# Lwnn Typing Rules

CS 260, Fall 2013

# 1 Typing Rules

# 1.1 Helpers

We use a ClassTable object to embody the necessary global set of classes. Our ClassTable is adapted from the one used in the FetherweightJava paper and is a map from class names to class declarations. Providing a mechanism for looking up field and method types for a given class. A program then is a pair (CT, e), we also make the assumption that the ClassTable is fixed.

$$lookup: ClassTable \times ClassT \rightarrow Class \\ lookup(ct, C) = ct[C]$$

$$method: ClassT \times Var \rightarrow Type$$
 
$$method(C, m) = classTable.lookup(C).method(m)$$

$$field: ClassT \times Var \rightarrow Type$$
 
$$field(C,f) = classTable.lookup(C).field(f)$$

# 1.2 Subtyping

$$A <: A$$
 (Reflexivity)

$$\frac{C <: B \quad B <: A}{C <: A} \tag{Transitivity}$$

$$\frac{class \ C \ extends \ D \ \{...\}}{C <: D} \tag{Inheritance}$$

#### 1.3 Classes

$$\frac{\Gamma \vdash}{todo}$$
 (T-Class)

# 1.4 Methods

$$\frac{\Gamma \vdash}{todo}$$
 (T-Method)

# 1.5 Statements

$$\frac{\Gamma \vdash x : \tau \qquad \Gamma \vdash e : \tau}{\Gamma \vdash x := e : \mathtt{null}} \tag{T-Assign}$$

$$\frac{\Gamma \vdash e_1 : C \qquad field(C, x) = \tau_f \qquad \Gamma \vdash e_2 : \tau_f}{\Gamma \vdash e_1 . x := e_2 : \mathtt{null}} \qquad (\text{T-UPDATE})$$

$$\frac{\Gamma \vdash e : C \qquad method(C,m) = \vec{\tau_d} \rightarrow \tau_r \qquad \Gamma \vdash \vec{e_i} : \vec{\tau_c} \qquad \vec{\tau_c} <: \vec{\tau_d} \qquad \Gamma \vdash x : \tau_r}{\Gamma \vdash x := e.m(\vec{e_i}) : \texttt{null}}$$

(T-METHOD-INVOCATION)

$$\frac{\Gamma \vdash x : D \qquad \Gamma \vdash e : C \qquad method(C, "C") = \vec{\tau_i} \to C \qquad \vec{e_i} : \vec{\tau_i} \qquad C <: D \qquad \mathbf{new} \ C(\vec{e_i}) : D}{\Gamma \vdash x := \mathbf{new} \ C(\vec{e_i}) : \mathbf{null}} \tag{T-New}$$

$$\frac{\Gamma \vdash e : \mathtt{bool}}{\Gamma \vdash \mathbf{if} \ (e) \ \vec{s_1} \ \mathbf{else} \ \vec{s_2} : \mathtt{null}} \tag{T-IF}$$

$$\frac{\Gamma \vdash e : \mathtt{bool}}{\Gamma \vdash \mathbf{while} \ (e) \ \vec{s} : \mathtt{null}} \tag{T-While}$$

#### 1.6 Expressions

$$\Gamma \vdash i : \mathtt{int}$$
 (T-INT)

$$\Gamma \vdash str : \mathtt{string}$$
 (T-STRING)

$$\Gamma \vdash \mathsf{true} : \mathsf{bool}$$
 (T-TRUE)

$$\Gamma \vdash \mathsf{false} : \mathsf{bool}$$
 (T-FALSE)

$$\Gamma \vdash \mathsf{null} : \mathtt{null}$$
 (T-NULLS)

$$\Gamma \vdash x : \Gamma(x)$$
 (T-VAR)

$$\frac{\Gamma \vdash e : C \qquad field(C,f) = \tau}{\Gamma \vdash e.f : \tau} \tag{T-Access}$$

$$\frac{\oplus \in \{+,-,*,\div,<,\leq\} \qquad \Gamma \vdash e_1 : \text{int} \qquad \Gamma \vdash e_2 : \text{int}}{\Gamma \vdash e_1 \oplus e_2 : \text{int}} \text{ (T-NumOps)}$$
 
$$\frac{\oplus \in \{\land,\lor\} \qquad \Gamma \vdash e_1 : \text{bool} \qquad \Gamma \vdash e_2 : \text{bool}}{\Gamma \vdash e_1 \oplus e_2 : \text{bool}} \qquad \text{(T-BoolOps)}$$
 
$$\frac{\oplus \in \{=,\neq\} \qquad \Gamma \vdash e_1 : \tau_1 \qquad \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash e_1 \oplus e_2 : \text{bool}} \qquad \text{(T-EqOps)}$$