(zi) + b)
!Figure out how to make modules save arrays
subroutine predict(orig_dataset, orig_labels, orig_rows, features, alpha_arr, bias,
    samples, samples_dim, type, predictions)
   real, dimension(:,:), intent(in) :: orig_dataset, samples
   real, dimension(:), intent(in) :: orig_labels, alpha_arr
   real, intent(in)
                                  :: bias
```

```
integer, intent(in)
                              :: orig_rows, features, samples_dim, type
   integer, dimension (:), intent(out) :: predictions
   real, dimension(:), allocatable
                                   :: y_x_alpha
   real, dimension(:,:), allocatable
                                      :: result
   allocate(y_x_alpha(orig_rows))
   allocate(result(samples_dim, orig_rows))
   y_x_alpha(1:orig_rows) = alpha_arr(1:orig_rows) * orig_labels(1:orig_rows)
   call construct_kernel_matrix_prediction(orig_dataset, samples, result, orig_rows,
       features, type, samples_dim)
   do i = 1, samples_dim
      predictions(i) = sign_func(dot_product(y_x_alpha, result(i,:)))
   enddo
end subroutine
integer function sign_func(input) result (out)
   real :: input
   if(input > 0) then
      out = 1
   else
      out = -1
   endif
end function
real function score(labels, prediction, n) result (out)
   integer, dimension(:) :: prediction
   real, dimension(:) :: labels
   integer
                  :: i, num_correct
   num_correct = 0
   do i = 1, n
```

```
if(int(labels(i)) == prediction(i)) then
              num_correct = num_correct + 1
          endif
       enddo
       out = dble(num_correct) / dble(n)
   end function
end module svm
use cudafor
use cublas
use svm
use data_load
integer, parameter :: kernel_type = 1, n = 400, max_iter = 1000
real, parameter :: learning_rate = 0.0000000002, C = 5.0
integer :: t1,t2,t3,t4
real, dimension(:,:), allocatable :: dataset, raw_dataset, test_dataset, raw_test_dataset
real, dimension(:,:), allocatable :: kernel_matrix
real, dimension(:), allocatable :: labels, alpha_arr, loss, test_labels
integer, dimension(:), allocatable :: predictions
integer :: rows, features, count_max, count_rate, test_rows
real :: bias
!Setup the cuda devices
istat = cudaSetDevice(0)
call system_clock(count_max = count_max, count_rate=count_rate)
rows =
    {\tt determine\_row\_num("/home/jrmerkel/Documents/Fortran/SVM\_CudaFortran/SVM\_Example/data/train.txt")}
features =
    {\tt determine\_feature\_size("/home/jrmerkel/Documents/Fortran/SVM\_CudaFortran/SVM\_Example/data/train.txt")}
device_rows = rows
device_features = features
! allocate the dataset and kernel matrices on host and devices
allocate(raw_dataset(rows,features))
```

```
print*, "Loading Dataset"
call
             {\tt load\_data("/home/jrmerkel/Documents/Fortran/SVM\_CudaFortran/SVM\_Example/data/train.txt", and the content of the content o
             raw_dataset, rows, features)
! allocate arr and matrices
allocate(labels(rows))
allocate(kernel_matrix(rows,rows))
allocate(alpha_arr(rows))
allocate(loss(max_iter))
print*, "Parsing labels"
call split_labels(raw_dataset, dataset, labels, rows, features)
call normalize_labels(labels, rows)
print*, "Constructing Kernel"
call cpu_construct_kernel_matrix(dataset, kernel_matrix, rows, features, kernel_type)
print*, "fit Svm"
call fit_svm(kernel_matrix, labels, rows, features, max_iter, learning_rate, alpha_arr,
             loss, bias)
! load test dataset
test_rows =
             {\tt determine\_row\_num("/home/jrmerkel/Documents/Fortran/SVM\_CudaFortran/SVM\_Example/data/test.txt")}
! allocate the dataset
allocate(raw_test_dataset(test_rows,features))
allocate(test_dataset(test_rows,features))
allocate(predictions(test_rows))
print*, "Loading test Data"
call
             load_data("/home/jrmerkel/Documents/Fortran/SVM_CudaFortran/SVM_Example/data/test.txt",
             raw_test_dataset, test_rows, features)
```

Data Load Helper

