hw3

March 3, 2021

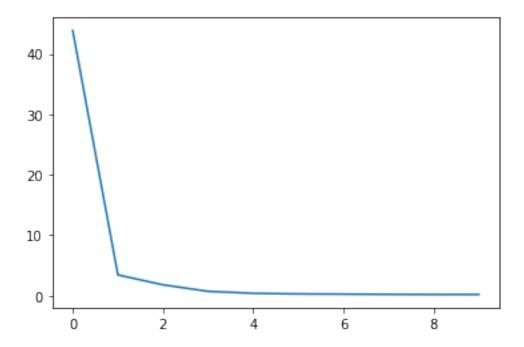
[1]: import numpy as np

```
import pandas as pd
        import matplotlib.pyplot as plt
        import sklearn.decomposition as skd
        import sklearn.preprocessing as skp
        import sklearn.pipeline as skpipe
[1060]: ff_factors = pd.read_csv('F-F_Research_Data_Factors.CSV', skiprows=3,__
        \rightarrowindex_col=0,
                                   engine='python', parse_dates=True,_
        ff_factors = ff_factors.loc[ff_factors.index >= 196311]
        ff_factors = ff_factors.loc[ff_factors.index <= 201712]</pre>
        portfolio_panel = pd.read_csv('25_Portfolios_5x5.CSV', skiprows=15, index_col=0,
                                   engine='python', parse_dates=True,_
        →infer_datetime_format=True)
        portfolio_1_names = portfolio_panel.columns
        portfolio_panel = portfolio_panel.loc[portfolio_panel.index >= 196311]
        portfolio_panel = portfolio_panel.loc[portfolio_panel.index <= 201712]</pre>
        portfolio370_panel = pd.read_csv('370portfolios.csv', skiprows=1, index_col=0,
                                   engine='python', parse_dates=True, __
        →infer_datetime_format=True)
        portfolio_2_names = portfolio370_panel.columns
[1014]: ff_factor_panel = ff_factors.to_numpy() / 100
        # make returns excess
        portfolio_return_panel = portfolio_panel.to_numpy() / 100 - ff_factor_panel[:,__
        →3:4]
        portfolio370_return_panel = portfolio370_panel.to_numpy() - ff_factor_panel[:,u
        <u></u>3:41
[1015]: panel_evals, = np.linalg.eigh(portfolio_return_panel.
        →dot(portfolio_return_panel.T))
        panel_evals = panel_evals[::-1]
        panel370_evals, _ = np.linalg.eigh(portfolio370_return_panel.
        →dot(portfolio370_return_panel.T))
```

```
panel370_evals = panel370_evals[::-1]
```

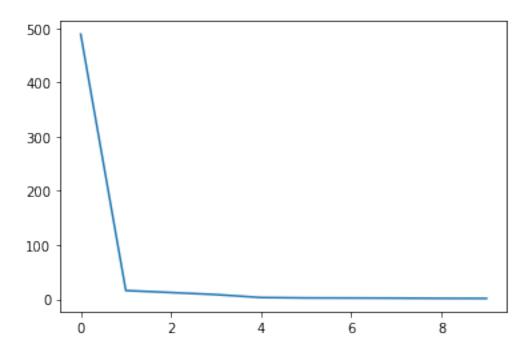
[1016]: plt.plot(panel_evals[:10])

[1016]: [<matplotlib.lines.Line2D at 0x1a5baf33c8>]



[1017]: plt.plot(panel370_evals[:10])

[1017]: [<matplotlib.lines.Line2D at 0x1a55e03240>]



