Racecar 101

James Wright

September 8, 2022

Outline

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Note

This first part is a very simplified breakdown

- It's not the most accurate
- It's not to insult anyone's intelligence

It's simply to not distract from the things that can be easily forgotten or muddied.

What makes a car go fast?

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To make a car **faster**, you must make the car **accelerate more**

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What famous equation involves acceleration?

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Newton's 2nd law!

$$F = ma$$

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We care about acceleration, so rearange:

$$a = \frac{F}{m}$$

How do we maximize acceleration?

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Decrease Mass

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The latter two hold **only if the tires can transfer the torque**

Balancing ↑Force vs ↓Mass

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Bigger Engine

Increases the total vehicle mass, but increases power output
Depending on the ratio, can lead to better acceleration.

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Smaller/Narrower Tires

Decreases total vehicle mass, but decreases total acceleration potential
Also reduces unsprung mass (improves vehicle handling and response)

Longitudinal Acceleration

Simplest acceleration to model:

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Tire traction capacity sets upper limit of the acceleration.

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- Ensure that car is capable of absolute maximum braking acceleration

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2. Power (positive)
   - Almost always limited by the power unit (ICE, electric motor, rubber band windup, etc.)

Lateral Acceleration

Turning causes *Lateral Acceleration*, which is not a change in speed, but of direction:

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Therefore given:

- a force, F (tire traction)
- a mass, m (the car)
- and a radius, r (the track/racing line)

there is a **limit to the maximum velocity**

Lateral Acceleration cont.

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   - How?

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   - Increase the maximum force the tires can exert
   - How?
     - Aero downforce
     - Different tires
     - Suspension design, etc....

Quick Review

Higher Acceleration = Faster Car

	Limited by	How to make better?
Longitudinal Acceleration	Force (Braking and Power)	Bigger Engine/Brakes
	Mass	Reduce it
Lateral Acceleration	Force (Tire Traction)	Increase Grip
	Mass	Reduce it

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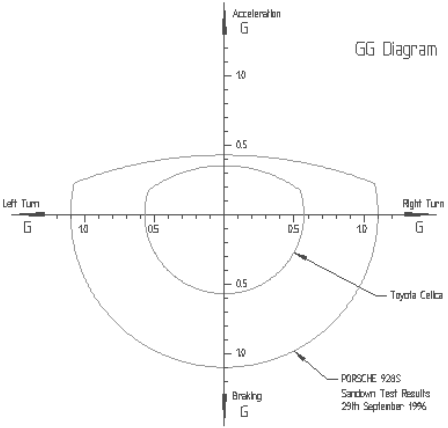

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G-G Curve

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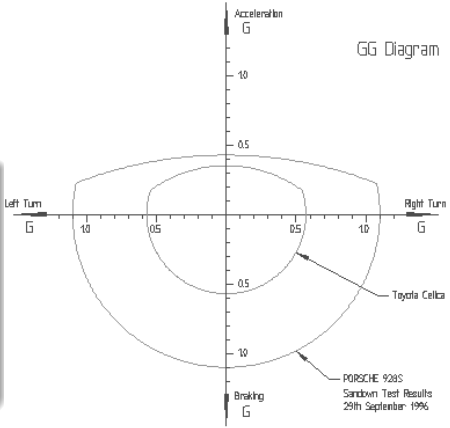
G-G Curve (or Traction Circle)

- Plots **maximum steady-state acceleration** that a vehicle can have in **any direction**



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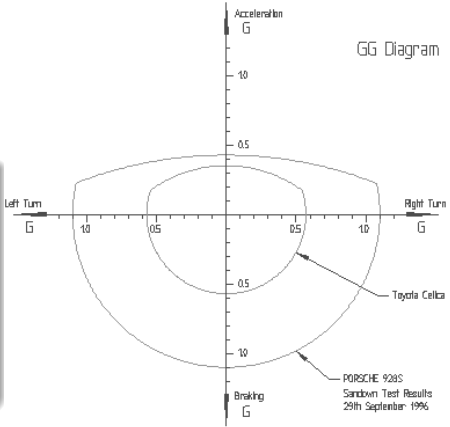

