

## MN-P1-ExParcial-2Q-21-22

### 1. Question 1

Given the differential equation  $-\frac{d}{dx} \left( (x+1) \frac{du}{dx} \right) + 3u = ax$ ,  $0 < x < 1$ , with boundary conditions  $u(0) = \alpha$  and  $u'(1) = 1.0$ , use the FEM approach with  $N = 100$  linear elements of the same length to compute:

(a) For  $a = -1$ ,  $\alpha = 2.0$ , the minimum of the nodal solution  $\{U_i\}_{i=1,\dots,N+1}$

- 1.3078e+00 ✓
- 1.3517e+00 (−25%)
- 1.2618e+00 (−25%)
- 1.3935e+00 (−25%)
- None of the given the answers (−25%)
- Blank (no penalty)

Hint. For The same value  $\alpha = 2.0$ , but fixing  $a = 0$ , the minimum of the nodal solution is  $\min_{i=1,\dots,N+1} U_i = 1.4115e+00$ .

(b) For  $a = -1$  and the same value of  $\alpha$ ,  $\alpha = 2.0$ , the interpolated value of  $u$  at the point  $x = 0.337$  using the values of  $u$  at nodes of the element to which it belongs

- 1.4126e+00 ✓
- 1.4383e+00 (−25%)
- 1.3870e+00 (−25%)
- 1.4639e+00 (−25%)
- None of the given the answers (−25%)
- Blank (no penalty)

(c) For  $a = -1$ , the value of  $\alpha$  such that the solution at node 27 minus the solution at node 70 twice the solution node 52

- -1.0392e+00 ✓
- -1.1741e+00 (−25%)
- -9.0436e-01 (−25%)
- -1.3089e+00 (−25%)
- None of the given the answers (−25%)
- Blank (no penalty)