# DYNAMIC MODELING AND CARACTERIZATION OF A HEXAPOD CRAWLING ROBOT

M. Mazzanti, J. R. Reynal, P. De Cristóforis, F. Pessacg.

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ICC-Conicet Universidad de Buenos Aires Laboratorio de Robótica y Sistemas Embebidos - DC

# INTRODUCTION - HEXAPOD ROBOT

- · Multi-legged robots vs wheeled platforms.
- · Cost: large number of degrees of freedom (DoF).



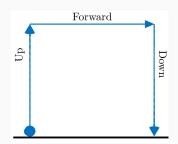
Phantom AX

- Foot-strike detection without using additional sensors → minimalistic approach.
- How can we achieve that using only the position feedback from the servomotors?



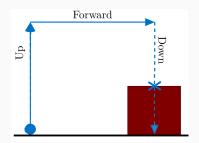
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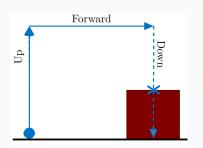


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## We need a dynamic model to:

- · Estimate the error between the goal and the measured position.
- Compensate external forces→ the locomotion can be adapted to the traversing terrain.

# DYNAMIXEL AX-12 SERVOMOTOR

- · P control in position.
- · Limited communication.
- · No torque measurements.



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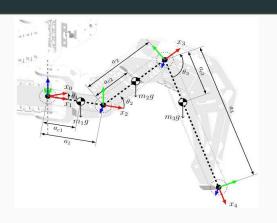


#### Electromechanical model:

$$J^{M}\ddot{\theta}^{M} + B\dot{\theta}^{M} + F^{M}(\dot{\theta}^{M}) + R\tau = K^{M}V$$

#### Euler-Lagrange formalism:

$$au = rac{\mathrm{d}}{\mathrm{d}t} \left( rac{\partial \mathcal{L}}{\partial \dot{m{ heta}}} 
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Euler-Lagrange formalism:

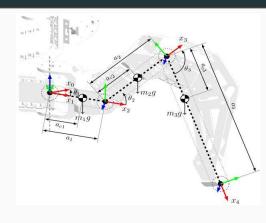
$$\boldsymbol{\tau} = \frac{\mathrm{d}}{\mathrm{d}t} \left( \frac{\partial \mathcal{L}}{\partial \dot{\boldsymbol{\theta}}} \right) - \frac{\partial \mathcal{L}}{\partial \boldsymbol{\theta}}$$

which can be written in matrix form:

$$D( heta)\ddot{ heta} + C( heta,\dot{ heta})\dot{ heta} + G( heta) = au$$

where the inertia matrix D:

$$D(\boldsymbol{\theta}) = \sum_{i=1}^{n} \left[ m_i J_{v_i}^{\mathsf{T}} J_{v_i} + J_{w_i}^{\mathsf{T}} {}^{\mathsf{O}} R_i I_i {}^{\mathsf{O}} R_i^{\mathsf{T}} J_{w_i} \right]$$



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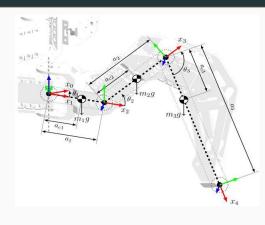
where the  $inertia\ matrix\ D$ :

$$D(\boldsymbol{\theta}) = \sum_{i=1}^{n} \left[ m_i J_{v_i}^{\mathsf{T}} J_{v_i} + \left[ J_{w_i}^{\mathsf{T}} {}^{\mathsf{Q}} R_i I_i^{\mathsf{Q}} R_i^{\mathsf{T}} J_{w_i} \right] \right]$$

$$:= D_{\mathbf{w}}$$

where  $D_w$  in the RR case is:

$$\begin{bmatrix} I_{2_{33}} + I_{3_{33}} & I_{3_{33}} \\ I_{3_{33}} & I_{3_{33}} \end{bmatrix}$$