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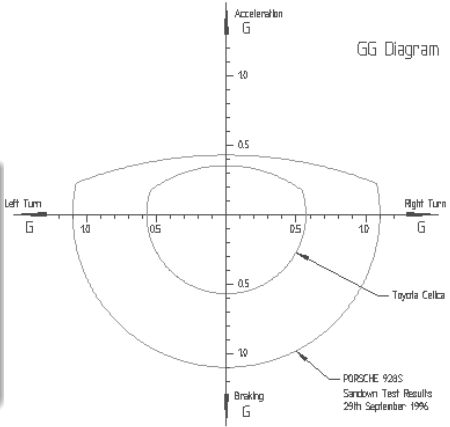

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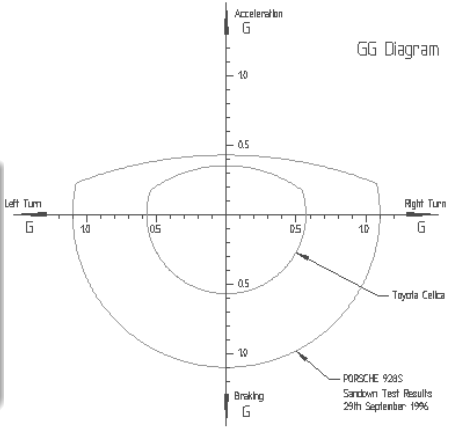

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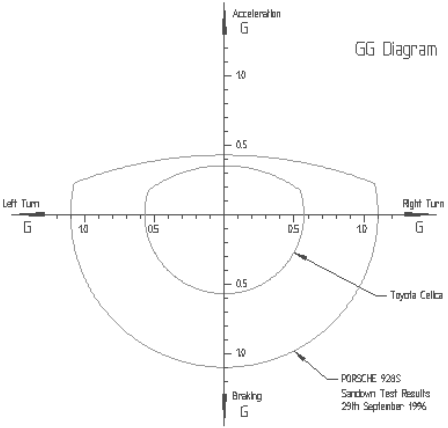
G-G Curve: Misc Remarks

- Circles



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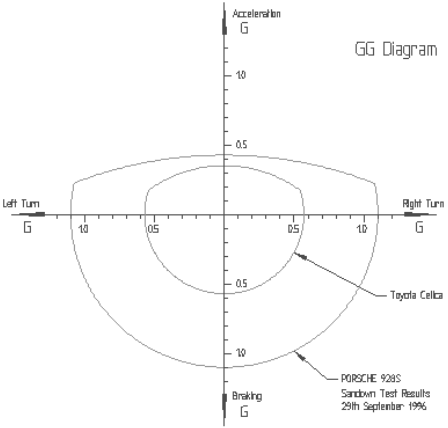

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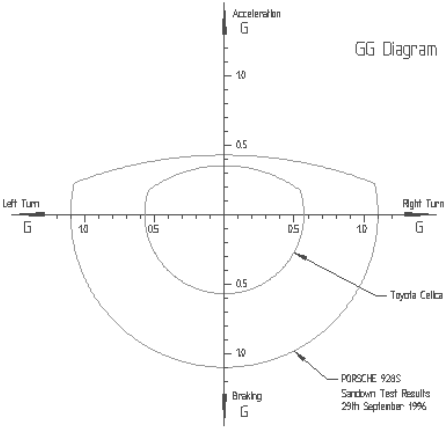

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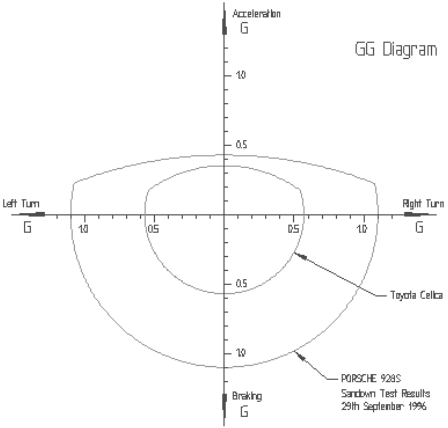

