

Longest Common Subsequence

Longest common Subsequence mean, we need to find common string between 2 strings where ~~ends~~ index of the string doesn't matter, but order of the string does matter.

For example, -

LCS for 'abcde' & 'ace' \Rightarrow 3 [ace]

LCS for 'ABCDGH' & 'AEDFHR' \Rightarrow 3 [ADH]

To Find the LCS,

we use following algorithm,
we use "DP approach"

- * Declare an array of length $(\text{len}(\text{text1})+1, \text{len}(\text{text2})+1)$
- * we iterate the DP array from $(\text{len}(\text{text1})+1, \text{len}(\text{text2})+1)$ to $(0,0)$
- * The LCS will be accumulated finally at $(0,0)$
- * In b/w we accumulate DP array as follows

if $(\text{text1}[i] == \text{text2}[j])$:

$$\text{dp}[i][j] = 1 + \text{dp}[i+1][j+1]$$

else:

$$\text{dp}[i][j] = \max(\text{dp}[i+1][j], \text{dp}[i][j+1])$$

After iterating the whole DP array we return $\text{dp}[0][0]$

$$(0,0) \Rightarrow a=a$$

$$\Downarrow$$
$$\text{dp}[0][0] = 1 + \text{dp}[1][1]$$

$$\text{dp}[0][0] = 1 + 2 = 3$$

$$\boxed{\text{dp}[0][0] = 3}$$

\hookrightarrow LCS

text1 = 'abcde'

text2 = 'ace'

	a	c	e
a	3	2	1
b	2	2	1
c	2	2	1
d	1	1	1
e	1	1	1
	0	0	0

Initialize DP array with 0

$$(2,4) \Rightarrow e=e$$

$$j \Rightarrow 1 + \text{dp}[i+1][j+1]$$

$$\text{dp}[2][4] \Rightarrow 1 + \text{dp}[3][4] = 1 + 0 = 1$$

$$\boxed{\text{dp}[4][2] = 1}$$

$$(4,1)(4,0)(3,2)(3,1)(3,0)$$

$$(2,2)$$

$$\Downarrow$$
$$\max(\text{dp}[i+1][j], \text{dp}[i][j+1])$$

$$(2,1) \Rightarrow c=c$$

$$\text{dp}[2][1] \Rightarrow 1 + \text{dp}[i+1][j+1] \Rightarrow 1 + 1 = 2$$

$$\boxed{\text{dp}[2][1] = 2}$$

$$(2,0)(1,2)(1,1)(1,0)(0,2)(0,1)$$

$$\Downarrow$$
$$\max(\text{dp}[i+1][j], \text{dp}[i][j+1])$$