

Human Early Life Mortality

Adaption or Selection?

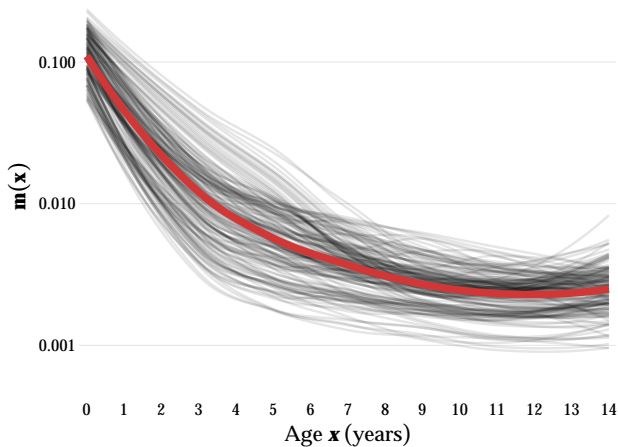
Jonas Schöley

schoeley@demogr.mpg.de



European
Doctoral School
of Demography

The Age Pattern of Early Life Mortality



**Early life
mortality rates**
Various countries
and years.
Data: HMD.

Adaption Models of Early Life Mortality

$$m(x) = A^{(x+B)^C}$$

Heligman and Pollard infant mortality term

Double exponential distribution.

“C measures the rate of mortality decline in childhood (the rate at which a child adapts to its environment).”

Heligman and Pollard 1980.

$$m(x) = ae^{-bx}$$

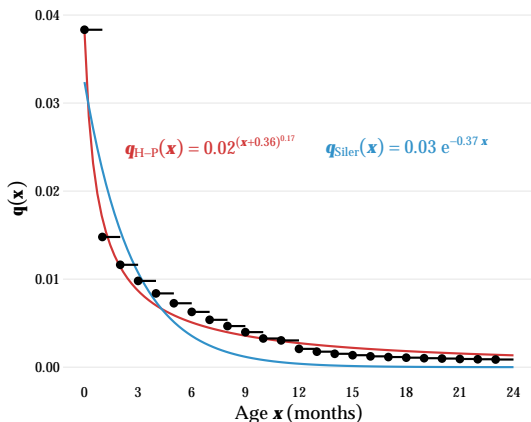
Siler infant mortality term

Negative- b -Gompertz hazard.

“While the most common use of this decreasing hazard would be to account for the hazard due to immaturity, it can also be used [. . .] for other hazards to which an animal adjusts successfully.”

Siler 1979.

Adaption Models of Early Life Mortality



Adaption models of infant mortality

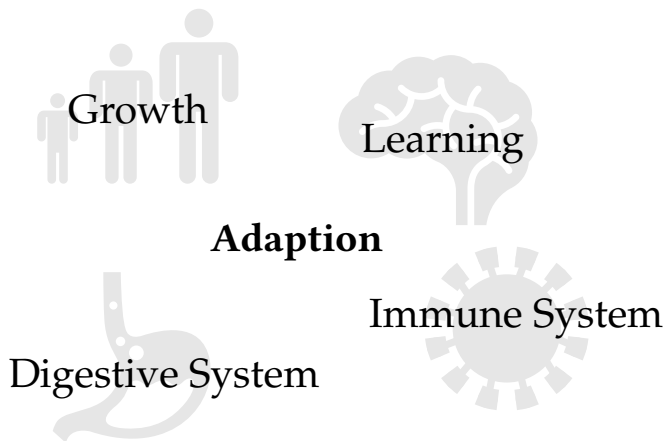
Observed versus predicted probabilities of dying.

Heligman and Pollard 1980 and Siler 1979 model infant mortality terms.

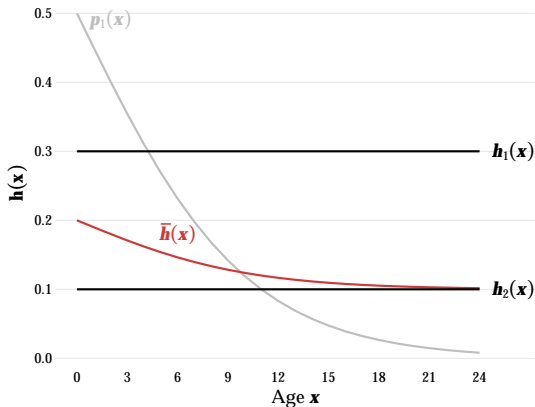
Data:

Statistiske Departement Danmark 1920. 1911–1915 period of Danish males.

Mechanisms of Adaption



A Selection Model of Early Life Mortality



The selection effect of heterogeneous mortality

$h_{1,2}(x)$: Baseline mortality rates for two groups.

$\bar{h}(x)$: Population mortality rate.

$p_1(x)$: Share of group 1 on the total population.

See Vaupel and Yashin 1985 for more of "Heterogeneity's Ruses".

A Selection Model of Early Life Mortality

The Frailty Model: James W. Vaupel, Kenneth G. Manton, and Eric Stallard (1979). “The impact of heterogeneity in individual frailty on the dynamics of mortality”. In: *Demography* 16.3, pp. 439–454

$$\mu(x|z) = \underbrace{z}_{\text{Frailty}} \cdot \underbrace{\mu_0(x)}_{\text{Baseline hazard}}$$

$$\bar{\mu}(x) = \frac{\mu_0(x)}{\gamma M_0(x) + 1}$$

Individual hazard with frailty

Mortality at x for single individual with given frailty factor z .

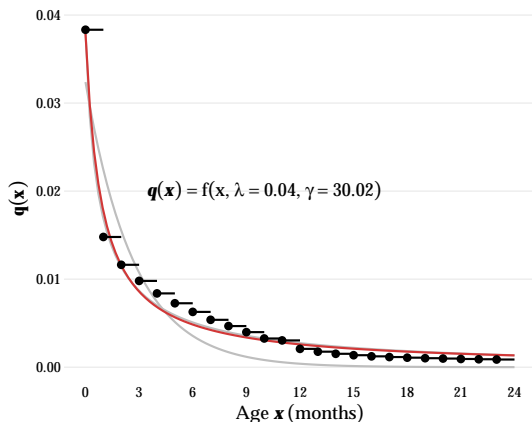
ibid.

Mean population hazard with frailty

Mean mortality in population at x

ibid.

A Selection Model of Early Life Mortality



A selective model of infant mortality

Observed versus predicted probabilities of dying.
Exponential-Gamma frailty model.

Data:

*Statistiske Departement Danmark
1920. 1911–1915 period of Danish
males.*

References

- Heligman, L. and J.H. Pollard (1980). “The Age Pattern of Mortality”. In: *Journal of the Institute of Actuaries* 107.1, pp. 49–80.
- Human Mortality Database* (2015). Online 2015–01–28. University of California, Berkeley and Max Planck Institute for Demographic Research. URL: www.mortality.org.
- Siler, William (1979). “A Competing-Risk Model for Animal Mortality”. In: *Ecology* 60.4.
- Statistiske Departement Danmark (1920). *Statistisk Aarbog 1919*. Danmarks Statistik. København: Nordisk Forlag.
- Vaupel, James W., Kenneth G. Manton, and Eric Stallard (1979). “The impact of heterogeneity in individual frailty on the dynamics of mortality”. In: *Demography* 16.3, pp. 439–454.
- Vaupel, James W. and Anatoli I. Yashin (1985). “Heterogeneity’s Ruses: Some Surprising Effects of Selection on Population Dynamics”. In: *The American Statistician* 39.3, pp. 176–185.