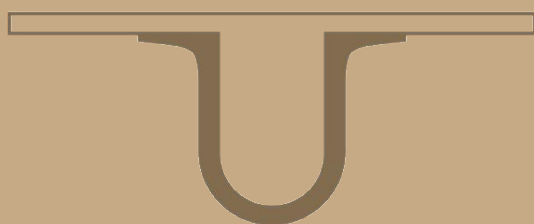# UNIVERSIDADE Ð COIMBRA

Nome Completo do Autor

TÍTULO DO PROJETO DE INVESTIGAÇÃO
SUBTÍTULO (SE EXISTIR)

Projeto de Investigação em XXXXXX no âmbito do Mestrado em Matemática orientada pelo/a Professor/a Doutor/a XXXXXX.

Mês de 20XX

Title of MSc Seminar

Author's Name

Master in Mathematics

Mestrado em Matemática

MSc Research Project in Pure Mathematics

Projeto de Investigação em Matemática Pura

January 2019 / Janeiro 2019

Acknowledgements

I would like to acknowledge ... (Never more than one page)

Abstract

If the Dissertation is in Portuguese, do not write here anything. This is where you write your abstract in English.

Resumo

Aqui escreve o Resumo em Português no caso da dissertação usar o Inglês.

Table of contents

List of figures

List of tables

Chapter 1

Introduction

1.1 First section of the first chapter

And now I begin my first chapter here . . .

And now to cite some people Ancey et al. [1], Read [2]

How to index a name:

A *LaTeX class file* is a file, which holds style information for a particular LaTeX.

How to start a list of Nomenclature and Notation (OPTIONAL): ...

1.1.1 First subsection in the first section

. . . and some more

1.1.2 Second subsection in the first section

. . . and some more . . .

First subsub section in the second subsection

. . . and some more in the first subsub section otherwise it all looks the same doesn't it? well we can add some text to it . . .

1.1.3 Third subsection in the first section

. . . and some more . . .

First subsub section in the third subsection

. . . and some more in the first subsub section otherwise it all looks the same doesn't it? well we can add some text to it and some more and some more and some more and some more and some more and some more and some more . . .

Second subsub section in the third subsection

. . . and some more in the first subsub section otherwise it all looks the same doesn't it? well we can add some text to it . . .

1.2   Second section of the first chapter

and here I write more . . .

1.3   The layout of formal tables

This section has been modified from "Publication quality tables in LATEX*" by Simon Fear.

The layout of a table has been established over centuries of experience and should only be altered in extraordinary circumstances.

When formatting a table, remember two simple guidelines at all times (see Table 1.4):

1. Never, ever use vertical rules (lines).

2. Never use double rules.

These guidelines may seem extreme but I have never found a good argument in favour of breaking them. For example, if you feel that the information in the left half of a table is so different from that on the right that it needs to be separated by a vertical line, then you should use two tables instead. Not everyone follows the second guideline:

There are three further guidelines worth mentioning here as they are generally not known outside the circle of professional typesetters and subeditors:

3. Put the units in the column heading (not in the body of the table).

4. Always precede a decimal point by a digit; thus 0.1 *not* just .1.

5. Do not use 'ditto' signs or any other such convention to repeat a previous value. In many circumstances a blank will serve just as well. If it won't, then repeat the value.

A frequently seen mistake is to use '\begin{center}' . . . '\end{center}' inside a figure or table environment. This center environment can cause additional vertical space. If you want to avoid that just use '\centering'

These guidelines may seem extreme but I have never found a good argument in favour of breaking them. For example, if you feel that the information in the left half of a table is so different from that on the right that it needs to be separated by a vertical line, then you should use two tables instead. Not everyone follows the second guideline:

There are three further guidelines worth mentioning here as they are generally not known outside the circle of professional typesetters and subeditors:

Table 1.1 A badly formatted table

	Species I		Species II	
Dental measurement	mean	SD	mean	SD
I1MD	6.23	0.91	5.2	0.7
I1LL	7.48	0.56	8.7	0.71
I2MD	3.99	0.63	4.22	0.54
I2LL	6.81	0.02	6.66	0.01
CMD	13.47	0.09	10.55	0.05
CBL	11.88	0.05	13.11	0.04