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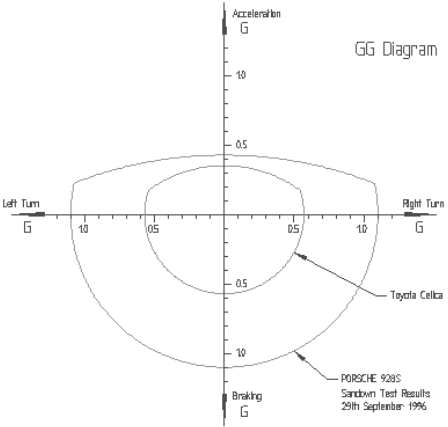

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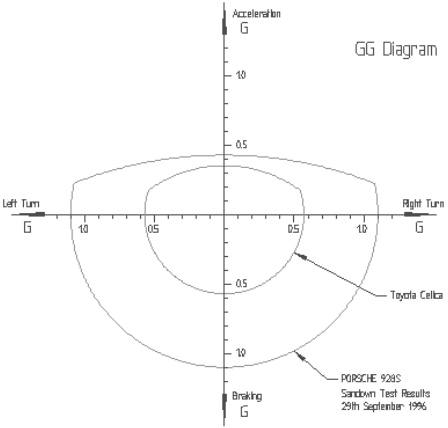
  - **Positive acceleration is nearly always limited by the power unit, not the tires**
  - For (nearly) all cars, the power unit is the most severe acceleration limitation.



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How do tires generate force?

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Via friction with the ground

Tires and Friction

Newton's Law of Friction

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where F is the max static friction force, N is the normal force, and μ is the static friction coefficient

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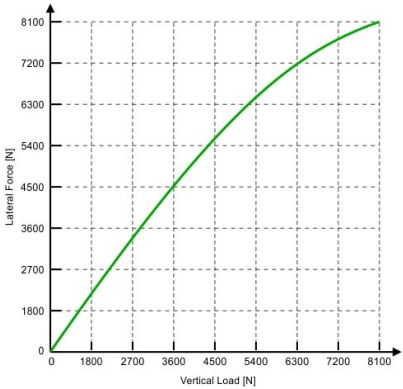
  - A tire is in *kinetic* friction if it's locked up or doing a burnout
- μ is generally assumed to be constant
  - So F is linearly dependent on N

Tires and Load Sensitivity

- Tires **do not** have a constant μ:

$$F = N\mu(N)$$



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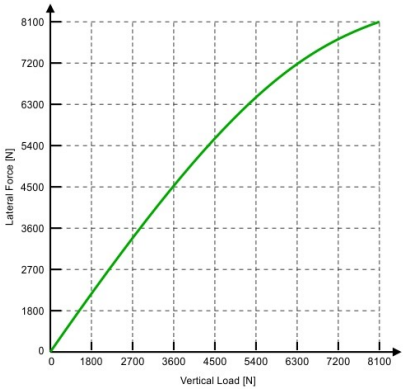

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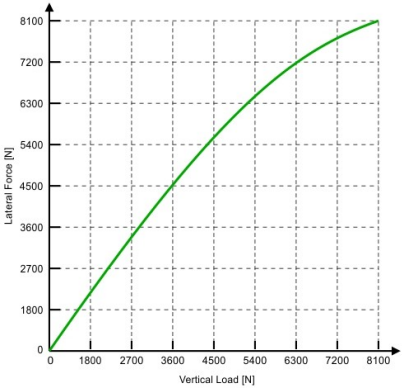

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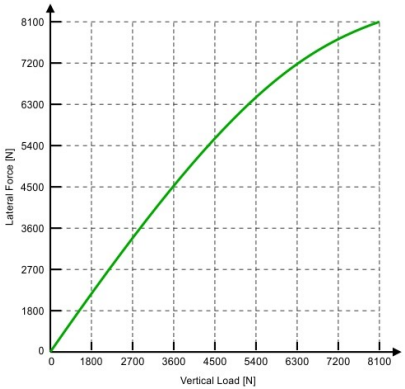