Code for parts 1-5

```
[1018]: def ic_1(N,T):
            NT = N*T
            N_plus_T = N+T
            return np.log(NT/N_plus_T) * N_plus_T/NT
        def 12_loss(N,T,data_panel, pred_data):
            return (1/(N*T))*np.sum(np.square(data_panel - pred_data))
        def fit_bai_ng(data_panel, K):
            T,N = data_panel.shape
            pipe = skpipe.Pipeline([('Factors', skd.TruncatedSVD(K,__
         →algorithm='arpack'))])
            lmbda = pipe.fit_transform((1/np.sqrt(T))*(data_panel - np.mean(data_panel,__
         ⇒axis=0, keepdims=True)).T).T
            F = np.linalg.lstsq(lmbda.T, data_panel.T, rcond=None)[0].T
            data_hat_last = F.dot(lmbda)
            return F, lmbda, data_hat_last
        def bai_ng_ev_criterion(data_panel, ic_func, max_evs=15):
            T, N = data_panel.shape
```

```
penalized_function_resuls = []
   for i in range(1, max_evs + 1):
       F, lmbda, pred_panel = fit_bai_ng(data_panel, i)
       penalized_function_resuls_append(np.log(12_loss(N,T,data_panel,_
 →pred_panel)) + i*ic_func(N,T))
   return penalized function resuls
def ahn_horenstein_evr(data_panel, max_evs=15):
   T, N = data_panel.shape
   means = np.mean(data_panel, axis=1, keepdims=True)
   evals, _ = np.linalg.eigh(data_panel.dot(data_panel.T) - means.dot(means.T))
   evals = evals[::-1][:max_evs]
   ratios = [x / y for x,y in zip(evals[:-1], evals[1:])]
   return ratios
def fit_rp_pca(data_panel, K, gamma):
   T, N = data_panel.shape
     std_pipe = skpipe.Pipeline([('Standardize', skp.
→StandardScaler(with_mean=True, with_std=True))])
   fit_pipe = skpipe.Pipeline([('loadings', skd.TruncatedSVD(K,__
→algorithm='arpack'))])
   r bar = np.mean(data panel, axis=0, keepdims=True)
   objective = (1/(N))*data_panel.T.dot(data_panel) + (gamma)*r_bar.T.
→dot(r bar)
   lmbda = fit_pipe.fit_transform(objective)
   print(lmbda.shape, data_panel.shape)
   F = np.linalg.lstsq(lmbda, data_panel.T, rcond=None)[0]
   return F.T, lmbda.T
def onatski(data panel, rmax=10, max iter=100):
   T,N = data_panel.shape
   evals, = np.linalg.eigh(data panel.dot(data panel.T) / T)
   evals = evals[::-1]
   converged = False
   i = 0
   j=rmax + 1
   offset_vect = np.array([[1, -1],
                            [1, 0],
                            [1, 1],
                            [1, 2],
                            [1, 3])
   while not converged and i < max_iter:</pre>
       i += 1
       tgt = evals[j-1:j+4]
```

```
regressor = np.copy(offset_vect)
regressor[:,1] += j
regressor[:,1] = regressor[:,1]**(2/3)
beta_hat = np.linalg.lstsq(regressor, tgt, rcond=None)[0][1]

delta = 2 * np.abs(beta_hat)

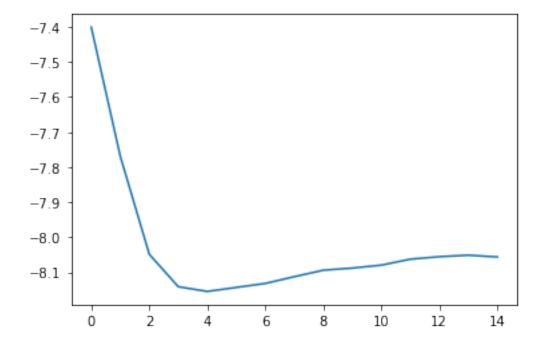
filtered = [i for i in range(rmax) if evals[i] - evals[i+1] >= delta]
rhat = max(filtered) if len(filtered) > 0 else 0
j_new = rhat + 1
converged = j_new == j
j = j_new
return j
```

0.0.1 1

```
[1019]: by_factor_ic = bai_ng_ev_criterion(portfolio_return_panel, ic_1)
print(np.argmin(by_factor_ic) + 1)
plt.plot(by_factor_ic)
```

5

[1019]: [<matplotlib.lines.Line2D at 0x1a54764c18>]

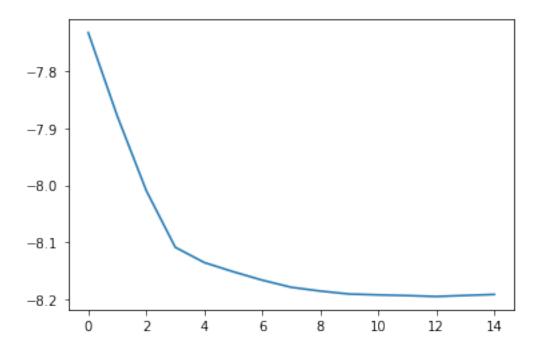


We see that in this case (the first information criterion function in Bai and Ng) we select $\mathbf{k}=5$ factors

```
[1038]: by_factor_ic = bai_ng_ev_criterion(portfolio370_return_panel, ic_1)
    print(np.argmin(by_factor_ic) + 1)
    plt.plot(by_factor_ic)
```

13

[1038]: [<matplotlib.lines.Line2D at 0x1a30a42128>]

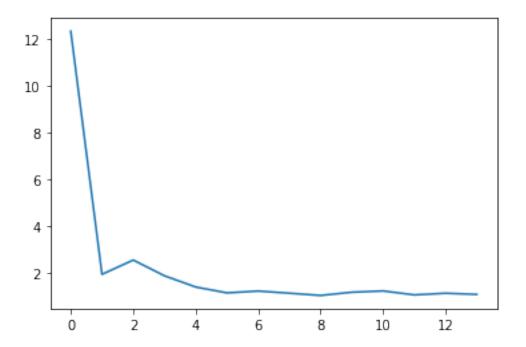


We see that in this case (the first information criterion function in Bai and Ng) we select $\mathbf{k}=13$ factors