Table 1.2 A nice looking table

Dental measurement	Species I		Species II	
	mean	SD	mean	SD
I1MD	6.23	0.91	5.2	0.7
I1LL	7.48	0.56	8.7	0.71
I2MD	3.99	0.63	4.22	0.54
I2LL	6.81	0.02	6.66	0.01
CMD	13.47	0.09	10.55	0.05
CBL	11.88	0.05	13.11	0.04

Table 1.3 Even better looking table using booktabs

Dental measurement	Species I		Species II	
	mean	SD	mean	SD
I1MD	6.23	0.91	5.2	0.7
I1LL	7.48	0.56	8.7	0.71
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CMD	13.47	0.09	10.55	0.05
CBL	11.88	0.05	13.11	0.04

Table 1.4 Characterizations of normal and extremally disconnected spaces

Space X	NORMAL	EXTREMALLY DISCONNECTED
Urysohn's separation type lemma	Every two disjoint CLOSED subsets of X are completely separated (Urysohn 1925).	Every two disjoint OPEN subsets of X are completely separated (Gillman & Jerison 1960).
Tietze's extension type theorem	Each CLOSED subset of X is C^*-embedded (Tietze 1915).	Each OPEN subset of X is C^*-embedded (Gillman & Jerison 1960).
Katětov-Tong insertion type theorem	For every UPPER semicontinuous real function f and LOWER semi-continuous real function g satisfying $f \leq g$, there exists a continuous real function h such that $f \leq h \leq g$ (Katětov 1951, Tong 1952).	For every LOWER semicontinuous real function f and UPPER semi-continuous real function g satisfying $f \leq g$, there exists a continuous real function h such that $f \leq h \leq g$ (Stone 1949, Lane 1975).
Hausdorff mapping invariance type theorem	The image of X under any CLOSED continuous map is NORMAL (Hausdorff 1935).	The image of X under any OPEN continuous map is EXTREMALLY DISCONNECTED.

1.4   Next section

1.5   Next section

Chapter 2

My second chapter

2.1 Reasonably long section title
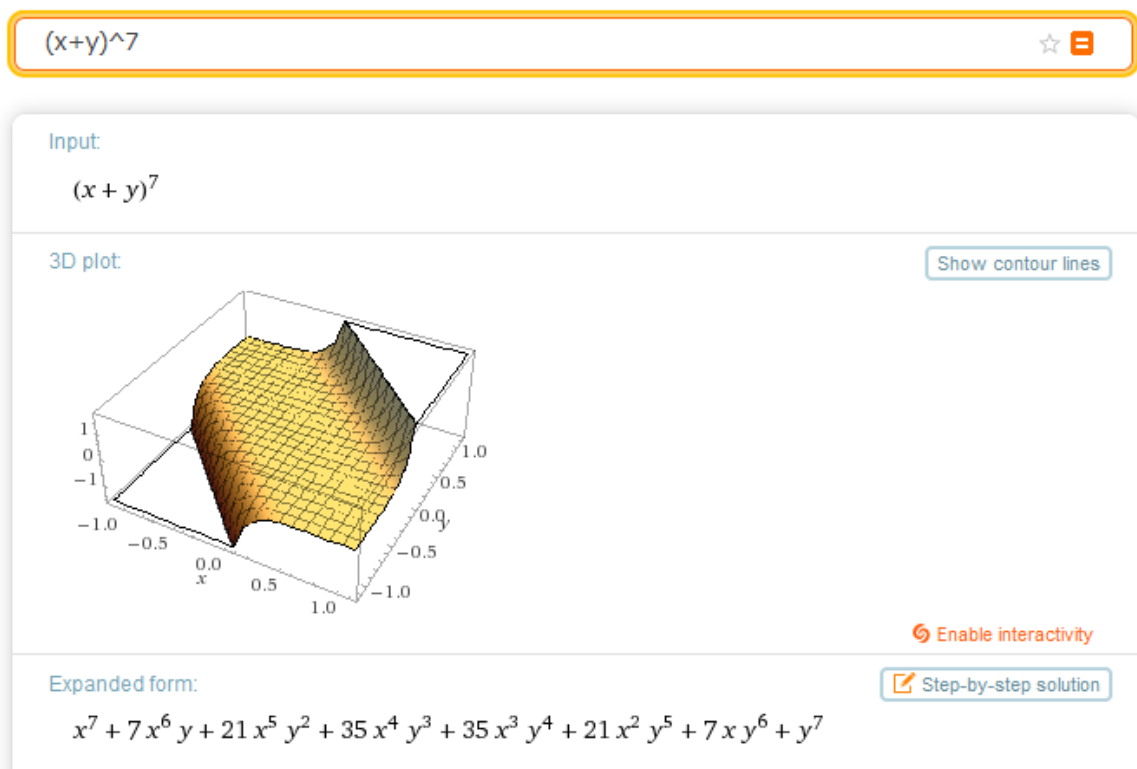
I'm going to randomly include a picture in Figure 2.1.

