Here is a list of important math rules you should know. We may not use all of them directly, or I may omit some to save time, but they are generally helpful in econometrics work.

Summation Rules

Let x and y be vectors of length n.

1. Summation definition: $\sum_{i=1}^{n} x_i \equiv x_1 + x_2 + \cdots + x_n$

2. The sum of $x+y$ is the same as the sum of x plus the sum of y: $sum_i(x_i+y_i) = \sum_{i=1} x_i + \sum_i y_i$

3. For any constant c, the sum of $c \times x$ is the same as c times the sum of x: $\sum_i cx_i = c\sum_i x_i$

4. In general, the sume of x times y is not equal to the sum of x times the sum of y:
   $\sum_i x_i y_i \neq \sum_i x_i \sum_i y_i$

Variance Rules

- The variance of a constant is zero: $Var c = 0$

- The variance of a constant times a random variable: $Var(cX) = c^2 Var(X)$

- The variance of a constant plus a random variable: $Var(c + X) = Var(x)$

- The variance of the sum of two random variables: $Var(X+Y) = Var(X)+Var(Y)+2Cov(X,Y)$

Covariance Rules

- The covariance of a random variable with a constant is 0: $Cov(X,c) = 0$

- The covariance of a random variable with itself is its variance: $Cov(X,X) = Var(X)$

- Constants can be brought outside of the covariance: $Cov(X,cY) = cCov(X,Y)$

- If Z is a third random variable, then: $Cov(X,Y + Z) = Cov(X,Y) + Cov(X,Z)$

$plim$ Rules

$plim$ stands for probability limit, that is: $plim_{n\to\infty}\hat{\theta}_n = 0$. So as the sample size n increases, the estimator $\hat{\theta}_n$ converges in probability to the true value θ.
Let c be a constant. Let x_n and y_n be sequences of random variables where $plim(x_n) = x$ and $plim(y_n) = y$

1. The probability limit of a constant is the constant: $plim(c) = c$

2. $plim(x_n + y_n) = x + y$

3. $plim(x_n y_n) = xy$

4. $plim(\frac{x_n}{y_n}) = \frac{x}{y}$

5. $plim(g(x_n, y_n)) = g(x,y)$ for any function $g()$

Expectations Rules

Let A and B be random variables, and let c be a constant.

1. $\mathbb{E}[A + B] = \mathbb{E}[A] + \mathbb{E}[B]$

2. In general, $\mathbb{E}[AB] \neq \mathbb{E}[A]\mathbb{E}[B]$

3. Constants can pass outside of an expectation: $\mathbb{E}[cA] = c\mathbb{E}[A]$

4. Since $\mathbb{E}[A]$ is a constant, then: $\mathbb{E}[B\mathbb{E}[A]] = \mathbb{E}[A]\mathbb{E}[B]$

Conditional Expectations Rules

If the conditional expectation of something is a constant, then the unconditional expectation is that same constant:

If $\mathbb{E}[A|B] = c$, then $\mathbb{E}[A] = c$.

Why? The **law of iterated expectations:**

$$\begin{aligned}
\mathbb{E}[A] &= \mathbb{E}[\mathbb{E}[A|B]] \\
&= \mathbb{E}[c] \\
&= c
\end{aligned}$$

Log Rules

1. $log_e(e) = 1$

2. $log(ab) = log(a) + log(b)$

3. $log(\frac{a}{b}) = log(a) - log(b)$

4. $log(a^b) = b \times log(a)$