0.0.2 2

```
[1040]: byf_factor_evr = ahn_horenstein_evr(portfolio_return_panel)
plt.plot(byf_factor_evr)
```

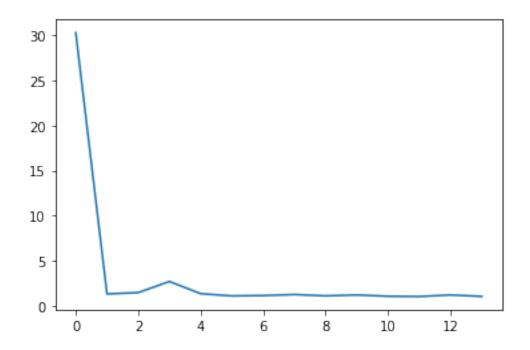
[1040]: [<matplotlib.lines.Line2D at 0x1a54b76940>]



In this case we would select k=2 factors

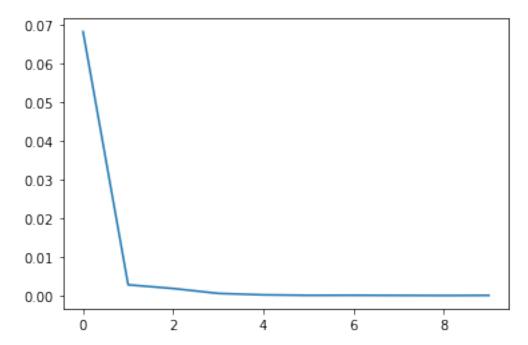
```
[1022]: byf_factor_evr = ahn_horenstein_evr(portfolio370_return_panel)
plt.plot(byf_factor_evr)
```

[1022]: [<matplotlib.lines.Line2D at 0x1a5b598b38>]



In this case we would select k=3 factors

0.0.3 3

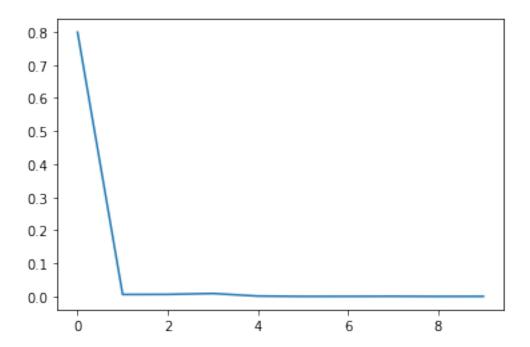


[1078]: (1, 1)

in this case we would select k=1 factor, we see that the choice is robust between rmax = 10 or 20

[1052]: plt.plot((panel370_evals[:10] - panel370_evals[1:11])/np.sum(panel370_evals))

[1052]: [<matplotlib.lines.Line2D at 0x1a5503fac8>]



```
[1080]: onatski(portfolio370_return_panel, rmax=10), onatski(portfolio370_return_panel, ⊔ →rmax=20)
```

[1080]: (4, 4)

in this case we would selct k=4 factors

0.0.4 4

```
[1050]: pca_factors_25, pca_loadings_25, _ = fit_bai_ng(portfolio_return_panel, 3) pca_factors_370, pca_loadings_370, _ = fit_bai_ng(portfolio370_return_panel, 5)
```

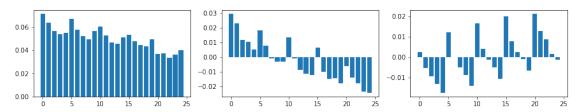
0.0.5 5

```
[1051]: rp_pca_factors_25, rp_pca_loadings_25 = fit_rp_pca(portfolio_return_panel, 3, u →gamma=20)
rp_pca_factors_370, rp_pca_loadings_370 = fit_rp_pca(portfolio370_return_panel, u →5, gamma=20)
```

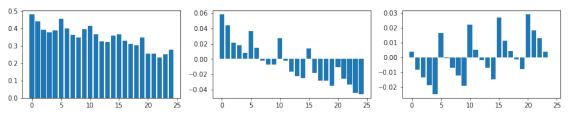
(25, 3) (650, 25) (370, 5) (650, 370)

0.0.6 6

```
[1027]: fig, axs = plt.subplots(1,3,figsize=(15,2.5))
for i in range(3):
    axs[i].bar(np.arange(25), pca_loadings_25[i])
plt.show()
```



```
[1028]: fig, axs = plt.subplots(1,3,figsize=(15,2.5))
for i in range(3):
    axs[i].bar(np.arange(25), rp_pca_loadings_25[i])
plt.show()
```