Load Sensitivity is the singular most impactful thing in racecar design

It alters practically every single decision

Load Transfer

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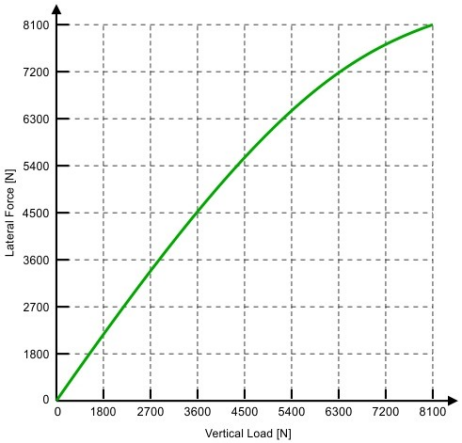
- **Reduces global vehicle grip due to load sensitivity**

Load Transfer Example

No load transfer vs 50% load transfer

Assume 4.5kN of static vertical load on each tire.



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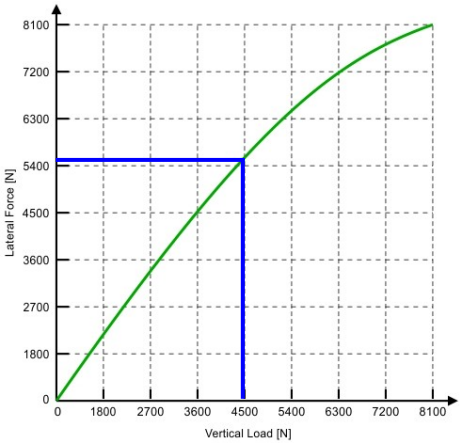

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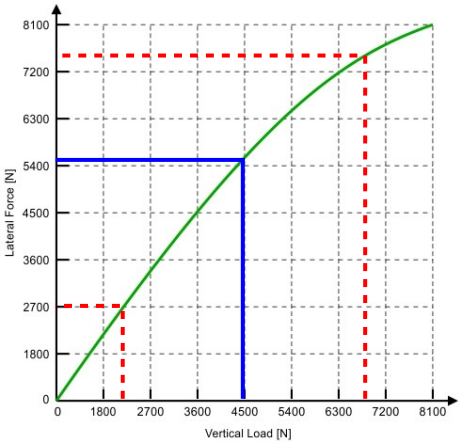

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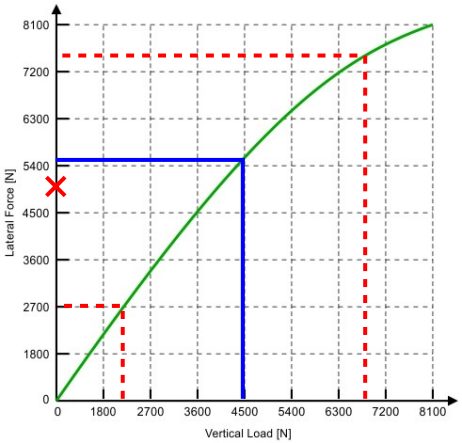

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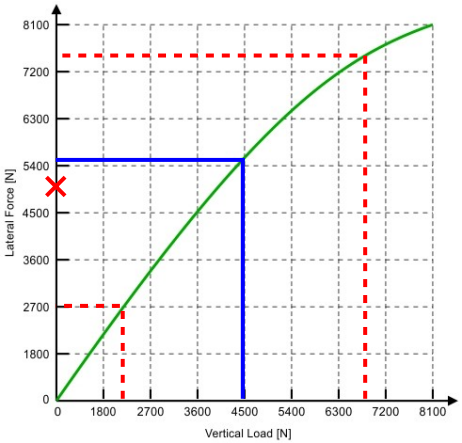
8% Drop in total traction!



