Racecar 101

James Wright

September 8, 2022

Outline

- What makes a car fast?
- Vehicle Basics
- Vehicle Balance and Control
- 4 Three Tenants of Racecar Design

Note

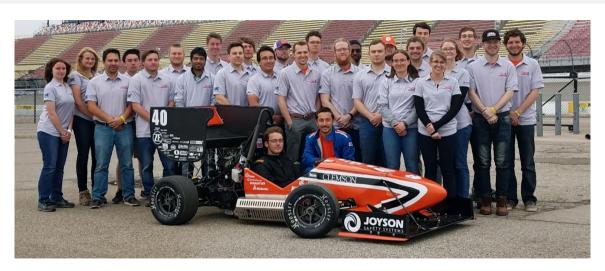
This first part is a very simplified breakdown

- It's not the most accurate
- It's not to insult anyone's intelligence

It's simply to not distract from the things that can be easily forgotten or muddied.

Also, I like audience participation. Ask questions. I'll be asking y'all questions.

Me



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$$Time = \frac{Distance}{Velocity}$$

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¹Assuming distance is constant

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• To lower time, we need to increase velocity¹

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To make a car faster, you must make the car accelerate more

¹Assuming distance is constant

What famous equation involves acceleration?

What famous equation involves acceleration?

Newton's 2nd law!

$$F=ma$$

What famous equation involves acceleration?

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$$F = ma$$

We care about acceleration, so rearange:

$$a = \frac{F}{n}$$

$$a = \frac{F}{m}$$

Decrease Mass

Make things lighter

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Decrease Mass

Make things lighter

Increase Force

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- Increase the force the tires can apply to the ground
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- Increase power output
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The latter two hold only if the tires can transfer the torque

Sometimes \uparrow mass $+ \uparrow$ force $= \uparrow$ acceleration

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Bigger Engine

Increases the total vehicle mass, but increases power output Depending on the ratio, can lead to better acceleration.

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Sometimes \downarrow mass $+ \downarrow$ force $= \uparrow$ acceleration

Smaller/Narrower Tires

Decreases total vehicle mass, but decreases total acceleration potential

Also reduces unsprung mass (improves vehicle handling and response)

Simplest acceleration to model:

$$a = \frac{F}{m}$$

Tire traction capacity sets upper limit of the acceleration.

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- Ensure that car is capable of absolute maximum braking acceleration

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Tire traction capacity sets upper limit of the acceleration.

Divided into 2 components:

Braking (negative)

- This is as much for safety as it is performance
- Ensure that car is capable of absolute maximum braking acceleration
- Power (positive)
 - Almost always limited by the power unit (ICE, electric motor, rubber band windup, etc.)

Lateral Acceleration

Turning causes Lateral Acceleration, which is not a change in speed, but of direction:

$$a_{\text{lat}} = \frac{V^2}{r}$$

where V is velocity, and r is the turning radius.

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Therefore given:

- \bullet a force, F (tire traction)
- \bullet a mass, m (the car)
- \bullet and a radius, r (the track/racing line)

there is a limit to the maximum velocity

How do we maximize the velocity? $V=\sqrt{\frac{Fr}{m}}$

lacktriangle Decrease mass m

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 - Add lightness
 - Has compounding affect due to load transfer (discussed later)

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 - How?

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- $oldsymbol{o}$ Increase force F
 - Increase the maximum force the tires can exert
 - How?
 - Aero downforce
 - Different tires
 - Suspension design, etc....

Quick Review

Higher Acceleration = Faster Car

	Limited by	How to make better?
Longitudinal	Force (Braking and Power)	Bigger Engine/Brakes
Acceleration	Mass	Reduce it
Lateral	Force (Tire Traction)	Increase Grip
Acceleration	Mass	Reduce it

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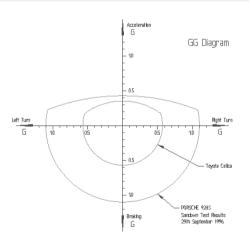


Figure 2

What about lateral and longitudinal acceleration at the same time? Answer: look at a G-G curve for the car

G-G Curve (or Traction Circle)

 Plots maximum steady-state acceleration that a vehicle can have in any direction

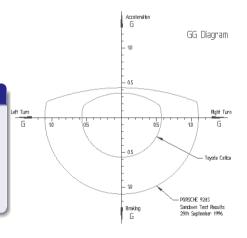


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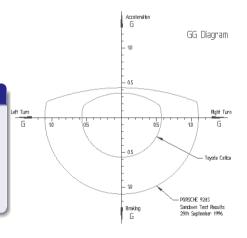


