

The Gestational Age Pattern of Human Mortality

Explaining Ontogenesce

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`https://github.com/jschoeley/fimort-agepat`

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“**Ontogenescence** is a population-level phenomenon in which the death rate of each cohort tends to decrease with increasing age between conception and maturity.” (Levitis 2011)

802 D. A. Levitis *Review. Mortality before senescence*

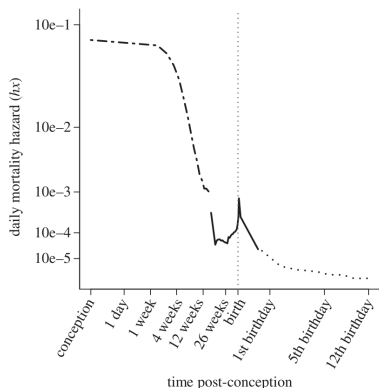


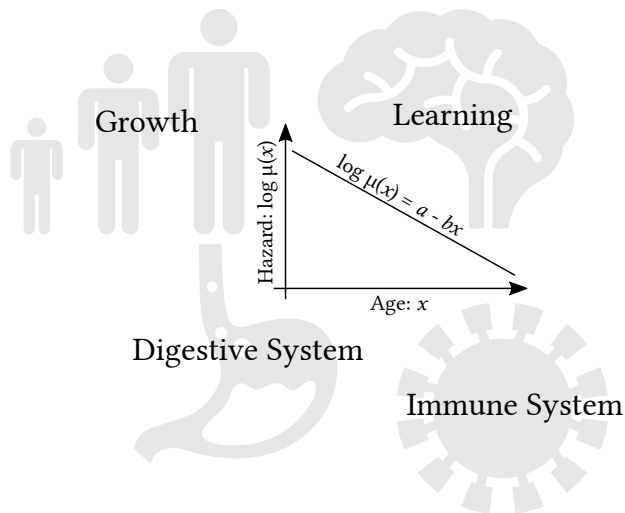
Figure 1. Mortality hazard from conception to 12th birthday.

Ontogenescence in Humans

Fetal- and infant life tables indicate a mortality continuum from conception to maturity disrupted by birth.

Source: Levitis (2011).

Ontogenescence as Acquired Robustness



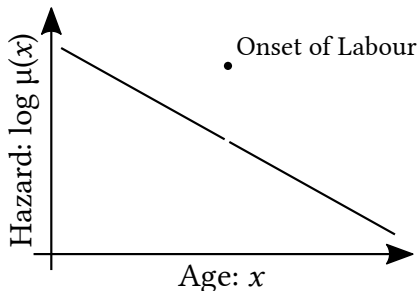
Acquired Robustness

Reduction of an individual's risk of death due to growth and adjustment.

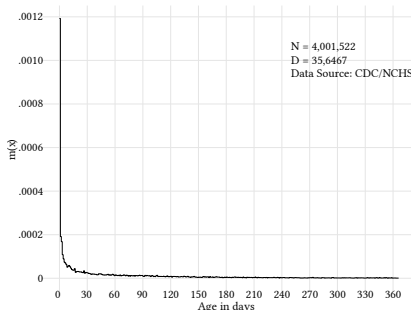
cp. Levitis (2011), Siler (1979)

Ontogenescence as Transitional Timing

**Idealized individual hazard
over gestational age.**

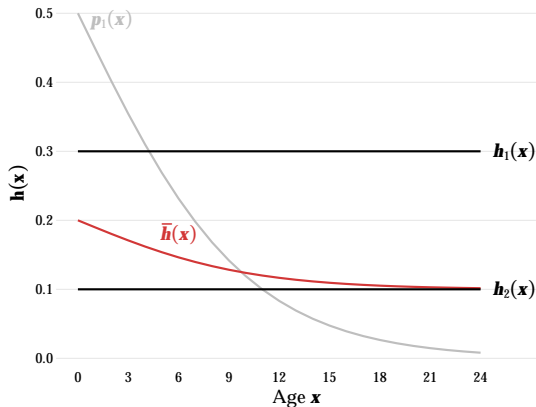


**US infant mortality 2014
by day of age.**



Transitional Timing Early life is full of risky transitions which increase an individuals mortality risk. The process of birth is a prominent example. *cp. Levitis (2011)*

