

practice questions 9/20

question 1

$$x(n) = 2x(n/2) + n, x(1) = 1$$

1. $x(n/2) = 2x(n/4) + (n/2)$
 1. $x(n) = 2(2x(n/4) + n/2) + n$
 2. $x(n) = 4x(n/4) + 2n$
2. $x(n/4) = 2x(n/8) + n/4$
 1. $x(n) = 4(2x(n/8) + n/4) + 2n$
 2. $x(n) = 8x(n/8) + 3n$
3. $x(n) = 2^{k \cdot x(n/(2^k))} + kn$
4. $1 = n/2^k$
 1. $2^k = n$
 2. $k = \lg(n)$
5. $x(n) = n + n \cdot \lg(n)$

brute force - check all possible solutions

generate all pathagorean triplets

$$// a^2 + b^2 = c^2$$

convex hull problem

A set of points (finite or infinite) in a plane is called convex if for any 2 points p and q in the set, the entire line segment with end points p and q belongs to the set.

The convex hull of a set S of points is the smallest convex set containing S.

so you have a cloud of points and you need to find the perimeter. you can solve this by choosing a line segment and checking if all other points are on one side of the segment. if they are, then it is a perimeter line. otherwise it is an inner line.

this is not just $n!$ or n^2 , because you need to create pairs of lines, and compare. creating the lines would be $C(n, 2)$, or $\frac{n!}{2!(n-2)!} = \frac{n(n-1)}{2}$ and for verifying takes on average $\frac{n}{2}$, for a total complexity of $\theta(n^3)$. Gram's method uses first sorts it and then it is a linear complexity.