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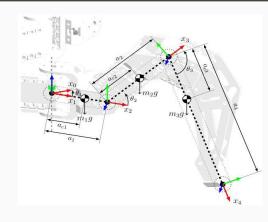
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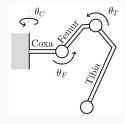
With coxa joint,  $D_w$  is:

$$\begin{bmatrix} I_{1_{33}} + I_{2_{33}}\cos^2(\theta_2) + I_{3_{33}}\cos^2(\theta_2 + \theta_3) \\ 0 \\ 0 \end{bmatrix}$$



$$\begin{bmatrix} 0 & 0 \\ I_{2_{33}} + I_{3_{33}} & I_{3_{33}} \\ I_{3_{33}} & I_{3_{33}} \end{bmatrix}$$

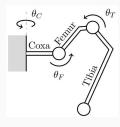
## COMBINING ACTUATOR AND LEG DYNAMICS



Leg Dynamical model:

$$D( heta)\ddot{ heta} + C( heta,\dot{ heta})\dot{ heta} + G( heta) = au$$

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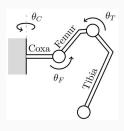
$$D( heta)\ddot{ heta} + C( heta,\dot{ heta})\dot{ heta} + G( heta) = au$$



Electromechanical model:

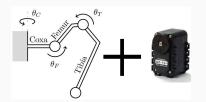
$$J^{M}\ddot{\boldsymbol{\theta}}^{M}+B\dot{\boldsymbol{\theta}}^{M}+F^{M}(\dot{\boldsymbol{\theta}}^{M})+R\boldsymbol{ au}=K^{M}V$$

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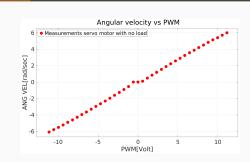
Complete dynamic model of a leg:

$$D'(\theta)\ddot{\theta} + C'(\theta)\dot{\theta} + F_{fric}(\dot{\theta}) + G'(\theta) = K'V$$

# CHARACTERIZATION OF SERVOMOTOR AND DYNAMIC MODEL

#### Servomotors characterization

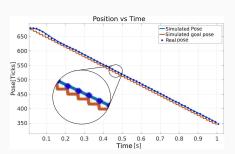
 Linear relationship between applied voltage and meassured velocity.

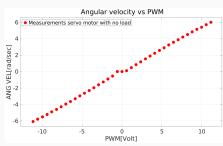


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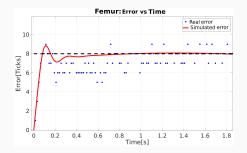




# Complete behaviour simulation:

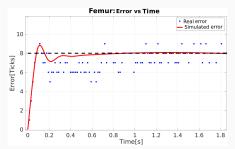
- · Full dynamic model
- · Interpolation
- · P control

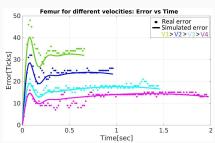
# **TRESHOLD**



Threshold offset established with mean value of simulation.

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Threshold offset established with mean value of simulation.

Different Thresholds for different velocities.

Adaptive gait from the Dynamic model.

# **EXAMPLES OF THRESHOLD**

#### Overestimated threshold



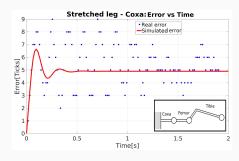
#### Precise threshold

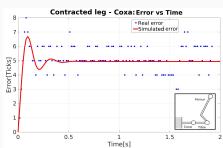


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#### **ERROR ANALYSIS IN COXA MEASUREMENTS**





- · Vibrations in the leg, not considered in our simulation.
- · Bigger Treshold error.

- · Less inertia moment implies less vibration.
- Future improvement: trapezoidal acceleration and a PID controler.

# **CONCLUTIONS AND FUTURE WORK**

## Challenge

- · Improve comunication with servo motor  $\rightarrow$  reducing reading delay.
- · Trapezoidal aceleration profile.
- · Add PID control.

#### Conclutions

- · Characterization of servo motor.
- · Implementation and simulation of leg dynamics.
- $\cdot$  Tresholds were determined using the dynamic model  $\to$  capability of traversing irregular terrains.

#### Thank you!



Questions?