

1 Eight Schools Model

```
data {
  int<lower=0> J;          // number of schools
  real y[J];              // estimated treatment effect (school j)
  real<lower=0> sigma[J];  // std err of effect estimate (school j)
}
parameters {
  real mu;
  real theta[J];
  real<lower=0> tau;
}
model {
  theta ~ normal(mu, tau);
  y ~ normal(theta, sigma);
}
```

2 Funnel Model

```
parameters {
  real y;
  vector[9] x;
}
model {
  y ~ normal(0,3);
  x ~ normal(0,exp(y/2));
}
```

3 Gaussian Process

```
// Fit a Gaussian process's hyperparameters
// for squared exponential prior
```

```
data {
  int<lower=1> N;
  vector[N] x;
  vector[N] y;
}
transformed data {
  vector[N] mu;
  for (i in 1:N)
    mu[i] <- 0;
}
parameters {
  real<lower=0> eta_sq;
```

```

    real<lower=0> rho_sq;
    real<lower=0> sigma_sq;
  }
  model {
    matrix[N,N] Sigma;

    // off-diagonal elements
    for (i in 1:(N-1)) {
      for (j in (i+1):N) {
        Sigma[i,j] <- eta_sq * exp(-rho_sq * pow(x[i] - x[j],2));
        Sigma[j,i] <- Sigma[i,j];
      }
    }

    // diagonal elements
    for (k in 1:N)
      Sigma[k,k] <- eta_sq + sigma_sq; // + jitter

    eta_sq ~ cauchy(0,5);
    rho_sq ~ cauchy(0,5);
    sigma_sq ~ cauchy(0,5);

    y ~ multi_normal(mu,Sigma);
  }

```