

# **Submission Packet for com104s1: Zeroth-Order Covariance Matrix Adaptation Evolution Strategy for Single Objective Bound Constrained Numerical Optimization Competition**

## Files Included in this Packet

*Competition Entry:  
Submission (com104s1)*

- Submission form data
- Paper Upload

# Submission Details: com104s1

**Track:** Competition Real Parameter Single Objective Bound Constrained Optimization (4) (**Comp RPSOBCO**)

**Overall Submission Status:** Received

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Latest stage: com104s3 (the "Conference Presentation" stage) [details](#)

## Competition

*Competition:* Competition Real Parameter Single Objective Bound Constrained Optimization

## Title

*Title:*

Zeroth-Order Covariance Matrix Adaptation Evolution Strategy for Single Objective Bound Constrained Numerical Optimization  
Competition

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**Abstract**

*Abstract (Maximum 200 words):*

The paper represents a competition entry for the competition on bound constrained single objective numerical optimization at The Genetic and Evolutionary Computation Conference (GECCO) 2022 by a hybrid algorithm named Zeroth-Order Covariance Matrix Adaptation Evolution Strategy (ZO-CMAES).

**Paper Upload**

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**Poster Presentation**

*Please indicate whether you will be presenting a poster:* Yes

**Edited for Publication**

This is not the program stage. The program stage, Stage 2: Camera-Ready Material, **has not** been approved. [view](#)

# Zeroth-Order Covariance Matrix Adaptation Evolution Strategy for Single Objective Bound Constrained Numerical Optimization Competition

Anonymous

## Abstract

The paper represents a competition entry for the competition on bound constrained single objective numerical optimization at The Genetic and Evolutionary Computation Conference (GECCO) 2022[3] by a hybrid algorithm named Zeroth-Order Covariance Matrix Adaptation Evolution Strategy (ZO-CMAES).

**CCS Concepts:** • Mathematics of computing → Evolutionary algorithms.

**Keywords:** CMAES, Zeroth-Order, CEC 2022

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## 1 Introduction

Zeroth-Order Covariance Matrix Adaptation Evolution Strategy (ZO-CMAES) is a hybrid algorithm, which combines the advantages of Covariance Matrix Adaptation Evolution Strategy (CMAES[1]) and Zeroth-Order Optimization (ZO[4]). CMAES is considered an efficient evolutionary algorithm and used to search global optima of unconstrained optimization problems. The Zero-Order optimization (ZO) mentioned in this article is a general term for a class of algorithms designed using the idea of difference technology. ZO can be used to quickly search for local optima. ZO-CMAES combines the global search capabilities of CMAES with the fast local search capabilities of ZO, it improves the stability of the final result of the optimization process.

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## 2 ZO-CMAES

The ZO-CMAES represents a hybrid algorithm that improves the stability of the original CMAES. ZO is used to generate new candidate local solutions after each iteration of CMAES. At the same time, the partial of local solutions can be used as extended information to calculate mean value and covariance matrix for next iteration of CMAES.

### 2.1 Global Search with CMAES

The capability of global search comes from the original CMAES proposed by Hansen[1]. The improvement of ZO-CMAES is the novel calculation logic of the mean value. Equation 1 shows the calculation the mean value in each generation.

$$m \leftarrow m + c_m \sum_{i=1}^{\mu} w_i (x_{i:\lambda} - m_{old}) \quad (1)$$

where  $m$  denotes the mean value in the current generation.  $c_m$  denotes a hyper-parameter that measures the importance of the previous generation mean value and the current generation mean value.  $w_i$  denotes the importance of each individual.  $\lambda$  denotes the number of individuals in the population.  $x_{i:\lambda}$  denotes sampled value of  $i$ -th individual.  $\mu$  denotes top- $\mu$  individuals.  $m_{old}$  is the mean value of the last generation.

The original update method of mean value  $m$  in CMAES is :  $m \leftarrow m + c_m \sum_{i=1}^{\mu} w_i x_{i:\lambda}$ . As we can see, ZO-CMAES utilizes the mean value from the last iteration, which allows the algorithm to obtain more global information. An interesting idea is that the mean value can also be computed by natural gradients [2, 5], which can be computed by difference technology. This is the second intuitive idea to deeply combine ZO and CMAES.