```
module data_load
  integer :: MAX_FEATURE_SIZE = 260
  integer :: MAX_LINE_CHARACTER_LEN = 4500
  integer :: FILE_UNIFIER = 20
  real :: DUMMY_VAL = -99999.d22
  contains
  ! NOTE this subtroutine reads in the data is (row,col)
  ! Consider Transposing for efficiency
  subroutine load_data(filepath, data_array, row_num, feature_size)
      character(len=*), intent(in) :: filepath
      integer, intent(in) :: row_num, feature_size
      real, dimension(:,:), intent(out) :: data_array
      ! Read in the data
      open(FILE_UNIFIER, FILE = filepath)
      do i = 1, row_num
```

```
read(FILE_UNIFIER, *) data_array(i, 1:feature_size)
       enddo
       ! Transpose matrix Fortran is Col
       !transpose(data_array)
       close(FILE_UNIFIER)
   end subroutine
! Changes the labels to be 1 or -1 so that SVM can be run
   subroutine normalize_labels(label_array, n)
       real, dimension(:), intent(inout) :: label_array
       integer, intent(in) :: n
       integer :: i
       do i = 1, n
          if(label_array(i) < 1.00001 .and. label_array(i) > 0.9999) then
              label_array(i) = 1.d0
          else
              label_array(i) = -1.d0
          endif
       enddo
   end subroutine
!splits the labels from the dataset because that needs to be separate to train/test the
    data
   subroutine split_labels(data_array, feature_array, label_array, row_num, feature_size)
       real, dimension(:,:), intent(in) :: data_array
       integer, intent(in) :: row_num, feature_size
       real, dimension(:,:), intent(out) :: feature_array
       real, dimension(:), intent(out) :: label_array
       label_array = data_array(1:row_num, 1)
       feature_array(1:row_num, 1:feature_size) = data_array(1:row_num, 1:feature_size)
       feature_array(1:row_num,1) = 1.d0
   end subroutine
```

```
!Determines the number of datapoints
   integer function determine_row_num(filepath) result (row)
       integer :: row, i, ios
       character(len=*) :: filepath
       character(len=200) :: huh
       real, dimension(2000) :: data_array
       ! Open file
       open(FILE_UNIFIER, FILE = filepath)
       row = 0
       do i=1, 2000
          read(FILE_UNIFIER, '(ES10.2)', iostat=ios), data_array(i)
          if (ios /= 0) then
              close(FILE UNIFIER)
              return
          endif
          row = row + 1
       enddo
       row = -1
       return
   end function
! Determines how many features are in use
   integer function determine_feature_size(filepath) result (feature)
       integer :: feature, i, ios
       character(len=*) :: filepath
       character(len=MAX_LINE_CHARACTER_LEN) :: Line
       real, dimension(MAX_FEATURE_SIZE) :: data_array
       ! Open file
       open(FILE_UNIFIER, FILE = filepath)
       feature = 0
       !init dummy vals
       data_array(1:MAX_FEATURE_SIZE) = DUMMY_VAL
       !Read line and then into array
```

```
read(FILE_UNIFIER, '(A)'), Line
read(Line, *, iostat=ios) data_array

do i = 1, MAX_FEATURE_SIZE
    if(data_array(i)/= DUMMY_VAL) then
        feature = feature + 1
    else
        close(FILE_UNIFIER)
        return
    endif
enddo
    close(FILE_UNIFIER)
    return
end function
```

GPU SVM

