

Survival Analysis

Session 4: The Kaplan-Meier Estimator

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Recap: Survival Identities

In survival analysis we consider the random variable
"X: Time until event"

$x = 0.1$ weeks, 2.3 weeks...

We express our knowledge about the distribution of X in any of these functions. Knowing any single function we can derive all other via the **Survival Identities**.

f(x): Density function
The relative likelihood of experiencing the event around time x .

$$F(x) = \int_0^x f(x) dx$$

F(x): Distribution function
aka Cumulative function
The probability of experiencing the event until time x .
 $F(x) = P(X \leq x)$

$$S(x) = 1 - F(x)$$

$$S(x) = \int_x^{\infty} f(x) dx \quad h(x) = -S'(x)/S(x)$$

S(x): Survival function

The probability of *not* experiencing the event until time x .
 $S(x) = P(X > x)$

h(x): Hazard function

The instantaneous rate of new events at time x among those who did not experience the event yet.

$$h(x) = \lim_{h \rightarrow 0} P(x \leq X < x+h | X \geq x) / h$$

$$H(x) = \int_0^x h(x) dx$$

$$H(x) = -\log S(x)$$

H(x): Cumulative Hazard
The integral of $h(x)$.

$$S(x) = \exp(-H(x))$$

What Does Survival Data Look Like?

In survival analysis we consider the random variable
"X: Time until event"