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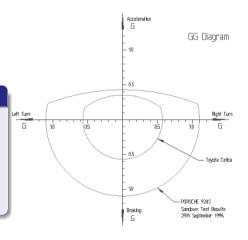


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- On the circle = driving at the edge

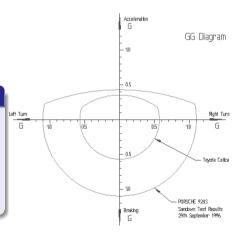


Figure 2

Circles

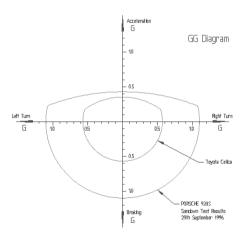


Figure 2

- Circles
 - Shape of the curve is circular, due to tires

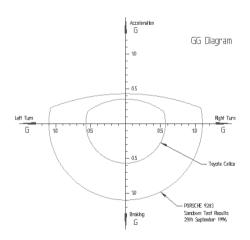


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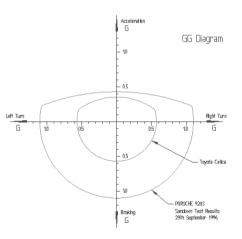


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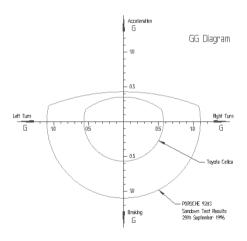


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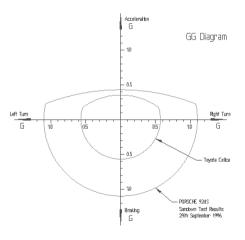


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Circles

- Shape of the curve is circular, due to tires
- Tires can be assumed to have a maximum force vector which can be applied in any direction
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 - Top part of curve isn't quite circular
 - Positive acceleration is nearly always limited by the power unit, not the tires
 - For (nearly) all cars, the power unit is the most severe acceleration limitation

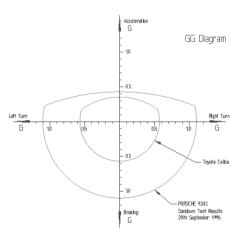


Figure 2

How do tires generate force?

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Via friction with the ground

Tires and Friction

Newton's Law of Friction

$$F = N\mu$$

where F is the max static friction force, N is the normal force, and μ is the static friction coefficient

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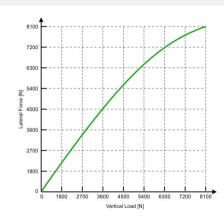
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- Tires create force via static friction
 - A tire is in kinetic friction if it's locked up or doing a burnout
- ullet μ is generally assumed to be constant
 - ullet So F is linearly dependent on N

• Tires **do not** have a constant μ :

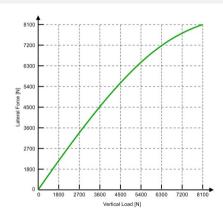
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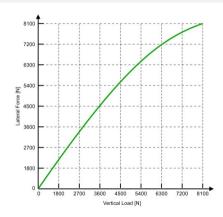
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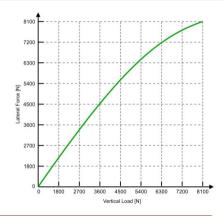
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Load Sensitivity is the singular most impactful thing in racecar design

It alters practically every single decision

Load Transfer

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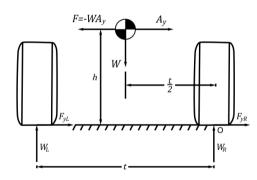
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Load Transfer

• Weight of vehicle shifting due to acceleration

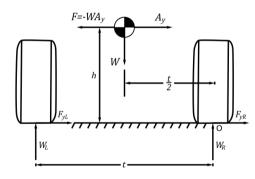
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Load Transfer

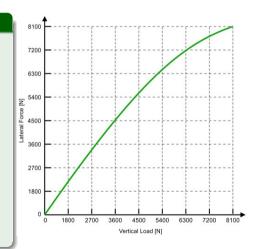
- Weight of vehicle shifting due to acceleration
- Caused by torque of tires against CG, not by body roll
- Reduces global vehicle grip due to load sensitivity



Load Transfer Example

No load transfer vs 50% load transfer

Assume 4.5kN of static vertical load on each tire.



