

Name and surnames:

- (4) Consider the domain  $\Omega$  defined by the mesh file **meshAleta2DQuad.m**. We want to study the thermal problem with two essential BC and two convection BC defined as:

$$\left\{ \begin{array}{l} -\frac{\partial}{\partial x} \left( k_c \frac{\partial T}{\partial x} \right) - \frac{\partial}{\partial y} \left( k_c \frac{\partial T}{\partial y} \right) = f(x, y), \quad (x, y) \in \Omega, \\ T(0, y) = 100, \\ T(5, y) = 200, \\ q_n(x, 0) = -3(T(x, 0) - 10), \\ q_n(x, y) = -2(T(x, y) - 20), \quad 0 \leq x \leq 5, \quad 5y - 2x - 10 = 0 \end{array} \right.$$

Take  $k_c = 0.7$  and  $f(x, y) \equiv 0$  on  $\Omega$  and compute the solution of the problem obtained by the finite element method.

- (a) Compute the minimum temperature achieved at the nodes and the coordinates  $(x, y)$  of the node with minimum temperature:

min Temperature =	1.7272e+01
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node coordinates =	2	0
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(Hint: The temperature at node 156 is: 8.4115e+01)

- (b) Using the point  $p = [2.3, 2.2]$ , find the number of the element to which  $p$  belongs, its second barycentric coordinate and the interpolated temperature  $T_p$  of the point  $p$

Element number =	93
$\alpha_2 =$	3.7260e-01
$T_p =$	4.5242e+01

- (c) The number of nodes whose temperature differs from  $T_p$  by less than 5 degrees.

Number of Nodes:	45
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(Hint: The number of points for a difference of 2 degrees is: 19)

(2.5 points)