Ontogenescence as a Selection Process



The selection effect of heterogeneous frailties

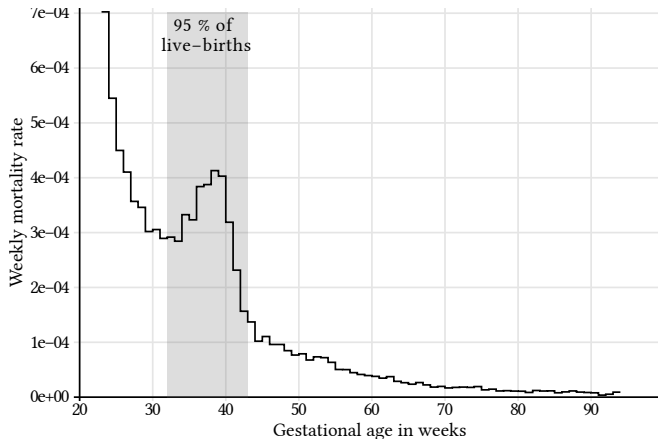
$h_{1,2}(x)$: Baseline hazard for two groups of different frailties

$\bar{h}(x)$: Mean hazard in the population

$p_1(x)$: Share of group 1 on the total population.

See Vaupel and Yashin 1985 for more of “Heterogeneity’s Ruses”.

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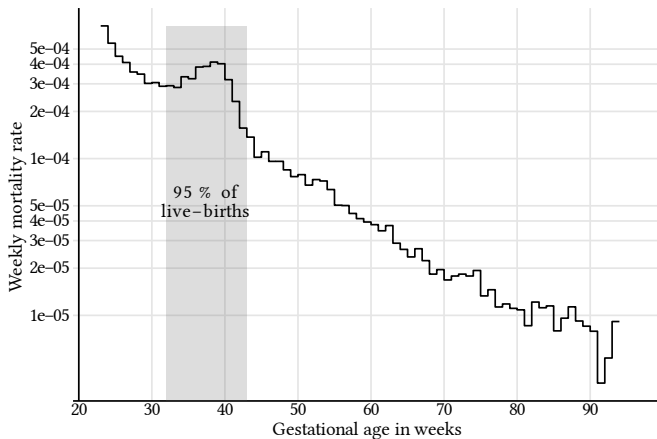


Mortality Rates by Week of Gestation

A joint fetal-infant life table for the US conception cohort of 2009.

Raw Data: Division of Vital Statistics (2015); the mortality rates have been calculated by the author after aggregating individual records of births, fetal- and infant deaths.

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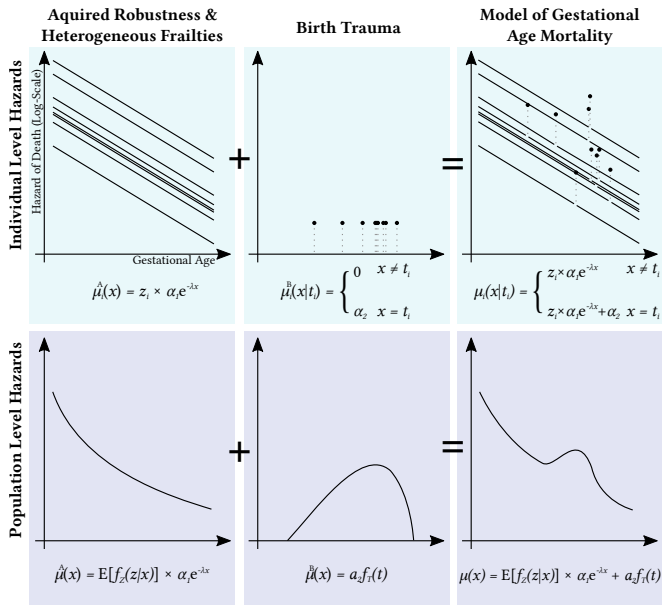