Fig. 2.1 This is just a long figure caption

Enumeration

1. The first topic is dull

2. The second topic is duller

    (a) The first subtopic is silly

    (b) The second subtopic is stupid

3. The third topic is the dullest

itemize

- The first topic is dull

- The second topic is duller

    - The first subtopic is silly

    - The second subtopic is stupid

- The third topic is the dullest

description

The first topic is dull

The second topic is duller

 The first subtopic is silly

 The second subtopic is stupid

The third topic is the dullest

2.2 Second section

Galois was born on 25 October 1811 to Nicolas-Gabriel Galois and Adélaïde-Marie (born Demante). His father was a Republican and was head of Bourg-la-Reine's liberal party. He became mayor of the village after Louis XVIII returned to the throne in 1814. His mother, the daughter of a jurist, was a fluent reader of Latin and classical literature and was responsible for her son's education for his first twelve years. At the age of 10, Galois was offered a place at the college of Reims, but his mother preferred to keep him at home.

In October 1823, he entered the Lycée Louis-le-Grand, and despite some turmoil in the school at the beginning of the term (when about a hundred students were expelled), Galois managed to perform well for the first two years, obtaining the first prize in Latin. He soon became bored with his studies and, at the age of 14, he began to take a serious interest in mathematics.

He found a copy of Adrien Marie Legendre's *Éléments de Géométrie*, which it is said that he read "like a novel" and mastered at the first reading. At 15, he was reading the original papers of Joseph Louis Lagrange, such as the landmark *Réflexions sur la résolution algébrique des équations*

which likely motivated his later work on equation theory, and *Leçons sur le calcul des fonctions*, work intended for professional mathematicians, yet his classwork remained uninspired, and his teachers accused him of affecting ambition and originality in a negative way.[1].

While many mathematicians before Galois gave consideration to what are now known as groups, it was Galois who was the first to use the word group (in French *groupe*) in a sense close to the technical sense that is understood today, making him among the founders of the branch of algebra known as group theory. He developed the concept that is today known as a normal subgroup. He called the decomposition of a group into its left and right cosets a proper decomposition if the left and right cosets coincide, which is what today is known as a normal subgroup. He also introduced the concept of a finite field (also known as a Galois field in his honor), in essentially the same form as it is understood today.

In his last letter to Chevalier and attached manuscripts, the second of three, he made basic studies of linear groups over finite fields:

- He constructed the general linear group over a prime field, $GL(\nu, p)$ and computed its order, in studying the Galois group of the general equation of degree p^ν.

- He constructed the projective special linear group $PSL(2, p)$. Galois constructed them as fractional linear transforms, and observed that they were simple except if p was 2 or 3. These were the second family of finite simple groups, after the alternating groups.

- He noted the exceptional fact that $PSL(2, p)$ is simple and acts on p points if and only if p is 5, 7, or 11.

---

[1]My footnote goes blah blah blah! ...