### 2.2 Local Search with ZO

ZO requires only a small number of iterations to obtain local optimal solutions. Therefore, it can be applied to calculate the search path at the local search stage. The intermediate results of the local search process can be recorded and passed to the CMAES. These intermediate results can provide more local information for CMAES and speed up the convergence speed of CMAES. The main formula of ZO is as follows:

$$\hat{\nabla}_x f(x) = \mathbb{E}_{u \sim p(u)} \left[ \frac{f(x + \epsilon u) - f(x)}{\epsilon} u \right] \quad (2)$$

where  $\epsilon$  is the radius of perturbation.  $p(\mu)$  is the pre-defined distribution of  $\mu$ .  $f(x + \epsilon\mu)$  represents the evaluation value of some points within a determined region of the sampled solution to find gradient information through perturbations and predefined distributions.  $f(x)$  denotes the evaluation value of sampled solution (individual).

Equation 2 describes how to calculate the zero-order gradient. ZO uses zero-order gradient instead of traditional one-order or two-order gradient to find the local optima. Specifically, CMAES generates feasible results during the search process, and these feasible results serve as the initial point of ZO, which can effectively utilize the local search ability of ZO.

### 2.3 Selection of candidate solutions

There are two ways to combine solutions generated by ZO and CMAES, called as ZO-after-CMAES and ZO-in-CMAES.

ZO-after-CMAES means that ZO uses only the solution generated by each CMAES iteration as its initial point. Better solutions can be found earlier in the CMAES iteration. It is a very simple hybrid algorithm idea.

Different from ZO-after-CMAES, in ZO-in-CMAES, solutions generated by ZO affect the next iteration of CMAES by combinational population. The final candidate solutions are selected from the local solutions generated by ZO and the sampled solutions based on the normal distribution generated from the covariance matrix in CMAES. First, ZO-CMAES combines all candidate solutions. Second, it randomly selects a population-sized subset of solutions from the combined candidate solutions as the next generation population. Equation 3 shows the detailed selection process of ZO-in-CMAES.

$$C_{new} = \text{random\_select}(C_{zo} \cup C_{cmaes}, \text{popsize}) \quad (3)$$

where  $C_{zo}$  denotes the set of the local solutions from ZO and  $C_{cmaes}$  denotes the set of global solutions from CMAES.  $\text{popsize}$  is size of the population. Function  $\text{random\_select}(S, a)$  will randomly select  $a$  samples from set  $S$  ( $a \leq |S|$ ).

The implementation of candidate solutions will improve the quality of the local population. By adding small disturbances, the algorithm can converge faster without destroying its global search ability.

## 3 Experiments

This section presents the experimental settings and results of ZO-CMAES. The hyper-parameters affect the results and robustness of the algorithm, especially the global search ability of CMAES is greatly affected by the hyperparameter sigma. The size of the population also has a big impact on the algorithm, both in terms of speed and results.

The values of the control parameters for ZO-CMAES were following: sigma=50, size of size of population ( $\text{popsize\_factor} \times \text{popsize} = 10 \times 11$ ), number of iterations of ZO ( $\text{num\_zo}$ )=10,

**Table 1.** Experimental results on 10 D problems

FID	Best	Worst	Median	Mean	Std
1	9.50e-11	7.25e-06	9.06e-08	7.86e-07	1.49e-06
2	3.21e-10	8.92e+00	1.99e+00	3.31e+00	3.74e+00
3	1.16e-08	4.74e+01	2.55e-08	2.32e+00	8.73e+00
4	1.47e-09	4.97e+00	1.99e+00	2.12e+00	1.38e+00
5	7.76e-11	6.61e-10	3.14e-10	3.31e-10	1.52e-10
6	1.30e-01	7.83e+02	1.78e+00	3.00e+01	1.40e+02
7	9.43e-09	2.50e+01	1.80e+00	9.39e+00	1.00e+01
8	3.50e-01	2.15e+01	2.07e+01	1.61e+01	8.45e+00
9	2.29e+02	2.29e+02	2.29e+02	2.29e+02	1.19e-04
10	1.00e+02	2.55e+02	1.01e+02	1.28e+02	5.53e+01
11	1.50e-08	3.00e+02	2.27e-08	1.00e+01	5.39e+01
12	1.63e+02	1.65e+02	1.63e+02	1.64e+02	5.51e-01

The seed is set as a list from 1 to 30 to generate random properties for evaluation of the stability of the algorithm.

## 4 Results

Due to the space limitation, we only list the best value, worst value, median value, mean value and standard deviation of 12 functions on 10 D problems at this version of paper. (see Table. 1). The detailed experimental results will be updated on a online supplementary material in the future.

From these results, we can see that ZO-CMAES can reach the near-optimal solutions (error value smaller than  $1e-8$ ) in function 1, 2, 4, and 7 and obtain a relatively good standard deviation in the mean time. In a nutshell, ZO-CMAES combine the global search (from CMAES) and local search (from ZO), which makes it possible to achieve a good performance on the given 12 test functions.

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