Spectroscopy (Really Just Photometry)

Robert Lupton

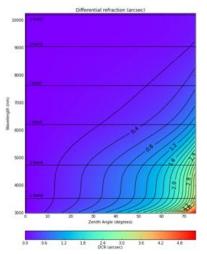
2018-01-25

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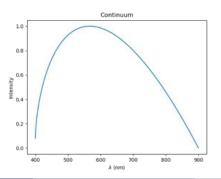
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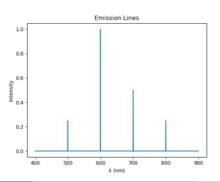
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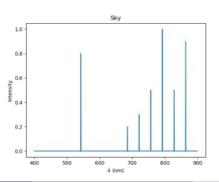
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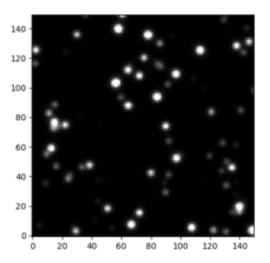
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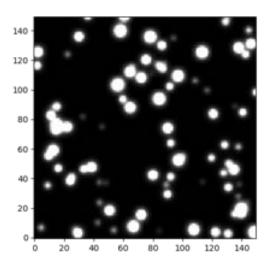


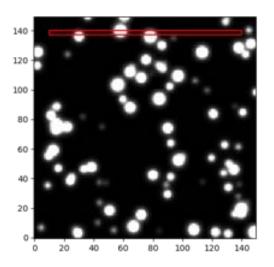
Instrumental Signature Removal

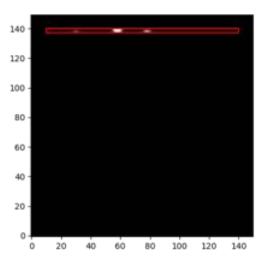
The ISR is similar to an imager's:

- overscan/bias removal
- dark current subtraction
- linearisation
- flat fielding
 - ▶ Use a dispersed flat -- the QE is in general a function of wavelength
 - ► It's not trivial to get a good flat for a fibre spectrograph
- cosmic ray masking/removal

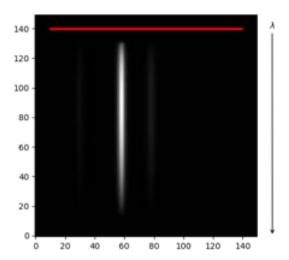




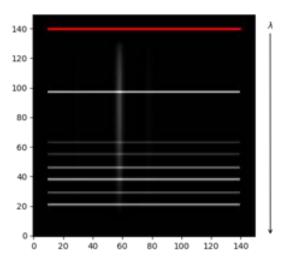




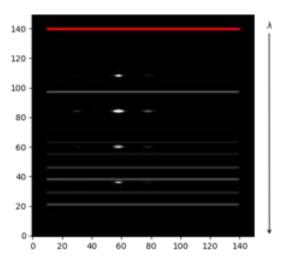
Direct Image with 3-pixel wide slit



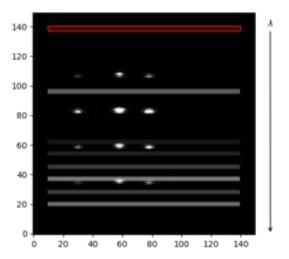
Dispersed 1-pixel wide slit continuum



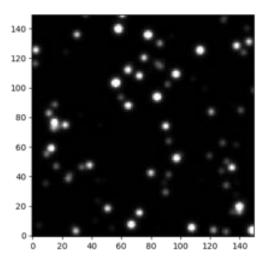
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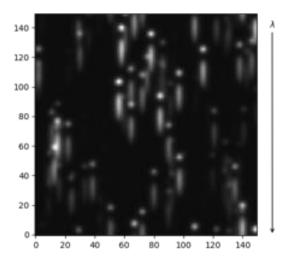