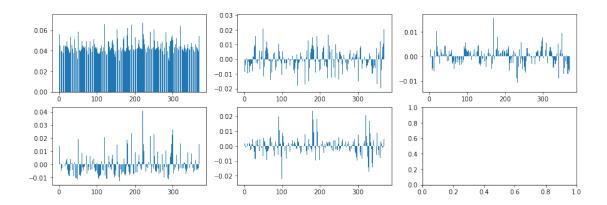
```
[1059]: portfolio_1_names

[1059]: Index(['SMALL LoBM', 'ME1 BM2', 'ME1 BM3', 'ME1 BM4', 'SMALL HiBM', 'ME2 BM1', 'ME2 BM2', 'ME2 BM3', 'ME2 BM4', 'ME2 BM5', 'ME3 BM1', 'ME3 BM2', 'ME3 BM3', 'ME3 BM4', 'ME3 BM5', 'ME4 BM1', 'ME4 BM2', 'ME4 BM3', 'ME4 BM4', 'ME4 BM5', 'BIG LoBM', 'ME5 BM2', 'ME5 BM3', 'ME5 BM4', 'BIG HiBM'],
```

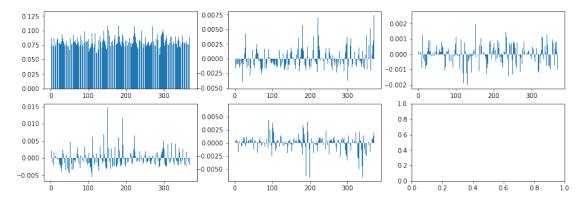
dtype='object')

In the case of the 25 factors, rp_pca and pca fit very similar factors. The first is clearly a market factor, the second is long small / low book to market stocks and moves somewhat linearly to short as btm/size increase. the spikes are whenever we switch from high book to market to low. The third factor is long small stocks, short low btm stocks.

```
[1029]: fig, axs = plt.subplots(2,3, figsize=(15,5))
for i in range(5):
    axs[i%2][i//2].bar(np.linspace(1, 370, 370), pca_loadings_370[i])
plt.show()
```



[1030]: fig, axs = plt.subplots(2,3, figsize=(15,5))
 for i in range(5):
 axs[i%2][i//2].bar(np.linspace(1, 370, 370), rp_pca_loadings_370[i])
 plt.show()



[1063]: print(', '.join(portfolio_2_names))

p1, p2, p3, p4, p5, p6, p7, p8, p9, p10, p1.1, p2.1, p3.1, p4.1, p5.1, p6.1, p7.1, p8.1, p9.1, p10.1, p1.2, p2.2, p3.2, p4.2, p5.2, p6.2, p7.2, p8.2, p9.2, p10.2, p1.3, p2.3, p3.3, p4.3, p5.3, p6.3, p7.3, p8.3, p9.3, p10.3, p1.4, p2.4, p3.4, p4.4, p5.4, p6.4, p7.4, p8.4, p9.4, p10.4, p1.5, p2.5, p3.5, p4.5, p5.5, p6.5, p7.5, p8.5, p9.5, p10.5, p1.6, p2.6, p3.6, p4.6, p5.6, p6.6, p7.6, p8.6, p9.6, p10.6, p1.7, p2.7, p3.7, p4.7, p5.7, p6.7, p7.7, p8.7, p9.7, p10.7, p1.8, p2.8, p3.8, p4.8, p5.8, p6.8, p7.8, p8.8, p9.8, p10.8, p1.9, p2.9, p3.9, p4.9, p5.9, p6.9, p7.9, p8.9, p9.9, p10.9, p1.10, p2.10, p3.10, p4.10, p5.10, p6.10, p7.10, p8.10, p9.10, p10.10, p1.11, p2.11, p3.11, p4.11, p5.11, p6.11, p7.11, p8.11, p9.11, p10.11, p1.12, p2.12, p3.12, p4.12, p5.12, p6.12, p7.12, p8.12, p9.12, p10.12, p1.13, p2.13, p3.13, p4.13, p5.13, p6.13, p7.13, p8.13, p9.13, p10.13, p1.14, p2.14, p3.14, p4.14, p5.14, p6.14, p7.14, p8.14, p9.14, p10.14, p1.15, p2.15, p3.15, p4.15, p5.15, p6.15, p7.15, p8.15, p9.15, p10.15, p1.16,

```
p2.16, p3.16, p4.16, p5.16, p6.16, p7.16, p8.16, p9.16, p10.16, p1.17, p2.17,
p3.17, p4.17, p5.17, p6.17, p7.17, p8.17, p9.17, p10.17, p1.18, p2.18, p3.18,
p4.18, p5.18, p6.18, p7.18, p8.18, p9.18, p10.18, p1.19, p2.19, p3.19, p4.19,
p5.19, p6.19, p7.19, p8.19, p9.19, p10.19, p1.20, p2.20, p3.20, p4.20, p5.20,
p6.20, p7.20, p8.20, p9.20, p10.20, p1.21, p2.21, p3.21, p4.21, p5.21, p6.21,
p7.21, p8.21, p9.21, p10.21, p1.22, p2.22, p3.22, p4.22, p5.22, p6.22, p7.22,
p8.22, p9.22, p10.22, p1.23, p2.23, p3.23, p4.23, p5.23, p6.23, p7.23, p8.23,
p9.23, p10.23, p1.24, p2.24, p3.24, p4.24, p5.24, p6.24, p7.24, p8.24, p9.24,
p10.24, p1.25, p2.25, p3.25, p4.25, p5.25, p6.25, p7.25, p8.25, p9.25, p10.25,
p1.26, p2.26, p3.26, p4.26, p5.26, p6.26, p7.26, p8.26, p9.26, p10.26, p1.27,
p2.27, p3.27, p4.27, p5.27, p6.27, p7.27, p8.27, p9.27, p10.27, p10.28, p2.28,
p3.28, p4.28, p5.28, p6.28, p7.28, p8.28, p9.28, p10.28, p1.29, p2.29, p3.29,
p4.29, p5.29, p6.29, p7.29, p8.29, p9.29, p10.29, p1.30, p2.30, p3.30, p4.30,
p5.30, p6.30, p7.30, p8.30, p9.30, p10.30, p1.31, p2.31, p3.31, p4.31, p5.31,
p6.31, p7.31, p8.31, p9.31, p10.31, p1.32, p2.32, p3.32, p4.32, p5.32, p6.32,
p7.32, p8.32, p9.32, p10.32, p1.33, p2.33, p3.33, p4.33, p5.33, p6.33, p7.33,
p8.33, p9.33, p10.33, p1.34, p2.34, p3.34, p4.34, p5.34, p6.34, p7.34, p8.34,
p9.34, p10.34, p1.35, p2.35, p3.35, p4.35, p5.35, p6.35, p7.35, p8.35, p9.35,
p10.35, p1.36, p2.36, p3.36, p4.36, p5.36, p6.36, p7.36, p8.36, p9.36, p10.36
```