```
use cudafor
   use cublas
   real, save, managed, dimension(:,:), allocatable :: kernel_matrix,orig_dataset
   ! real, save, dimension(:,:), managed, allocatable :: test
   integer,save, managed:: rows, features, max_iter, num_cudathreads, type,
        num_ex,num_blocks
   real,save, managed :: learning_rate, C
   real, save, dimension(:), managed, allocatable :: labels
   contains
!impelments the row by row kernel calculations in gpu
   attributes(device) subroutine gpu_kernel(x_i, x_j, transform)
        ! integer, device, intent(in):: type
        real, device, dimension(:), intent(in):: x_i, x_j
```

```
real, device, intent(out) :: transform
       real, device:: temp
       select case (type)
          !linear kernel x_i^T * x_j
          case(0)
              transform = dot_product(x_i,x_j)
          ! polynomial kernel (x_i^T * x_j)^2
          case(1)
              temp = (dot_product(x_i,x_j) + 1)
              transform = temp * temp * temp
          case default
              ! print*, "ERROR: NOT SUPPORTED KERNEL TYPE"
              ! call exit(0)
       end select
       return
   end subroutine
!impelments the row by row kernel calculations in cpu
   subroutine kernel(x_i, x_j, type, transform)
       integer, intent(in):: type
       real, dimension(:) , intent(in):: x_i, x_j
       real, intent(out) :: transform
       real :: temp
       select case (type)
          !linear kernel x_i^T * x_j
          case(0)
              transform = dot_product(x_i,x_j)
          ! polynomial kernel (x_i^T * x_j)^2
          case(1)
              temp = (dot_product(x_i,x_j) + 1)
              transform = temp * temp * temp
          ! rbf kernel
          case(2)
          case default
```

```
! print*, "ERROR: NOT SUPPORTED KERNEL TYPE"
               ! call exit(0)
       end select
       return
   end subroutine
   !Constructs the kernel matrix for the kernel trick of svm
   attributes(global) subroutine gpu_construct_kernel_matrix()
       real, dimension(rows) :: rowA, rowB
   do i=1, num_ex
       do j=1, rows
           \label{eq:condition} \mbox{rowA = orig_dataset(((i-1)*num_cudathreads)+ threadidx%x + (blockidx%x - 1))} \\
                *num_blocks ,:)
           rowB = orig_dataset(j,:)
           call gpu_kernel(rowA, rowB, kernel_matrix((i-1)*num_cudathreads + threadidx%x+
                (blockidx%x - 1) *num_blocks,j))
       enddo
   enddo
   end subroutine
!Utility function to test kernel
   attributes(host) integer function write_kernel() result (out)
       open(23,FILE = "./orig_data.txt")
     write(23, *), orig_dataset(1,:)
     close(23)
     out = 1
     return
   end function
```

```
subroutine construct_kernel_matrix_prediction(datasetA, datasetB, result, result_dim)
       integer, intent(in) :: result_dim
       real, dimension(:,:), intent(in) :: datasetA, datasetB
       real, dimension(:,:), intent(out) :: result
       do i=1, result_dim
          do j=1, rows
              ! call kernel(dataset(i,1:features), dataset(j,1:features), type,
                   kernel_matrix(i,j))
              call kernel(datasetA(j, :), datasetB(i, :), type, result(i,j))
          {\tt enddo}
       enddo
   end subroutine
!Implement Np.outer for vector
   attributes(global) subroutine gpu_vec_to_matrix(matrix, vector)
       real, device,dimension (:), intent(in) :: vector
       real, device,dimension (:,:), intent(out) :: matrix
       integer :: i,j
       !num_ex = ceiling(real(rows) / real(num_cudathreads))
   do j = 1, num_ex
       ! print*, " j = ", (j-1)*(num\_cudathreads) + ((blockidx%x - 1) *num\_blocks) +
            threadidx%x
            do i = 1, rows
                matrix(i, (j-1)*(num\_cudathreads) + ((blockidx%x - 1) *num\_blocks) +
                     threadidx\%x) = vector(i) * vector((j-1)*(num_cudathreads) +
                     ((blockidx%x - 1) *num_blocks) + threadidx%x)
     ! matrix(i,((j-1)*(num_cudathreads + (blockidx%x - 1) *num_blocks) + threadidx%x)) =
          vector(i) * vector((j-1)*(num_cudathreads + (blockidx%x - 1) *num_blocks) +
          threadidx%x)
            enddo
         enddo
   end subroutine
```

!Dot product of a matrix and a vector