Dispersed 1-pixel wide slit 4 emission lines sky

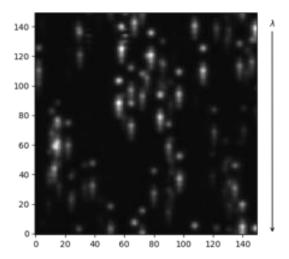


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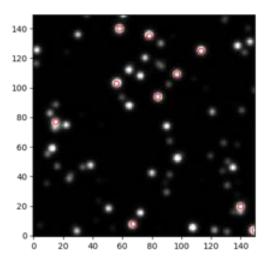


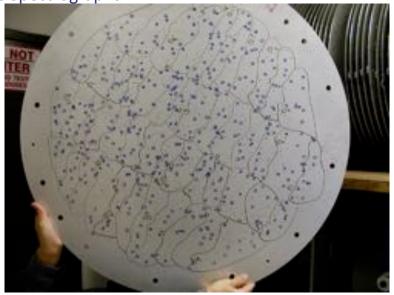


Grism; note 0-order and 1-order images continuum sky



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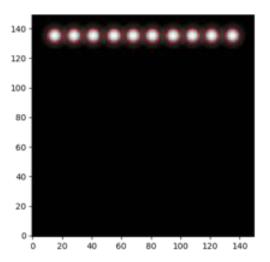


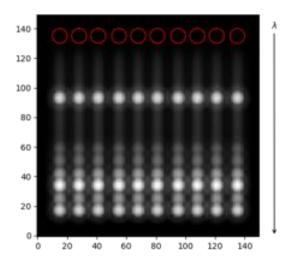


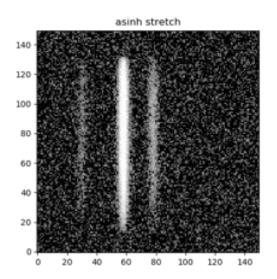
Steel plate into which fibres are plugged



Connecting the sky to the SDSS spectrograph using optical fibres



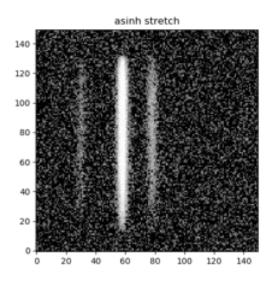


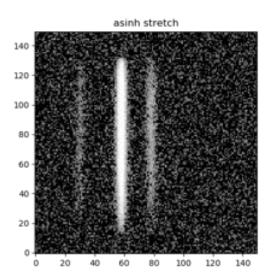


Poisson noise + Gaussian background (readnoise, dark current)

N.b.

$$asinh(x) = \begin{cases} x & |x| \ll 1 \\ \pm \ln|x| & |x| \gg 1 \end{cases}$$

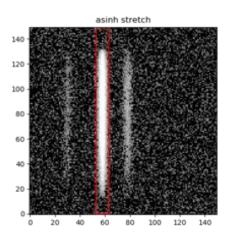




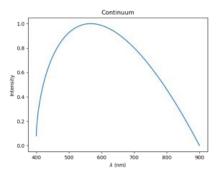
How should we measure those spectra?

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- The rest of the noise is Poisson.

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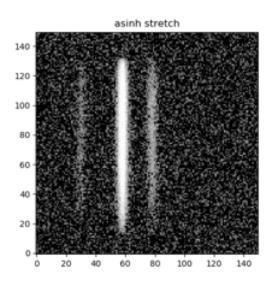
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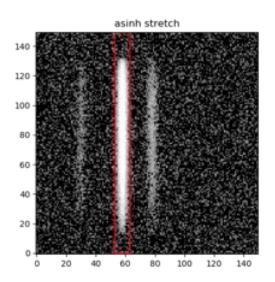
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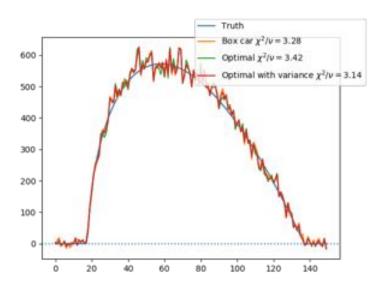
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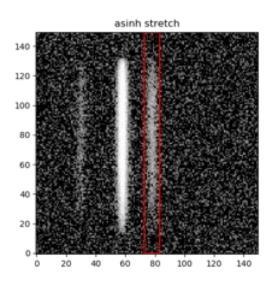
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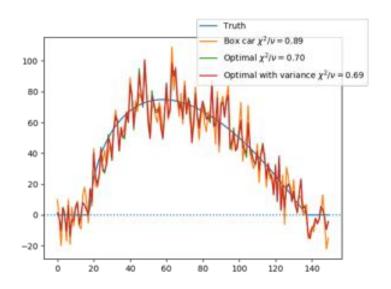
This doesn't invalidate the estimator \hat{A} , but it does mean that it isn't optimal.