These are naturally a little harder to visually interprit, although we can certainly say that the first is a market factor. We can in this case, however, see a clear difference bewteen pca and rp-pca emerging.

0.0.7 7

```
[1031]: def sharpe(series):
            return np.mean(series) / np.std(series)
        def sharpe_factors(factors_t_n):
            mu_f = np.mean(factors_t_n, axis=0, keepdims=True)
            return np.sqrt(mu_f.dot(np.linalg.inv(np.cov(factors_t_n.T))).dot(mu_f.T))
        def markowitz(panel_t_n):
            T,N = panel_t_n.shape
            mu = np.mean(panel_t_n, axis=0, keepdims=True)
            cov = np.cov(panel_t_n.T)
            if N > 1:
                return np.linalg.inv(cov).dot(mu.T)
            else:
                return mu.T / cov
        def sharpe_of_factors(factors):
            portfolio = markowitz(factors)
            return sharpe(factors.dot(portfolio))
```

```
market factor
[1032]: sharpe_of_factors(ff_factor_panel[:,0:1])
[1032]: 0.11964372062827072
       fama french 3 factor
[1033]: sharpe_factors(ff_factor_panel[:,0:3])
[1033]: array([[0.2072842]])
       pca 3 factors
[1034]: sharpe_factors(pca_factors_25)
[1034]: array([[0.21833483]])
       rp-pca 3 factors
[1035]: sharpe_factors(rp_pca_factors_25)
[1035]: array([[0.22187965]])
       pca 5 factors second portfolios
[1036]: sharpe_factors(pca_factors_370)
[1036]: array([[0.24663223]])
       rp-pca 5 factors second portfolios
[1037]: sharpe_factors(rp_pca_factors_370)
[1037]: array([[0.57723402]])
       0.0.8 8
 [959]: import scipy as scp
 [981]: def time_series_ap_test(factors, test_assets):
            T, N = test_assets.shape
            _, K = factors.shape
            ones_T = np.ones((T,1))
            loadings = np.linalg.lstsq(np.concatenate([ones_T, factors], axis=1),
                             test assets, rcond=None)[0]
            alphas = loadings[0:1, :]
            betas = loadings[1:, :]
```

```
residuals = test_assets - np.concatenate([ones_T, factors], axis=1).
      →dot(loadings)
                f_bar = np.mean(factors, axis=0, keepdims=True)
                if K == 1:
                              omega = (1/T)*sum([(factors[t:t+1,:] - f bar).T.dot(factors[t:t+1,:] - f bar).T.dot(factors[
     \rightarrowf bar) for t in range(T)])
                else:
                              omega = np.cov(factors.T)
                sigma_hat = (1/T)*sum([residuals[i:i+1,:].T.dot(residuals[i:i+1,:]) for iu
     \rightarrowin range(T)]) * np.eye(N)
                fscore = ((T - N - K) / N) * ((1 + f_bar.dot(np.linalg.inv(omega))).
     \rightarrowdot(f_bar.T))**(-1)) * \
                               (alphas.dot(np.linalg.inv(sigma_hat)).dot(alphas.T))
                fscore = fscore[0][0]
                p = 1-scp.stats.f.cdf(fscore, N, T - N - K) #find p-value of F test
     \hookrightarrow statistic
                print({
                              "p value": p,
                              "f score": fscore,
                              "df1": N,
                              "df2": T-K-N,
                })
                return p, fscore, N, T - N - K
market factor, 25 portfolios
{'p value': 3.3306690738754696e-16, 'f score': 5.687256129620094, 'df1': 25,
```

```
rp-pca factors, 25 portfolios
```

```
[986]: _ = time_series_ap_test(rp_pca_factors_25, portfolio_return_panel)
      {'p value': 6.186828827026147e-12, 'f score': 4.529720391307021, 'df1': 25,
      'df2': 622}
      pca factors, 370 portfolios
[987]: | = time_series_ap_test(pca_factors_370, portfolio370_return_panel)
      {'p value': 8.043448616046334e-07, 'f score': 1.736326068441845, 'df1': 370,
      'df2': 275}
      rp-pca factors, 370 portfolios
[988]: | = time_series_ap_test(rp_pca_factors_370, portfolio370_return_panel)