```
attributes(global) subroutine gpu_matrix_dot_product(matrixA, VecB, outVector)
    real, device, dimension(:,:), intent(in) :: matrixA
    real, device, dimension(:), intent(in) :: VecB
    real, device, dimension(:), intent(out) :: outVector
    real :: acc
    integer :: i
! print*, "blockidx", blockidx%x, "threadidx", threadidx%x
    do i = 1, num_ex
       acc = 0.d0
       do j = 1, rows
           \verb| acc = acc + (matrixA((i-1)*num_cudathreads + threadidx%x+ (blockidx%x - 1)| \\
                *num_blocks,j) * VecB(j))
       outVector((i-1)*num_cudathreads + threadidx%x+ (blockidx%x - 1) *num_blocks) =
            acc
    enddo
end subroutine
attributes(host) subroutine fit_svm(alpha_arr, loss, bias)
    !Inputs
    !Local Vars
    real, dimension(:,:), managed, allocatable :: labels_matrix
    integer :: i, j
    real, dimension(:,:), managed, allocatable :: y, alpha_matrix
    real, dimension(:), managed, allocatable :: bias_arr, y_x_alpha, gradient
    ! Inout since alphas change
    real, dimension(:), managed, intent(out) :: alpha_arr
    real, intent(inout) :: bias
    ! Outputs
    real, dimension(:), intent(out) :: loss
```

```
print*, "Init alphas"
    ! Randomize initial alphas
    call random_number(alpha_arr(1:rows))
    ! Init bias, ones, and gradient
    allocate(gradient(rows))
    bias = 0.d0
    allocate(bias_arr(rows))
    bias_arr(1:rows) = 0.d0
    allocate(y(rows, rows))
    allocate(labels_matrix(rows,rows))
    allocate(alpha_matrix(rows,rows))
    !Temp vars
    allocate(y_x_alpha(rows))
    ! calculate matrix form of labels
    call gpu_vec_to_matrix<<<num_cudathreads/num_blocks,num_blocks>>>(labels_matrix,
         labels)
istat = cudaDeviceSynchronize()
    y(1:rows, 1:rows) = labels_matrix(1:rows, 1:rows) * kernel_matrix(1:rows, 1:rows)
    ! Training
    do i = 1, max_iter
        print*, "Epoch = ", i
        ! Calculate gradient and update alpha
        istat = cudaDevuceSynchronize
   call gpu_matrix_dot_product<<<num_cudathreads/num_blocks, num_blocks>>>(y,
        alpha_arr, y_x_alpha)
        istat = cudaDeviceSynchronize()
       !$cuf kernel do <<<num_cudathreads/num_blocks, 64>>>
```

```
do j = 1, rows
              gradient(j) = 1.d0 - y_x_alpha(j)
              alpha_arr(j) = alpha_arr(j) + learning_rate * gradient(j)
              if(alpha_arr(j) > C) then
                  alpha_arr(j) = C
              else if (alpha_arr(j) < 0) then</pre>
                  alpha_arr(j) = 0
              endif
          enddo
          istat = cudaDeviceSynchronize()
          ! Loss = sum alpha - 1/2 sum_i sum_j alphasij yij K Loss is not necessary to
               calculate
           !call gpu_vec_to_matrix<<<num_cudathreads/num_blocks,
               num_blocks>>>(alpha_matrix, alpha_arr)
      ! loss(i) = sum(alpha_arr) - 0.5 * sum(alpha_matrix * y)
       enddo
       !Calc bias = avg if alpha within range, yi - aiyiK
       y_x_alpha(1:rows) = alpha_arr(1:rows) * labels(1:rows)
       print*, "bias calc"
       do j = 1, rows
          if(alpha_arr(j) > 0 .and. alpha_arr(j) < C) then
              bias_arr(j) = labels(j) - dot_product(y_x_alpha, kernel_matrix(:, j))
          endif
       enddo
       bias = 1.d0
   end subroutine
   !yhat = sign(sum alphai yi kernel(xi)T kernel(zi) + b)
!Predict for the incoming dataset
   subroutine predict(original_dataset, orig_labels, orig_rows, alpha_arr, bias, samples,
        samples_dim, predictions)
```