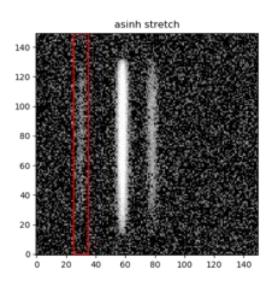


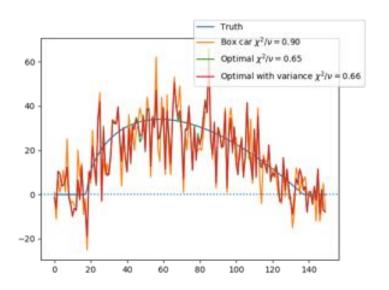












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In reality grism spectra overlap. It helps to take multiple exposures with the grism at a range of positions.

We analysed the case:

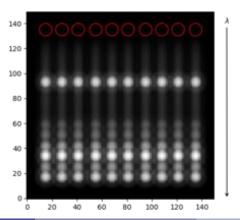
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Unfortunately this is computationally very expensive.

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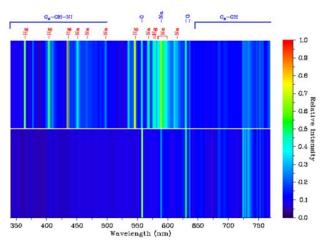
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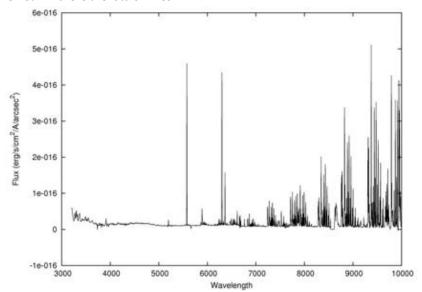
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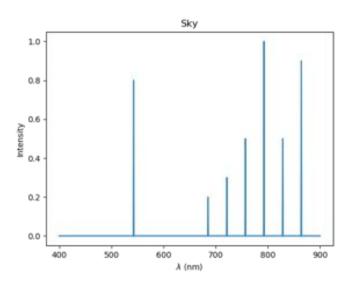
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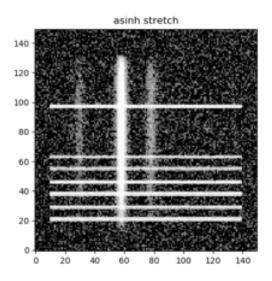


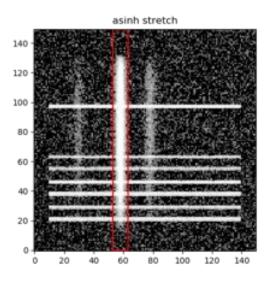
In the near IR there are lots of lines.

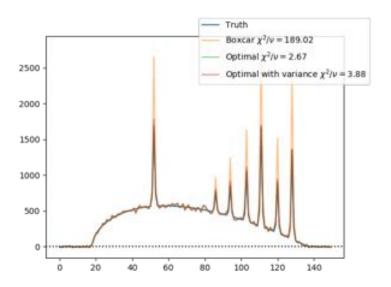


It's a lot worse than this!



