

(3) Consider the following differential equation

$$-\frac{d}{dx}(3x^2 \frac{du}{dx}) + 2u + 3 = 0$$

defined for  $x \in [2, 5]$  and with boundary conditions  $u(2) = 3, u(5) = 8$ . Applying the Finite Element Method with 200 **linear finite elements** of equal length:

(a) Compute the assembled stiff matrix and write the element  $K(50,50)$ :

$K(50,50)=$	2.9921e+03
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**Hint1:** We know that  $K(20,21) = -1.0511e + 03$

**Hint2:** You can use that the stiff matrix associated to a term  $a_1(x) = ax^2$  is

$$K^{k,1} = \frac{a}{3h_k^2}(x_{i+1}^3 - x_i^3) \begin{pmatrix} 1 & -1 \\ -1 & 1 \end{pmatrix}$$

(b) Compute *meanValue*, the mean of the values of  $u$  obtained, and compute  $N$ , the number of nodes for which the value of  $u$  fulfills  $|u - \text{meanValue}| < 0.1$ :

<i>meanValue</i> =	5.9182e+00
$N =$	9

( **Hint:** We know that  $u(25)=3.9730e+00$ )

(3 points)