Three Tenants of Racecar Building

In order of importance:

1. Make it Lighter
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3. Make it more Central
   - When turning, car has to physically rotate:

$$T = I\alpha$$

     where T is torque, I is rotational inertia, and α is angular acceleration
   - Reducing inertia is similar to reducing mass

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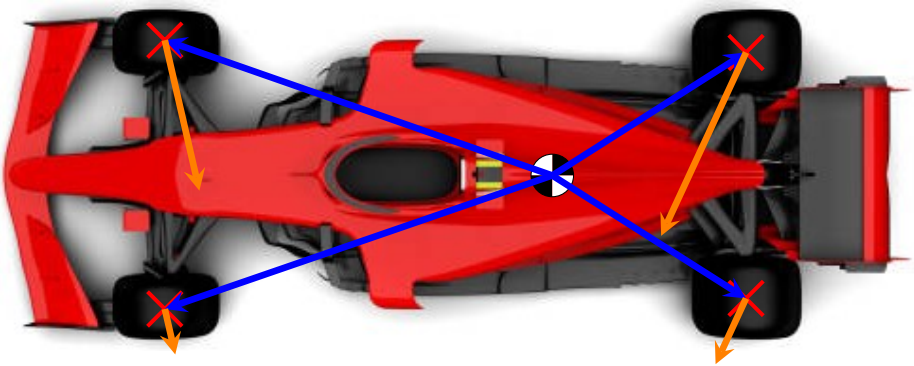
The car that is lighter, has a lower CG, or has a lower inertia will be faster

Vehicle Balance

Why do Formula 1 and Indy cars have larger tires at the rear than the front?

Vehicle Balance - Formula 1 Car

Balance the moments of the car $M = F \times r$



Vehicle Balance - Delta Wing

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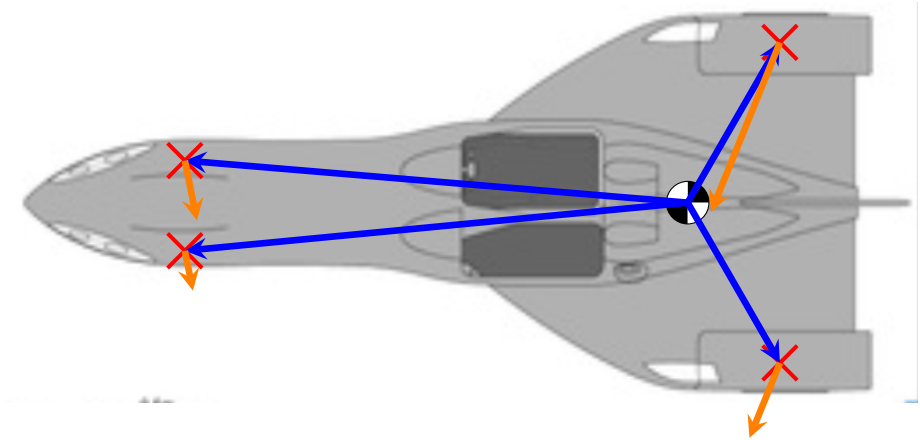

Oversteer vs Understeer

Neutral Steer

Moments balance out

Oversteer vs Understeer

Neutral Steer

Moments balance out

Under Steer

Unbalance moments cause under-rotation

Oversteer vs Understeer

Neutral Steer

Moments balance out

Under Steer

Unbalance moments cause under-rotation

Over Steer

Unbalance moments cause over-rotation

Oversteer vs Understeer

Neutral Steer

Moments balance out

Under Steer

Unbalance moments cause under-rotation

Over Steer

Unbalance moments cause over-rotation

- A car can dynamically change between all three states

Oversteer vs Understeer

Neutral Steer

Moments balance out

Under Steer

Unbalance moments cause under-rotation

Over Steer

Unbalance moments cause over-rotation

- A car can dynamically change between all three states
- Changes occur due to differences in load transfer, suspension magic, and through dynamic movement

Questions