      {'p value': 0.020416396615084986, 'f score': 1.2619538042259923, 'df1': 370,
      'df2': 275}
      0.0.9 9
[997]: def xs_ap_test(factors, test_assets):
           T, N = test_assets.shape
           _, K = factors.shape
           ones_T = np.ones((T,1))
           loadings = np.linalg.lstsq(np.concatenate([ones_T, factors], axis=1),
                           test_assets, rcond=None)[0]
           a_s = loadings[0:1, :]
           betas = loadings[1:, :]
           print(betas.shape)
           resids = test_assets - np.concatenate([ones_T, factors], axis=1).
        →dot(loadings)
           Sigma = np.eye(N) * np.cov(resids.T)
           Sigma_F = np.cov(factors.T)
           expected_returns = np.mean(test_assets, axis=0)
           ones_N = np.ones((N,1))
           lambdas = np.linalg.lstsq(betas.T, expected_returns, rcond=None)[0]
           alphas = expected_returns.T - betas.T.dot(lambdas)
           in_minus_beta = np.eye(N) - betas.T.dot(np.linalg.inv(betas.dot(betas.T))).
        →dot(betas)
           if factors.shape[1] > 1:
```

```
shanken_correction = 1 + lambdas.T.dot(np.linalg.inv(Sigma_F)).
        →dot(lambdas)
                shanken_correction = 1
          else:
              shanken_correction = 1 + lambdas.T.dot(lambdas) / (Sigma_F)
                shanken correction = 1
          cov_alpha = (1/T) * in_minus_beta.dot(Sigma).dot(in_minus_beta.T) *_u
       ⇒shanken_correction
          score = alphas.T.dot(cov_alpha).dot(alphas)
          p = 1-chi2.cdf(score, N-K) #find p-value
              "p value": p,
              "score": score,
              "df": N-K,
          })
          return p, score, N - K
[998]: from scipy.stats.distributions import chi2
[999]: from linearmodels.asset_pricing.model import LinearFactorModel
[1000]: | lfm = LinearFactorModel(portfolio_return_panel, ff_factor_panel[:,0:1])
       lfm_fit = lfm.fit()
[1001]: lfm_fit
「1001]:
                          LinearFactorModel Estimation Summary
       No. Test Portfolios:
                                        25
                                            R-squared:
                                                                         0.7275
       No. Factors:
                                            J-statistic:
                                                                         115.56
       No. Observations:
                                       650
                                            P-value
                                                                         0.0000
       Date:
                           Wed, Mar 03 2021
                                            Distribution:
                                                                       chi2(24)
                                  20:04:27
       Time:
       Cov. Estimator:
                                    robust
                                Risk Premia Estimates
          ______
                 Parameter Std. Err. T-stat
                                                 P-value
                                                          Lower CI
               ------
                                                            0.2988
                    0.6627
                              0.1857
                                        3.5694
                                                  0.0004
                                                                       1.0266
```

Covariance estimator:
HeteroskedasticCovariance

See full_summary for complete results LinearFactorModelResults, id: 0x1a458afd68

[1002]: LinearFactorModel Estimation Summary

No. Test Portfolios: 25 R-squared: 0.9157

 No. Factors:
 3
 J-statistic:
 94.059

 No. Observations:
 650
 P-value
 0.0000

 Date:
 Wed, Mar 03 2021
 Distribution:
 chi2(22)

