Tabelas

579

TABELA DE DERIVADAS

Nesta tabela $u \in v$ são funções deriváveis de $x \in c$, $\alpha \in a$ são constantes.

- (1) $y = c \Rightarrow y' = 0$
- $(2) \quad y = x \Rightarrow y' = 1$
- (3) $y = c \cdot u \Rightarrow y' = c \cdot u'$
- (4) $y=u+v \Longrightarrow y'=u'+v'$
- (5) $y = u \cdot v \Rightarrow y' = u \cdot v' + v \cdot u'$
- (6) $y = \frac{u}{v} \Rightarrow y' = \frac{y \cdot u' u \cdot y'}{v^2}$
- (7) $y = u^{\alpha}, (\alpha \neq 0) \Rightarrow y' = \alpha \cdot u^{\alpha 1} \cdot u'$
- (8) $y = a^{\mu} (a > 0, a \neq 1) \Rightarrow y' = a^{\mu} \cdot \ln a \cdot \mu'$
- (9) $y = e^{u} \Rightarrow y' = e^{u} \cdot u'$
- (10) $y = \log_a u \Rightarrow y' = \frac{u'}{u} \log_a e$
- (11) $y = \ln u \Rightarrow y' = \frac{u'}{u}$
- $(12) \ \ y=u^{\nu} \Rightarrow y \ , = \nu \cdot u^{\nu-1} \cdot u \ , + u^{\nu} \cdot \ln u \cdot \nu \ , \ (u>0)$
- (13) $y = \operatorname{sen} u \Rightarrow y' = \cos u \cdot u'$
- (14) $y = \cos u \Rightarrow y' = -\sin u \cdot u'$
- (15) $y = tg u \Rightarrow y' = sec^2 u \cdot u'$
- (16) $y = \cot u \Rightarrow y' = -\csc^2 u \cdot u'$
- (17) $y = \sec u \Rightarrow y' = \sec u \cdot tg u \cdot u'$

- (18) $y = \csc u \Rightarrow y' = -\csc u \cdot \cot u \cdot u'$
- (19) $y = \operatorname{arc sen} u \Rightarrow y' = \frac{u'}{\sqrt{1 u^2}}$
- (20) $y = \operatorname{arc} \cos u \Rightarrow y' = \frac{-u'}{\sqrt{1-u^2}}$
- (21) $y = \text{arc tg } u \Rightarrow y' = \frac{u'}{1+u^2}$
- (22) $y = \operatorname{arc cot} y = y' = \frac{-u'}{1+u^2}$
- (23) $y = \text{arc sec } u, |u| \ge 1 \Rightarrow y' = \frac{u'}{|u| \sqrt{u^2 1}}, |u| > 1$
- (24) y = arc cosec u, $|u| \ge 1 \Rightarrow y' = \frac{-u'}{|u| \sqrt{u^2 1}}$, |u| > 1
- (25) $y = \operatorname{senh} u \Rightarrow y' = \cosh u \cdot u'$
- (26) $y = \cosh u \Rightarrow y' = \operatorname{senh} u \cdot u'$
- (27) $y = \operatorname{tgh} u \Rightarrow y' = \operatorname{sech}^2 u \cdot u'$
- (28) $y = \operatorname{cotgh} u \Rightarrow y' = -\operatorname{cosech}^2 u \cdot u'$
- (29) $y = \operatorname{sech} u \Rightarrow y' = -\operatorname{sech} u \cdot \operatorname{tgh} u \cdot u'$
- (30) $y = \operatorname{cosech} u \Rightarrow y' = -\operatorname{cosech} u \cdot \operatorname{cotgh} u \cdot u'$
- (31) $y = \arg \sinh u \Rightarrow y' = \frac{u}{\sqrt{u^2 + 1}}$
- (32) $y = \arg \cosh u \Rightarrow y' = \frac{u'}{\sqrt{u^2 1}}, u > 1$
- (33) $y = \arg \tanh u \Rightarrow y' = \frac{u'}{1 u^2}$, |u| < 1