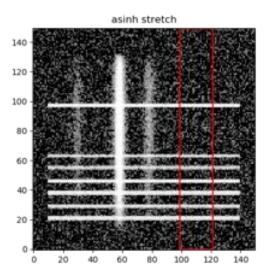




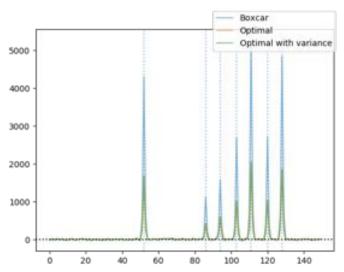


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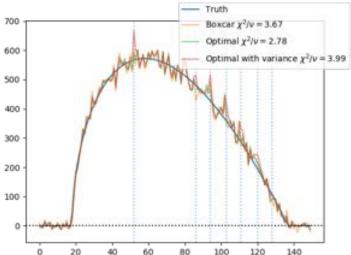


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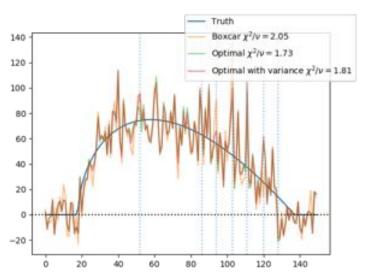
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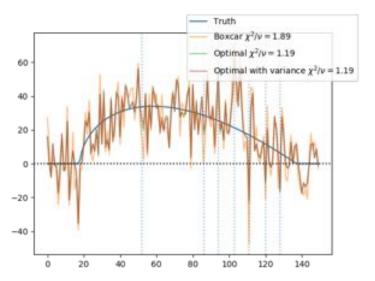


Note the residuals near the sky lines in the "Optimal with variance" spectrum

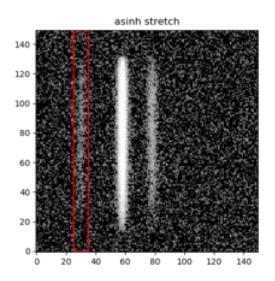
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Sky Subtraction



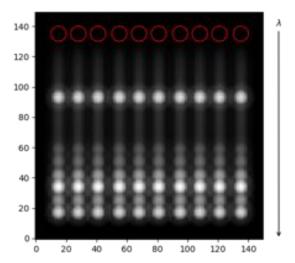
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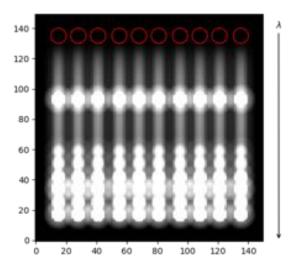
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One successful technique is to do a PCA decomposition of all the sky spectra and use those components to subtract sky.





Note that the wings of the PSF extend to the neighbouring fibres.

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 - 2394 fibres
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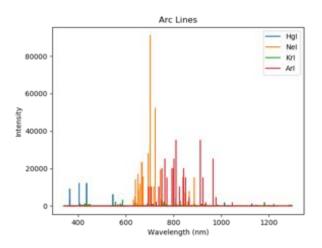
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Wait a year or two, than ask me if it works

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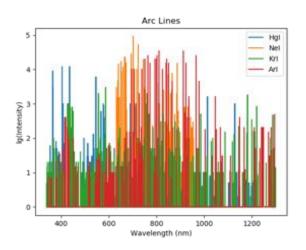
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You then take a spectrum, find the lines (whose wavelengths you know), and estimate the mapping $x \to \lambda$.

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The problem is that high-order polynomials fitted to noisy data tend to be *very* badly behaved between the data points.

Instead, use Chebyshev polynomials, valid for $x \in [-1, 1]$:

$$T_0(x) = 1$$

 $T_1(x) = x$
 $T_2(x) = 2x^2 - 1$
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In general,

$$T_n(x) = \cos(n\arccos(x))$$

so
$$-1 \leq T_n(x) \leq 1$$

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In general,

$$T_n(x) = \cos(n\arccos(x))$$

so
$$-1 \leq T_n(x) \leq 1$$
 and

$$\lambda(x) = \sum_{r=0}^{n-1} a_r T_r(x)$$

is bounded by

$$\lambda(x) = \sum_{r=0}^{n-1} |a_r|$$

Instead, use Chebyshev polynomials, valid for $x \in [-1, 1]$:

$$T_0(x) = 1$$

 $T_1(x) = x$
 $T_2(x) = 2x^2 - 1$
 $T_3(x) = 4x^3 - 3x$
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E.g. np.polynomial.chebyshev.Chebyshev

Photometric Calibration

We've fixed the x-axis; what about the y-axis? This is tricky for two reasons:

- We don't know the sensitivity of the instrument (telescope, grating, detector, ...)
 as a function of lambda
- We don't know what the atmosphere does

The Atmosphere

Scattering and absorption both remove light from the target:

Gray: Clouds

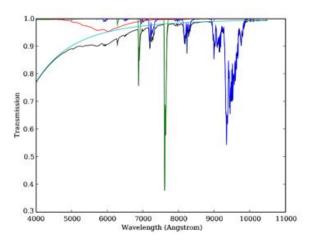
• Chromatic: Aerosols (τ, n) , O_3 , O_2 , H_2O

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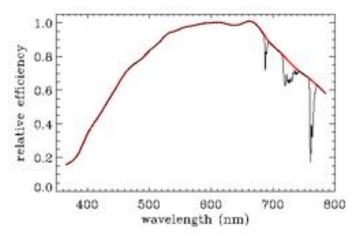
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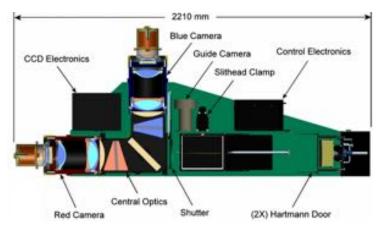


Multi-arm Spectrographs

Many spectrographs have too large a spectral range to only use one detector; the usual solution is to split the light into 2 (or more) paths using *dichroics*.

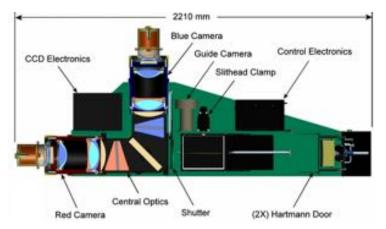
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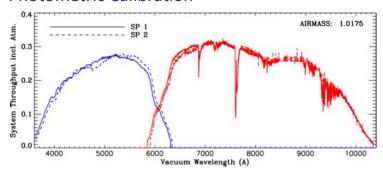
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Now we have a new problem: how do we tie the two arms together?

Photometric Calibration



An SDSS Spectrograph

The solution is to observe objects of known spectrum; ideally

- with a smooth well-known spectrum
- bright
- near your science target

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Objects at a variety of redshifts with known spectra (e.g. Luminous Red Galaxies) provide a way to check for features in our spectro-photometric standards that we failed to fit/model.

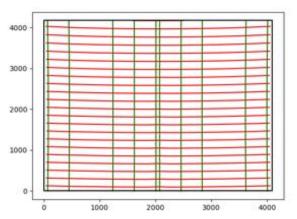
Real Fibre Spectrographs

In the real world fibre spectra don't lie nicely up-and-down the chip, and sky lines don't run along rows of the CCD.

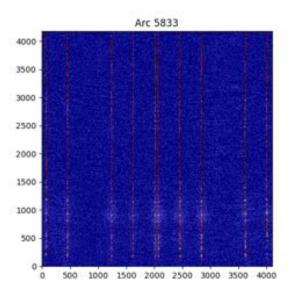
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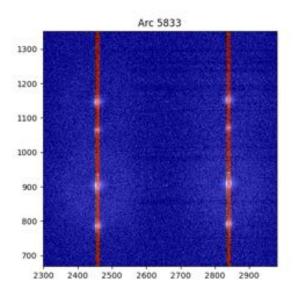
Here's the model that the PFS pipeline uses of the 10 fibres that are currently illuminated in the first spectrograph (it's "r1" -- red arm, spectrograph 1),



What does the data look like?



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Ne arc

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- We still have to understand the spectra, e.g.
 - classify the objects (stars, galaxies, QSOs)
 - fit redshifts
 - fit metallicities, gravities (if appropriate)
 - fit equivalent widths of emission and absorption lines
 - •