Time: 20:04:27 Cov. Estimator: robust

Risk Premia Estimates

Parameter Std Err T-stat P-value Lower CI Upper CI

	Parameter	Sta. Err.	1-stat	P-value	Lower CI	Upper CI
factor.0	0.5046	0.1751	2.8817	0.0040	0.1614	0.8479
factor.1	0.1911	0.1232	1.5504	0.1210	-0.0505	0.4326
factor.2	0.4071	0.1144	3.5593	0.0004	0.1829	0.6313

Covariance estimator:

HeteroskedasticCovariance

See full_summary for complete results

LinearFactorModelResults, id: 0x1a5676b710

market factors, 25 portfolios

```
[1008]: _ = xs_ap_test(ff_factor_panel[:,0:1], portfolio_return_panel)
```

(1, 25)

{'p value': 1.0, 'score': 3.414303463356029e-10, 'df': 24}

ff 3 factors, 25 portfolios

[1009]: _ = xs_ap_test(ff_factor_panel[:,0:3], portfolio_return_panel)

(3, 25)

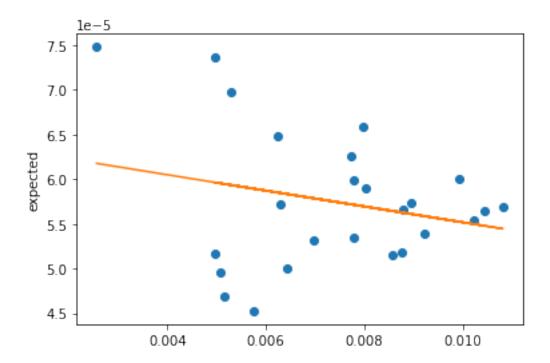
{'p value': 1.0, 'score': 3.101863737637997e-11, 'df': 22}

pca factors, 25 portfolios

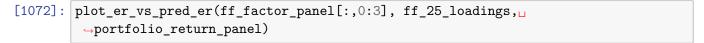
[1010]: _ = xs_ap_test(pca_factors_25, portfolio_return_panel)

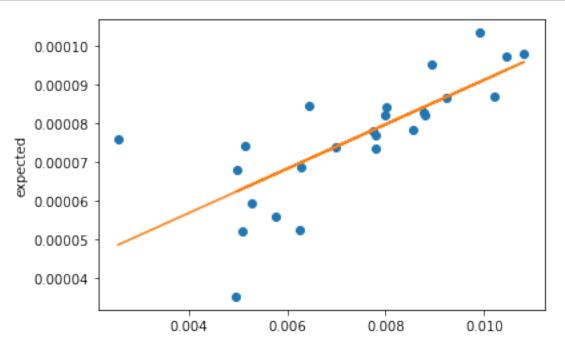
(3, 25)

```
{'p value': 1.0, 'score': 1.990960861796633e-11, 'df': 22}
       rp-pca factors, 25 portfolios
[1011]: = xs_ap_test(rp_pca_factors_25, portfolio_return_panel)
       (3, 25)
       {'p value': 1.0, 'score': 1.935256194220642e-11, 'df': 22}
       pca factors, 370 portfolios
[1012]: _ = xs_ap_test(pca_factors_370, portfolio370_return_panel)
       (5, 370)
       {'p value': 1.0, 'score': 4.2356681111082273e-10, 'df': 365}
       rp-pca factors, 370 portfolios
[1013]: _ = xs_ap_test(rp_pca_factors_370, portfolio370_return_panel)
       (5, 370)
       {'p value': 1.0, 'score': 2.6022219702128646e-10, 'df': 365}
       0.0.10 10
 [857]: mkt_loadings = np.linalg.lstsq(ff_factor_panel[:,0:1], portfolio_return_panel,__
         →rcond=None) [0]
 [858]: ff_25_loadings = np.linalg.lstsq(ff_factor_panel[:,0:3],__
         →portfolio_return_panel, rcond=None)[0]
[1070]: def plot_er_vs_pred_er(factors, loadings, returns):
            expected_returns = np.mean(returns, axis=0)
            mean_predicted_return = np.mean(factors@loadings, axis=0)
            m, b = np.polyfit(expected_returns, mean_predicted_return, 1)
            plt.plot(expected_returns, mean_predicted_return, 'o')
            plt.plot(expected_returns, m*expected_returns + b)
            plt.ylabel("predicted")
            plt.ylabel("expected")
            plt.show()
       market factor, 25 portfolios
[1071]: plot_er_vs_pred_er(ff_factor_panel[:,0:1], mkt_loadings, portfolio_return_panel)
```