```
real, dimension(:,:), intent(in) :: original_dataset, samples
     real, dimension(:), intent(in) :: orig_labels, alpha_arr
     real, intent(in)
     integer, intent(in)
                               :: orig_rows, samples_dim
         integer, dimension (:), intent(out) :: predictions
     real, dimension(:), allocatable
                                        :: y_x_alpha
     real, dimension(:,:), allocatable
                                       :: result
     allocate(y_x_alpha(orig_rows))
     allocate(result(samples_dim, orig_rows))
!Calculate alpha * Labels
     y_x_alpha(1:orig_rows) = alpha_arr(1:orig_rows) * orig_labels(1:orig_rows)
     call construct_kernel_matrix_prediction(original_dataset, samples, result,
         samples_dim)
     do i = 1, samples_dim
        predictions(i) = sign_func(dot_product(y_x_alpha, result(i,:)))
     enddo
  end subroutine
!Sign function is used to determine which label is the prediction.
   integer function sign_func(input) result (out)
     real :: input
     if(input > 0) then
        out = 1
     else
        out = -1
     endif
   end function
```

```
!Score the predictions
   real function score(labels, prediction, n) result (out)
       integer, dimension(:) :: prediction
       real, dimension(:) :: labels
       integer
                         :: i, num_correct, n
       num_correct = 0
       do i = 1, n
          if(int(labels(i)) == prediction(i)) then
              num_correct = num_correct + 1
          endif
       {\tt enddo}
       out = dble(num_correct) / dble(n)
   end function
!Allocate datasets
   integer function allc() result (out)
       allocate(kernel_matrix(rows,rows))
  allocate(labels(rows))
  allocate(orig_dataset(rows, features))
   end function
!Utility function to test
   attributes(host) integer function write_dataset(in_data, in_labels) result (out)
  real, dimension(:,:) :: in_data
  real,dimension (:) :: in_labels
       labels = in_labels
  orig_dataset = in_data
   end function
!Sets the dimensional values that will be used in fit
   integer function set_dim(r, f, m, num_cuda, lr, svmC, t, tpb) result(out)
       integer :: r,f, m, num_cuda, t, tpb
      real :: lr, svmC
       rows = r
```

```
features = f
      max_iter = m
      num_cudathreads = num_cuda
       learning_rate = lr
       C = svmC
       type = t
       num_ex = ceiling(real(rows) / real(num_cudathreads))
  num_blocks = tpb
   end function
end module gpu_svm
! integer, parameter :: kernel_type = 1, n = 700, max_iter = 10
! real, parameter :: learning_rate = 0.0000000002, C = 5.0
use cudafor
use cublas
use gpu_svm
use data_load
implicit none
integer, parameter :: kernel_type = 1, main_n = 1600, main_max_iter = 1000, main_type = 1,
    threadsPerBlock = 64
real, parameter :: main_learning_rate = 0.0000000002, main_C = 5.0
integer :: t1,t2,t3,t4
real, dimension(:,:), allocatable :: dataset, raw_dataset, test_dataset, raw_test_dataset
! real, device, dimension(:,:), allocatable :: device_kernel_matrix
real, dimension(:), allocatable :: main_labels, main_alpha_arr, main_loss, test_labels
integer, dimension(:), allocatable :: predictions
! real, allocatable, device :: device_dataset(:,:)
! real, allocatable, device :: device_kernel_matrix(:,:)
integer :: main_rows, main_features, count_max, count_rate, test_rows
integer :: istat
integer(8) :: heap
real :: main_bias
!Increase heap size
heap = 16 * 2000 * 2000
```

```
!Setup the cuda devices
istat = cudaSetDevice(0)
istat = cudaDeviceSetLimit(cudaLimitMallocHeapSize, heap)
print*, istat
call system_clock(count_max = count_max, count_rate=count_rate)
    determine_row_num("/home/jrmerkel/Documents/Fortran/SVM_CudaFortran/SVM_Example/data/train.txt")
main_features =
    {\tt determine\_feature\_size("/home/jrmerkel/Documents/Fortran/SVM\_CudaFortran/SVM\_Example/data/train.txt")}
istat = set_dim(main_rows, main_features, main_max_iter, main_n, main_learning_rate,
    main_C, main_type, threadsPerBlock)
istat = allc()
! allocate the dataset and kernel matrices on host and devices
allocate(raw_dataset(main_rows,main_features))
print*, "main_rows", main_rows
print*, "Loading Dataset"
call
    load_data("/home/jrmerkel/Documents/Fortran/SVM_CudaFortran/SVM_Example/data/train.txt",
    raw_dataset, main_rows, main_features)
! allocate arr and matrices
allocate(dataset(main_rows,main_features))
allocate(main_labels(main_rows))
allocate(main_alpha_arr(main_rows))
allocate(main_loss(main_max_iter))
call split_labels(raw_dataset, dataset, main_labels, main_rows, main_features)
call normalize_labels(main_labels, main_rows)
call gpu_construct_kernel_matrix <<<main_n/num_blocks, num_blocks>>>()
istat = cudaDeviceSynchronize()
istat = write_kernel()
```

```
print*, "fit Svm"
call fit_svm( main_alpha_arr, main_loss, main_bias)
call system_clock(t2)
print*, "time = ", t2-t1
print*, "fit done"
! load test dataset
test_rows =
             determine_row_num("/home/jrmerkel/Documents/Fortran/SVM_CudaFortran/SVM_Example/data/test.txt")
! allocate the dataset
allocate(raw_test_dataset(test_rows,main_features))
allocate(test_dataset(test_rows,main_features))
allocate(predictions(test_rows))
print*, "Loading test Data"
call
             {\tt load\_data("/home/jrmerkel/Documents/Fortran/SVM\_CudaFortran/SVM\_Example/data/test.txt", and the properties of the p
             raw_test_dataset, test_rows, main_features)
print*, "Predicting"
! Get the prediction array
allocate(test_labels(test_rows))
call split_labels(raw_test_dataset, test_dataset, test_labels, test_rows, main_features)
call normalize_labels(test_labels, test_rows)
istat = cudaGetLastError()
call predict(dataset, main_labels, main_rows, main_alpha_arr, main_bias, test_dataset,
             test_rows, predictions)
print*, "Writing"
istat = cudaGetLastError()
print *, cudaGetErrorString(istat)
! Score
print*, "predicts ", score(test_labels, predictions, test_rows), "%"
```

```
istat = cudaGetLastError()
print *, cudaGetErrorString(istat)
end
```

Unit tests

```
module unittests
   use svm
   use gpu_svm
   use cudafor
contains
   integer function test_matrix_dot_product() result (out)
       real, dimension(3,3) :: matrixA
       real, dimension(3) :: VecB, outVector
       integer :: n, i, j
       n = 3
       do i = 1, n
          do j = 1, n
              matrixA(i,j) = i*3 -3 + j
          enddo
          VecB(i) = i + 1
       enddo
       call matrix_dot_product(matrixA, VecB, n, outVector)
       if(outVector(1) == 20.00000 .and. outVector(2) == 47.00000 .and. outVector(3) ==
           74.00000) then
          out = 1
       else
          out = 0
       endif
```