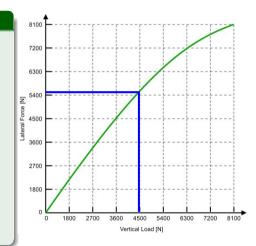
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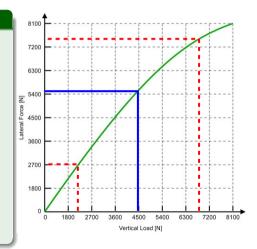
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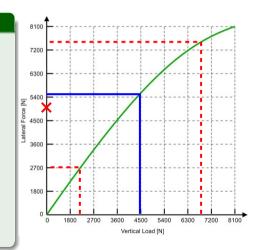
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8% Drop in total traction!

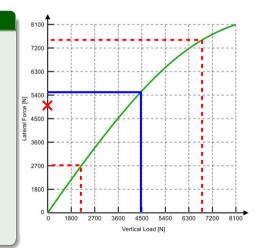


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- Change in position
 - The path the car takes on track
 - Governed by Conservation of (linear) Momentum (F = ma)

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- Previous topics primarily cover vehicle dynamics for translation
- Now we'll cover orientation/rotation

Angular Momentum

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	Linear	Angular
External Action	F	M
Object's resistance to change	m	I
Rate of Change	a	α
State Variable	V	ω

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ullet Moments can be calculated from a force F and distance r via $M=F\times r$

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This is where balance and control comes into play

Ensure that the car is oriented such that we can achieve maximum linear acceleration

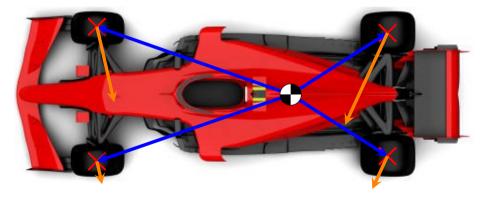
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Vehicle Balance

Why do Formula 1 and Indy cars have larger tires at the rear than the front?

Vehicle Balance - Formula 1 Car

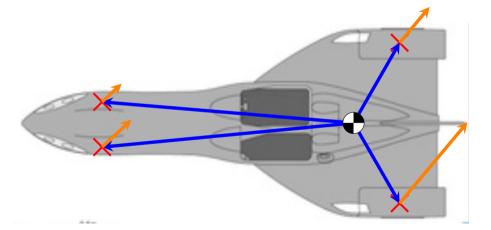
Balance the moments of the car $M = F \times r$



Vehicle Balance - Delta Wing

Balance the moments of the car $M = F \times r$

$$M = F \times r$$



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Neutral Steer

Moments in perfect imbalance

Neutral Steer

Moments in perfect imbalance

Under Steer

Unbalanced moments cause under-rotation

Neutral Steer

Moments in perfect imbalance

Under Steer

Unbalanced moments cause under-rotation

Over Steer

Unbalanced moments cause over-rotation

Neutral Steer

Moments in perfect imbalance

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• The latter two prevent achieving maximum linear acceleration

Neutral Steer

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- The latter two prevent achieving maximum linear acceleration
- A car can dynamically change between all three states

Neutral Steer

Moments in perfect imbalance

Under Steer

Unbalanced moments cause under-rotation

Over Steer

Unbalanced moments cause over-rotation

- The latter two prevent achieving maximum linear acceleration
- A car can dynamically change between all three states
- Changes occur due to differences in load transfer, suspension magic, and through dynamic movement

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- Make it Lighter
 - Improves acceleration, load transfer, responsiveness, etc.

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- Make it more Central
 - Reduces $I \Rightarrow$ makes the car more responsive

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- Make it Lower
 - Lowering a component lowers CG ⇒ reduces load transfer
- Make it more Central
 - Reduces $I \Rightarrow$ makes the car more responsive

The car that is lighter, has a lower CG, or has a lower inertia will be faster

Recommended Resources

- Tune to Win by Carroll Smith
 - Vehicle dynamics for normal people
 - Covers the gamut of racecar design topics (aero, cooling, VD, powertrain, etc.)
- Racecar Vehicle Dynamics by Milliken & Milliken
 - "The Bible"
 - It's a textbook, but incredibly useful
 - More specialized to vehicle dynamics (shocking given the name)

Questions