(a) 7 Bridges

(b) Collatz

(c) Venn diagram

Fig. 2.2 Best Pictures
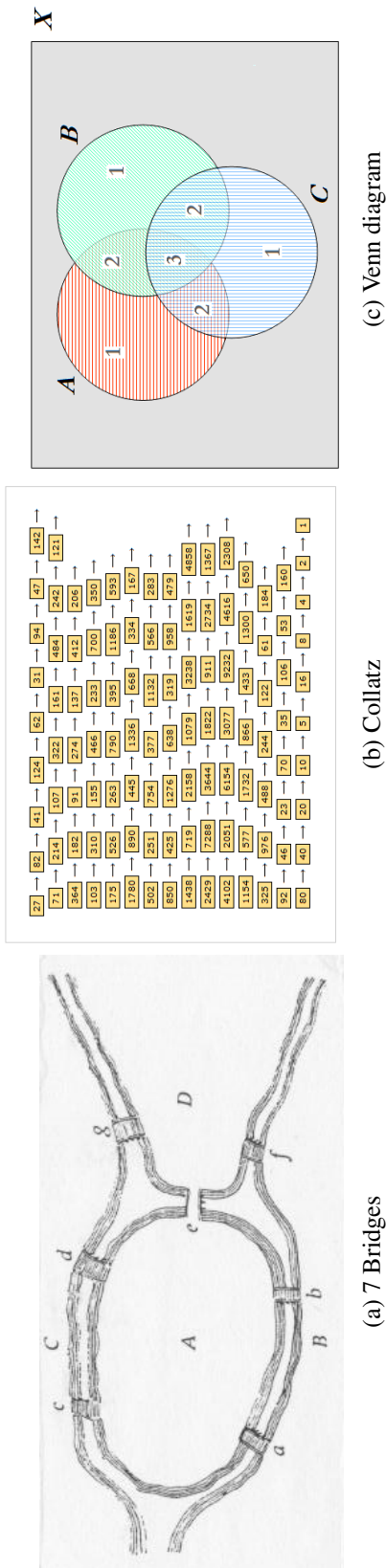
Subplots

I can cite AAA (see Fig. 2.2b) and BBB (Fig. 2.2c) or I can cite the whole figure as Fig. 2.2

2.3 Third section

2.4 Hidden section

Chapter 3

My third chapter

3.1 Title with math σ

The well known Pythagorean theorem $x^2 + y^2 = z^2$ was proved to be invalid for other exponents. Meaning the next equation has no integer solutions: $x^n + y^n = z^n$.

The binomial coefficient is defined by the next expression:

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

And of course this command can be included in the normal text flow $\binom{n}{k}$. Limit $\lim_{x \to \infty} f(x)$ inside text.

$$\lim_{x \to \infty} f(x)$$

The most famous equation in the world: $E^2 = (m_0 c^2)^2 + (pc)^2$, which is known as the **energy-mass-momentum** relation as an in-line equation.

$$CIF: \quad F_0^j(a) = \frac{1}{2\pi\iota} \oint_\gamma \frac{F_0^j(z)}{z-a} dz \tag{3.1}$$

Integral $\int_a^b x^2 dx$ inside text.

$$\iiint_V \mu(u,v,w)\,du\,dv\,dw \tag{3.2}$$

3.2 Preliminaries I. Free constructions

We will work with point-free real numbers as they are usually described in literature, that is, by generators subject to relations. Since the free generators come from a set that is in fact a meet-semilattice (while its elements are used in the free construction simply as elements of a set) we think that it may be useful for the reader to compare the free frames over sets with free frames over semilattices.

11

We will work with point-free real numbers as they are usually described in literature, that is, by generators subject to relations. Since the free generators come from a set that is in fact a meet-semilattice (while its elements are used in the free construction simply as elements of a set) we think that it may be useful for the reader to compare the free frames over sets with free frames over semilattices.

3.2.1   Free semilattice with 1.

For a set X define $F(X) = \{A \subseteq X \mid A \text{ finite}\}$ ordered by $\leq = \supseteq$ so that we have the meet $A \wedge B = A \cup B$. Denote by β_X the mapping

$$\beta_X = (x \mapsto \{x\}) \colon X \to F(X).$$

Then we have for each meet-semilattice S with 1 and each mapping $f \colon X \to S$ precisely one meet-semilattice homomorphism $\overline{f} \colon F(X) \to S$ such that $\overline{f}\beta_X = f$ and $\overline{f}(\emptyset) = 1$, namely the homomorphism defined by $\overline{f}(A) = \bigwedge_{x \in A} f(x)$.