```
integer function test_vect_to_matrix() result (out)
real, dimension(3,3) :: outMatrix
real, dimension(3) :: VecA
integer :: n, i, j
n = 3
do i = 1, n
    VecA(i) = i + 1
enddo
call vec_to_matrix(outMatrix, VecA, n)
do i = 1, n
    if(outMatrix(i,1) == (i+1) * 2 .and. outMatrix(i,2) == (i+1) * 3 .and.
         outMatrix(i,3) == (i+1) * 4) then
       out = 1
    else
        out = 0
        return
    \verb"endif"
enddo
end function
attributes(host) integer function gpu_test_vect_to_matrix() result (out)
real,managed, dimension(3,3) :: outMatrix
real,managed, dimension(3) :: VecA
integer :: n, i, j
n = 3
do i = 1, n
    VecA(i) = i + 1
enddo
x = set_dim(3, 3, 1, 10, 0.001, 1.00, 1, 1)
```

end function

```
call gpu_vec_to_matrix<<<1,3>>>(outMatrix, VecA)
do i = 1, n
   if(outMatrix(i,1) == (i+1) * 2 .and. outMatrix(i,2) == (i+1) * 3 .and.
        outMatrix(i,3) == (i+1) * 4) then
       out = 1
   else
       out = 0
       return
   endif
{\tt enddo}
end function
attributes(host) integer function gpucpu_test_vect_to_matrix() result (out)
real,managed, dimension(77,77) :: outMatrix_cpu, outMatrix_gpu
real,managed, dimension(77) :: VecA
integer :: n, i, j
n = 77
call random_number(VecA(i:n))
call gpu_vec_to_matrix<<<5,10>>>(outMatrix_gpu, VecA)
call vec_to_matrix(outMatrix_cpu, VecA, n)
i = cudaDeviceSynchronize()
do i = 1, n
   do j = 1, n
 if(outMatrix_gpu(j,i) == outMatrix_cpu(j,i)) then
    out = 1
 else
    print*, j, i
    out = 0
    return
 endif
```

enddo

```
end function
attributes(host) integer function gpucpu_test_matrix_dot() result (out)
real,managed, dimension(77) :: outVector_cpu, outVector_gpu
real,managed, dimension(77) :: VecB
real, managed, dimension(77,77) :: MatrixA
integer :: n, i, j
n = 77
 do i = 1, n
    Vecb(i) = i + 1
do j = 1, n
  MatrixA(j,i) = i+1
enddo
enddo
i = cudaDeviceSynchronize()
i = cudaGetLastError()
print *, cudaGetErrorString(i)
call gpu_matrix_dot_product<<<5,10>>>(MatrixA, VecB, outVector_gpu)
call matrix_dot_product(MatrixA, VecB, n, outVector_cpu)
i = cudaDeviceSynchronize()
i = cudaGetLastError()
print *, cudaGetErrorString(i)
do i = 1, n
if(outVector_gpu(i) == outVector_cpu(i)) then
  out = 1
else
  out = 0
  return
endif
 enddo
 end function
```

enddo

```
end module
use svm
use gpu_svm
use unittests
integer :: x,y
x = cudaSetDevice(0)
y = set_dim(3, 3, 1, 10, 0.001, 1.00, 1, 1)
x = 1
if(test_matrix_dot_product() == 0) then
   print*, "Matrix Dot Product fails"
   x=0
endif
if(test_vect_to_matrix() == 0) then
   print*, "Vect to Matrix (np.outer) fails"
   x = 0
endif
y = set_dim(77, 3, 1, 10, 0.001, 1.00, 1,1)
if(gpu_test_vect_to_matrix() == 0) then
   print*, "GPU Vect to Matrix (np.outer) fails"
   x = 0
endif
y = set_dim(77, 3, 1, 50, 0.001, 1.00, 1, 10)
if(gpucpu_test_vect_to_matrix() == 0) then
   print*, "GPU and CPU Vect to Matrix (np.outer) mismatch"
   x = 0
endif
if(x == 1)print*,"All Tests Pass"
end
```