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Modelling the Pattern



Modelling the Pattern

Modelling human ontogenescence across gestational age taking into account *acquired robustness*, *birth trauma* and *selection*.

$$\underbrace{\bar{\mu}(x)}_{\text{Population hazard at gestational age } x} = \underbrace{E[f_Z(z|x)]}_{\text{Average frailty in population at gestational age } x} \times \underbrace{\alpha_1 e^{-\lambda x}}_{\text{Acquired robustness component of hazard at gestational age } x} + \underbrace{\alpha_2 f_T(t)}_{\text{Birth trauma component of hazard at gestational age } x}.$$

Modelling the Pattern

Frailty is assumed to be *Gamma* Distributed, the gestational age at onset of labour *Beta* distributed.

$$\underbrace{\bar{\mu}(x)}_{\text{Population hazard at gestational age } x} = \underbrace{\frac{\alpha_1 e^{-\lambda x}}{\frac{\gamma \alpha_1}{-\lambda} (e^{-\lambda x} - 1) + 1}}_{\text{Gamma-Gompertz Frailty Model}} + \underbrace{\frac{\alpha_2 x^{s_1-1} (24 - x)^{s_2-1}}{B(s_1, s_2) \cdot 24^{s_1+s_2-1}}}_{\text{Birth trauma component of hazard at gestational age } x.}$$

α_1 The initial mortality level (at week 23 and process time 0).

λ The relative rate of mortality decline over age.

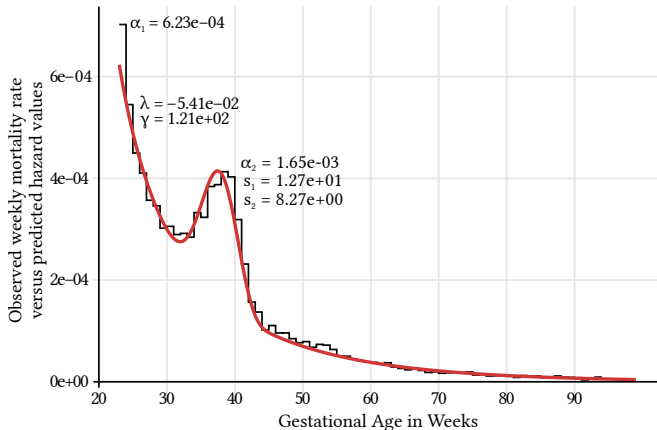
γ The initial variance of frailties in the population (at week 23 and process time 0).

α_2 The added mortality risk due to the stress of birth.

s_1 The modal gestational age at onset of labour (in weeks after week 23).

s_2 The shape of the age distribution at onset of labour.

Modelling the Pattern



Mortality Rates by Week of Gestation, Observed versus Predicted

A joint fetal-infant life table for the US conception cohort of 2009.

Raw Data: Division of Vital Statistics (2015); the mortality rates have been calculated by the author after aggregating individual records of births, fetal- and infant deaths.

References

- Division of Vital Statistics (2015). *Vital Statistics Data. Period Linked Birth-Infant Death Data Files and Fetal Death Data Files*. Online 2015-12-14. National Center for Health Statistics. URL: http://www.cdc.gov/nchs/data_access/Vitalstatsonline.htm.
- Human Mortality Database Team (2015). *Human Mortality Database*. Online 2015-01-28. University of California, Berkeley and Max Planck Institute for Demographic Research. URL: www.mortality.org.
- Levitis, Daniel A. (2011). “Before senescence: the evolutionary demography of ontogenesis”. In: *Proceedings of the Royal Society B* 278, pp. 801–809.
- Siler, William (1979). “A Competing-Risk Model for Animal Mortality”. In: *Ecology* 60.4.
- Vaupel, James W. and Anatoli I. Yashin (1985). “Heterogeneity’s Ruses: Some Surprising Effects of Selection on Population Dynamics”. In: *The American Statistician* 39.3, pp. 176–185.