ODE number: 1

$$dxxy(x) + dx(x+1)\frac{d}{dx}y(x) = 0$$

Solution:

$$y(x) = C(x+1)e^{-x}$$

CORRECT

ODE number: 2

$$x\frac{d}{dx}y(x) - 2y(x) = bx^3y^2(x)$$

Solution:

$$y(x) = \frac{5x^2}{C - bx^5}$$

CORRECT

ODE number: 3

$$dxxy(x) + dx(x+1)\frac{d}{dx}y(x) = 0$$

Solution:

$$y(x) = C(x+1)e^{-x}$$

CORRECT

ODE number: 4

$$x\frac{d}{dx}y(x) - 2y(x) = bx^3y^2(x)$$

Given solution:

$$y(x) = \frac{5x^2}{C + x^5}$$

is INCORRECT

The correct one is:

$$y(x) = \frac{x^2}{C_1 - \frac{bx^5}{5}}$$

ODE number: 5

$$\frac{d}{dx}y(x) = (9x + y(x) - 1)^2$$

Solution:

$$y(x) = -9x + -\frac{3\sin(C - 3x)}{\cos(C - 3x)} + 1$$

CORRECT