3.2.2   Free frame generated by a semilattice with 1.

For a meet-semilattice S with 1 set $\mathfrak{D}(S) = \{U \subseteq S \mid \downarrow U = U \neq \emptyset\}$. $\mathfrak{D}(S)$ is a frame with unions for joins and intersections for meets and if we denote by α_S the mapping

$$\alpha_S = (s \mapsto \downarrow s) \colon S \to \mathfrak{D}(S)$$

we have a meet-semilattice homomorphism such that for each frame L and each meet-semilattice homomorphism $h \colon S \to L$ there is precisely one frame homomorphism $\widehat{h} \colon \mathfrak{D}(S) \to L$ such that $\widehat{h}\alpha_S = h$, namely that defined by $\widehat{h}(U) = \bigvee_{s \in U} h(s)$.

The free frame over a set can be now obtained combining F and $\mathfrak{D}$, that is, as $\mathfrak{D}F(X)$.

3.2.3   Free frames over a set and over a meet-semilattice compared.

Well, one may go on adding more and more subsections, but these are enough to illustrate how this works!

3.3   Where does it come from?

And this illustrates how one may add more sections to the text.

3.4   Next section

3.5   Next section

Chapter 4

Conclusion

We end with some final comments . . .

References

[1] Ancey, C., Coussot, P., and Evesque, P. (1996). Examination of the possibility of a fluid-mechanics treatment of dense granular flows. *Mechanics of Cohesive-frictional Materials*, 1(4):385–403.

[2] Read, C. J. (1985). A solution to the invariant subspace problem on the space l_1. *Bull. London Math. Soc.*, 17:305–317.

Appendix A

More information $\int$

Carl Friedrich Gauss

Johann Carl Friedrich Gauss (30 April 1777 – 23 February 1855) was a German mathematician who contributed significantly to many fields, including number theory, algebra, statistics, analysis, differential geometry, geodesy, geophysics, electrostatics, astronomy, matrix theory, and optics.

Sometimes referred to as the Princeps mathematicorum (Latin, "the Prince of Mathematicians" or "the foremost of mathematicians") and "greatest mathematician since antiquity", Gauss had a remarkable influence in many fields of mathematics and science and is ranked as one of history's most influential mathematicians.

Gauss was a child prodigy. There are many anecdotes about his precocity while a toddler, and he made his first ground-breaking mathematical discoveries while still a teenager. He completed Disquisitiones Arithmeticae, his magnum opus, in 1798 at the age of 21, though it was not published until 1801. This work was fundamental in consolidating number theory as a discipline and has shaped the field to the present day.

Gauss's intellectual abilities attracted the attention of the Duke of Brunswick, who sent him to the Collegium Carolinum (now Braunschweig University of Technology), which he attended from 1792 to 1795, and to the University of Göttingen from 1795 to 1798. While at university, Gauss independently rediscovered several important theorems; his breakthrough occurred in 1796 when he showed that any regular polygon with a number of sides which is a Fermat prime (and, consequently, those polygons with any number of sides which is the product of distinct Fermat primes and a power of 2) can be constructed by compass and straightedge. This was a major discovery in an important field of mathematics; construction problems had occupied mathematicians since the days of the Ancient Greeks, and the discovery ultimately led Gauss to choose mathematics instead of philology as a career. Gauss was so pleased by this result that he requested that a regular heptadecagon be inscribed on his tombstone. The stonemason declined, stating that the difficult construction would essentially look like a circle.

The year 1796 was most productive for both Gauss and number theory. He discovered a construction of the heptadecagon on 30 March. He further advanced modular arithmetic, greatly simplifying manipulations in number theory. On 8 April he became the first to prove the quadratic reciprocity law. This remarkably general law allows mathematicians to determine the solvability of any quadratic

equation in modular arithmetic. The prime number theorem, conjectured on 31 May, gives a good understanding of how the prime numbers are distributed among the integers.

Another section

Subsection

Subsubsection

...