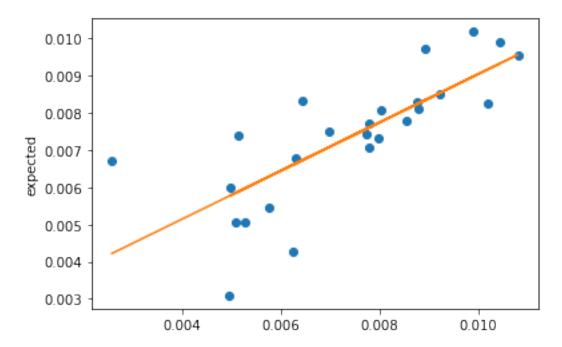
ff 3 factors, 25 portfolios



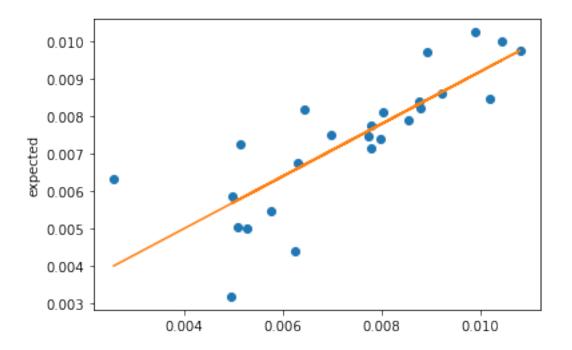


pca factors, 25 portfolios

[1073]: plot_er_vs_pred_er(pca_factors_25, pca_loadings_25, portfolio_return_panel)

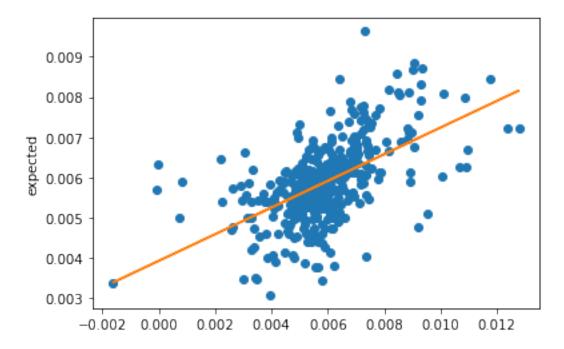


rp-pca factors, 25 portfolios



pca factors, 370 portfolios

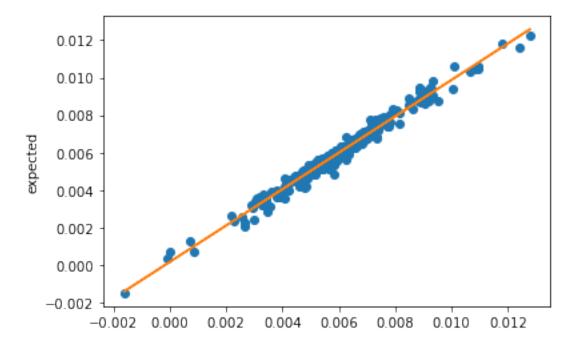
[1076]: plot_er_vs_pred_er(pca_factors_370, pca_loadings_370, portfolio370_return_panel)



rp-pca factors, 370 portfolios

[1077]: plot_er_vs_pred_er(rp_pca_factors_370, rp_pca_loadings_370, ⊔

→portfolio370_return_panel)



0.0.11 11

The results here are largely what we expect rp-pca slightly betas pca in the small K/N setting, however it dominates it in the high dimensional setting. On the 25 portfolio case, we see that the statistical factors are slightly better than the FF french ones, however they are very close. This is by construction, we are forming portfolios based on the stock characteristics from which two of those three factors are derived. #### Part 8 For the 25 portfolios, we saw that the time series alphas were statistically significantly nonzero for all sets of factors. For the 370 portfolios, we saw that while the alphas for the PCA factors statistically significantly nonzero, the alpha for the RP-PCA factors were statistically significantly nonzero at 5 %, but not at 1 % #### Part 9 For this test, we saw that the alphas for the cross sectiontional asset pricing test were not statistically significantly different than zero for any of the sets of factors or test portfolios #### Part 10 For part 10, we see that the average return predicted by the market factor is not at all forming a straight line with the portfolios. This is expected. For the other three sets of factors, we see that they get the trend right, but that there is still a lot of variation around the average predicted return. This confirms our suspicion based on the similarities of the sharpe ratios of the factors that they price the 25 portfolios reasonably similarly. PCA get's the trend right for the average return of the 370 anomaly portfolios, however there is still a lot of variation around that line. RP-PCA is clearly superior in terms of average return vs mean predicted return for the anomaly portfolios, this is in line with the fact that the alphas for the rp-pca factors for the time series regression test were not statistically significant at the 1 % level.

[]: