# The Gestational Age Pattern of Human Mortality

**Explaining Ontogenescece** 

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### onto gen ecence, noun

"Ontogenescence is a population-level phenomenon in which the death rate of each cohort tends to decrease with increasing age between conception and maturity." (Levitis 2011)

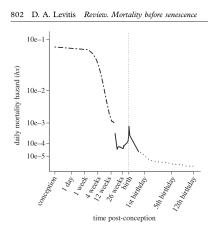


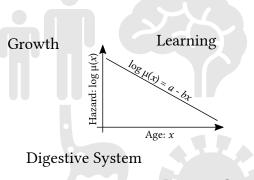
Figure 1. Mortality hazard from conception to 12th birthday.

# Ontogenescence in humans

Fetal- and infant life tables indicate a mortality continuum from conception to maturity disrupted by birth.

Source: Levitis (2011).

### **Ontogenescence as Acquired Robustness**

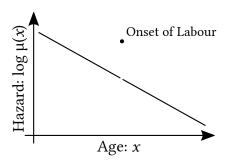


# Acquired robustness

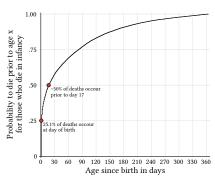
Reduction of an individuals risk of death due to growth and adjustment. *cp. Levitis (2011), Siler (1979)* 

# **Ontogenescence as Transitional Timing**

# **Idealized individual hazard** over gestational age.

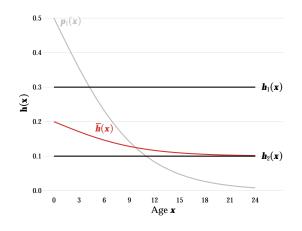


# US infant mortality 2009 by day of age.



**Transitional timing** Early life is full of risky transitions which increase an individuals mortality risk. The process of birth is a prominent example. *cp. Levitis* (2011)

### **Ontogenescence as a Selection Process**



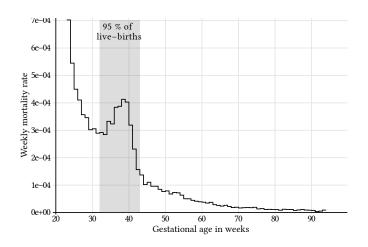
# The selection effect of heterogeneous frailties

 $h_{1,2}(x)$ : Baseline hazard for two groups of different frailties

h(x): Mean hazard in the population

 $p_1(x)$ : Share of group 1 on the total population. See Vaupel and Yashin 1985 for more of "Heterogeneity's Ruses".

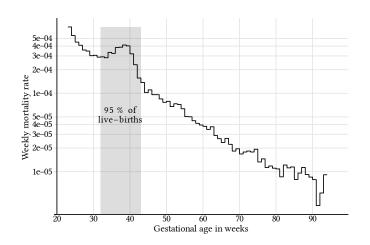
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#### Mortality rates by week of gestation

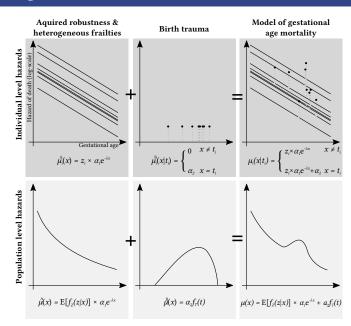
A joint fetal-infant life table for the US conception cohort of 2009. Raw Data: Division of Vital Statistics (2015); the mortality rates have been calculated by the author after aggregating individual records of births, fetal- and infant deaths.

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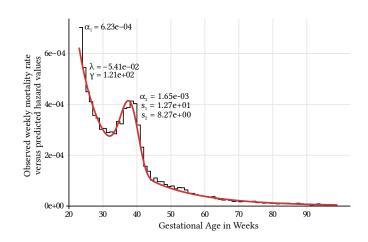
Modelling human ontogenescence across gestational age taking into account *acquired robustness*, *birth trauma* and *selection*.

$$\overline{\mu}(x) = \underbrace{E[f_Z(z|x)]}_{\text{Population hazard at gestational age } x} = \underbrace{E[f_Z(z|x)]}_{\text{Average frailty}} \times \underbrace{\alpha_1 e^{-\lambda x}}_{\text{Acquired robustness component of hazard at gestational age } x}_{\text{at gestational age } x} + \underbrace{\alpha_2 f_T(t)}_{\text{of hazard at gestational age } x}$$

Frailty is assumed to be *Gamma* Distributed, the gestational age at onset of labour *Beta* distributed.

$$\underline{\overline{\mu}(x)}_{\text{Population hazard at gestational age }x} = \underbrace{\frac{\alpha_1 e^{-\lambda x}}{\frac{\gamma \alpha_1}{-\lambda} (e^{-\lambda x} - 1) + 1}}_{\text{Gamma-Gompertz Frailty Model}} + \underbrace{\frac{\alpha_2 x^{s_1 - 1} (24 - x)^{s_2 - 1}}{B(s_1, s_2) \cdot 24^{s_1 + s_2 - 1}}}_{\text{Birth trauma component of hazard at gestational age }x}.$$

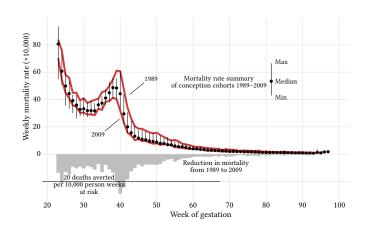
	at gestational age $x$ .
$\alpha_1$	The initial mortality level (at week 23 and process
	time 0).
λ	The relative rate of mortality decline over age.
γ	The initial variance of frailties in the population
	(at week 23 and process time 0).
$lpha_2$	The added mortality risk due to the stress of birth.
$s_1$	The modal gestational age at onset of labour (in
	weeks after week 23).
$s_2$	The shape of the age distribution at onset of
	labour.



#### Mortality rates by week of gestation, observed versus predicted

A joint fetal-infant life table for the US conception cohort of 2009. Raw Data: Division of Vital Statistics (2015); the mortality rates have been calculated by the author after aggregating individual records of births, fetal- and infant deaths.

# Mortality Improvements by Gestational Age



Mortality rates by week of gestation, different conception cohorts Based on single year conception cohorts 1989–2009. No data is available for the years 1991–1994. Raw Data: Division of Vital Statistics (2015); the mortality rates have been calculated by the author after aggregating individual records of births, fetal- and infant deaths.

#### References

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