

Homework/Programming Assignment #2

Homework/midterm Due: 04/05/2022- 5:00 PM

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Name/EID: Email:

Signature (required)

I/We have followed the rules in completing this

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Assignment.

Question	Points	Total
HA 1	25	
HA 2	25	
HA 3	25	
HA 4	25	
PA	100	
PA. k (Bonus)	15	
PA. m (Bonus)	30	
Presentation* (Bonus)	20	

Instruction:

- 1. Remember that this is a graded assignment. It is the equivalent of a <u>midterm</u> take-home exam.
- 2. * You should present the results of the PA in the class and receive extra bonus depending on the quality of your presentation!
- 3. **For PA questions**, you need to write a report showing how you derived your equations, describes your approach, test functions, and discusses the results. You should show your test results for each function.
- 3. You are to work alone or in teams of two and are not to discuss the problems with anyone other than the TAs or the instructor.
- 4. It is open book, notes, and web. But you should cite any references you consult.
- 5. Unless I say otherwise in class, it is due before the start of class on the due date mentioned in the Assignment.
- 6. **Sign and append** this score sheet as the first sheet of your assignment.
- 7. Remember to submit your assignment in Canvas.

$$HA: 4.8, 4.11, 5.12, 5.13$$

$$H=\begin{bmatrix} 1 & 0 & 0 & L_1 \\ 0 & 1 & 0 & L_3 + L_4 \\ 0 & 0 & 1 & -25 - 26 \end{bmatrix}$$

$$i \quad \omega; \quad g_i \quad v_i$$
 $1 \quad (-1.0.0) \quad (0.0.0) \quad (0.0.0)$
 $2 \quad (0.0,-1) \quad (2_{1,0,0}) \quad (0,2_{1,0})$
 $3 \quad (0,1.0) \quad (2_{1,0,2_1}) \quad (-2_{2,0,2_1})$
 $4 \quad (1.0.0) \quad (2_{1,2_3+2_4,0}) \quad (0,1,0)$
 $5 \quad (0.0.0) \quad (2_{1,2_3+2_4,0}) \quad (0,1,0)$
 $6 \quad (0,1.0) \quad (2_{1,2_3+2_4,-2_5}) \quad (2_{5,0,2_1})$

$$5, = [-1,0,0,0,0,0]^{T}
5_{s} = [0,0,-1,0,2,0]^{T}
5_{s} = [0,1,0,-2,0,2,]^{T}
5_{4} = [1,0,0,0,0,-2,3]^{T}
5_{5} = [0,0,0,0,1,0]^{T}
5_{6} = [0,1,0,2,0,2,3]^{T}$$

$$M^{-1} = \begin{bmatrix} 1 & 0 & 0 & -L_1 \\ 0 & 1 & 0 & -L_3 - L_4 \\ 0 & 0 & 1 & L_5 + L_6 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$B_1 = [-1, 0, 0, 0, -15-16, -13-14]^T$$
 $B_2 = [0, 0, -1, 13+14, 0, 0]^T$
 $B_3 = [0, 1, 0, -15-16-12, 0, 0]^T$
 $B_4 = [1, 0, 0, 0, 1, 0]^T$
 $B_5 = [0, 0, 0, 0, 1, 0]^T$
 $B_6 = [0, 1, 0, -16, 0]^T$

$$M = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$i \quad W; \quad \mathcal{Z}; \quad V;$$
 $1 \quad (0,0,1) \quad (0,0,0) \quad (0,0,0)$
 $2 \quad (0,0,6) \quad (0,0,0) \quad (1,0,0)$
 $3 \quad (0,0,1) \quad (1,0,0) \quad (0,-1,0)$
 $4 \quad (0,-1,0) \quad (1,0,-1) \quad (-1,0,-1)$
 $5 \quad (-1/2,0,1/12) \quad (2,0,-1) \quad (0,-1/12,0)$

$$S_{1} = [0,0,1,0,0,0]^{T}$$
 $S_{2} = [0,0,0,1,0,0]^{T}$
 $S_{3} = [0,0,1,0,-1,0]^{T}$
 $S_{4} = [0,-1,0,-1,0,-1]^{T}$
 $S_{5} = [-1/\sqrt{2},0,1/\sqrt{2},0]^{T}$

$$\mathcal{M}^{-1} = \begin{bmatrix} 1 & 0 & 0 & -37 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$Ady_{1} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 3 & 0 & 1 & 0 \\ 0 & -3 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$B_1 = [0,0,1,0,3,0]^T$$
 $B_2 = [0,0,0,1,0,0]^T$
 $B_3 = [0,0,1,0,2,0]^T$
 $B_4 = [0,-1,0,-1,0,2]^T$
 $B_5 = [-1/\sqrt{2},0,1/\sqrt{2},0,\sqrt{2},0]^T$

$$5.12a)i$$
 $W;$ $9;$ $V;$ 1 $(0.0.1)$ $(0,-2-0_4,-2)$ $(-2-0_4,0.0)$ 2 $(1,0.0)$ $(0,2-0_4,0)$ $(0,0,2+0_4)$ 3 $(0.0.1)$ $(0.-0_4,0)$ $(-0_4,0.0)$ $(0,1.0)$

$$\int_{B_{1}} = Ad_{e}^{-ce_{1}7\theta_{4}} e^{-[B_{1}]\theta_{3}} e^{-[B_{1}]\theta_{1}} B,$$

$$= \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 1 & 0 &$$

5.13(a)
$$i$$
 W_i g_i V_i
 i $(0,0,1)$ $(0,0,0)$
 i $(0,0,0)$ $(0,0,0)$
 i $(0,0,0)$ $(0,0,0)$
 i $(0,0,0)$ $(0,0,0)$
 i $(0,0,0)$ $(0,0,0,0)$
 i $(0,0,0)$ $(0,0,0,0)$

$$[5_{1}] = \begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad 5_{1} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$[5_{2}] = \begin{bmatrix} 0 & 0 & 1 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad 5_{2} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$[5_{3}] = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad 5_{3} = \begin{bmatrix} -1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$[5_{4}] = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 2L \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad 5_{4} = \begin{bmatrix} -1 \\ 0 \\ 0 \\ 0 \\ 2L \end{bmatrix}$$

$$[3s] = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & -1 & 0 & 3L & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$[3s] = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{bmatrix}$$

$$[3s] = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{bmatrix}$$

$$[3s] = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{bmatrix}$$

Each column of the Jacobian motrix can be columnted as below with each joint angle

J3, = 3,

b) Kinematie singularities 1 Colinear when $0_3 = 0_4 = 0_5 = 0$, joints 2 and b are colinear. From the above calculation, Js3 = Adecs, 70, Es, 70, 53 Jsy = Adp ES, 70, p ES, 70, 54 JS6 = Adpls, 70, pls, 70, 55 JS6 = Adpls,70, pls,70, 36 Based on the representation of $53, \dots, 56$, it's easy to see that I is singular.

Thus, when $O_3 = O_4 = O_5 = 0$, the end effector losses freedom in the y-and Z-directions