$x = 0.1 \text{ month}, 2.3 \text{ months} \dots$

Who? 8 breast cancer patients

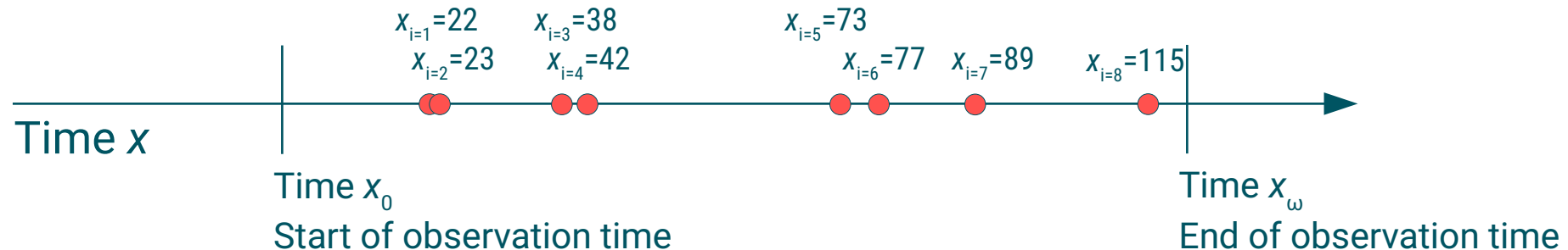
Start of observation? Cancer diagnosis

Event of interest? Death

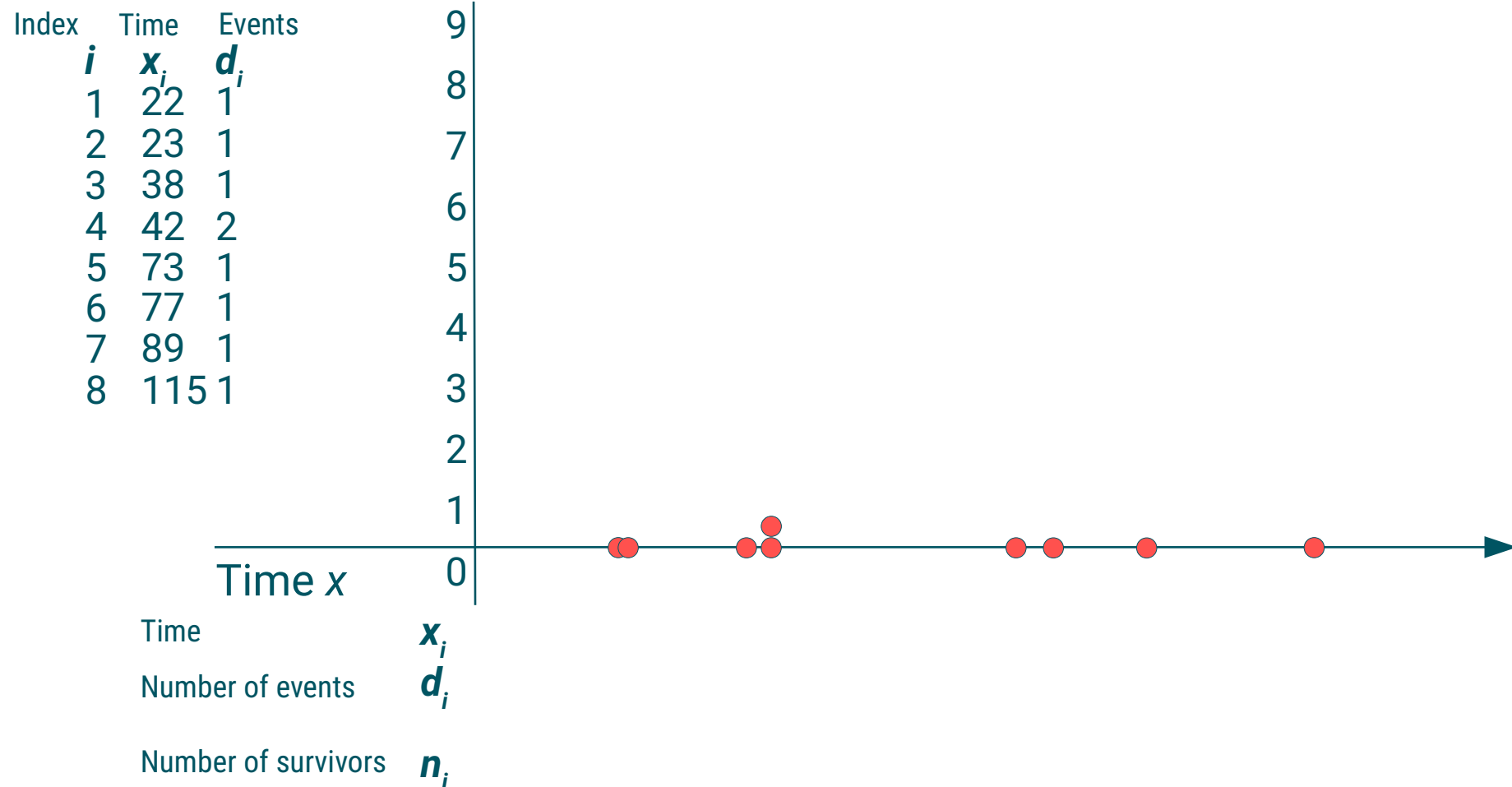
Time unit? Months

End of observation? 10 years follow up

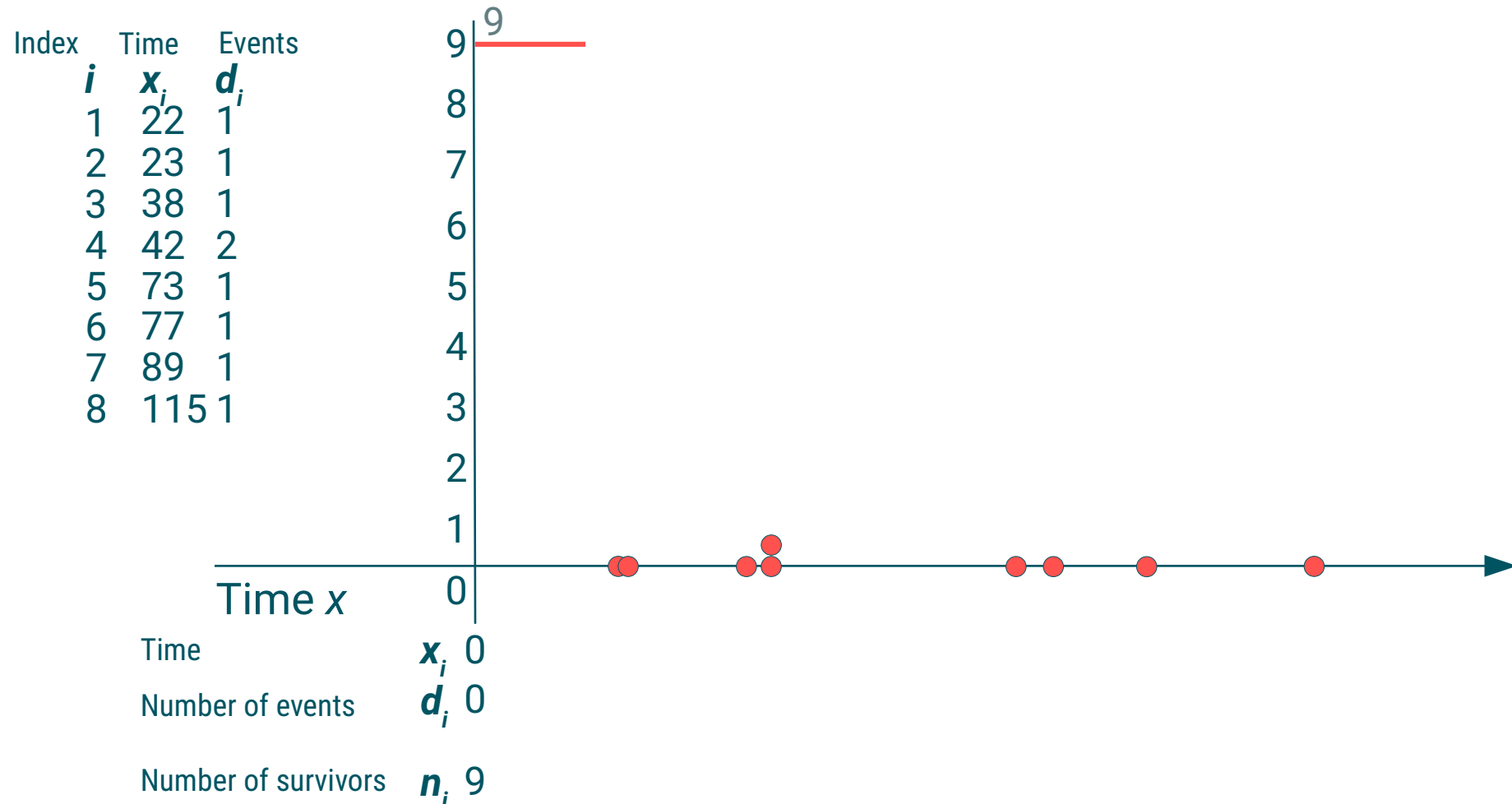
Observation index	Observed event time
i	x
1	22
2	23
3	38
4	42
5	73
6	77
7	89
8	115



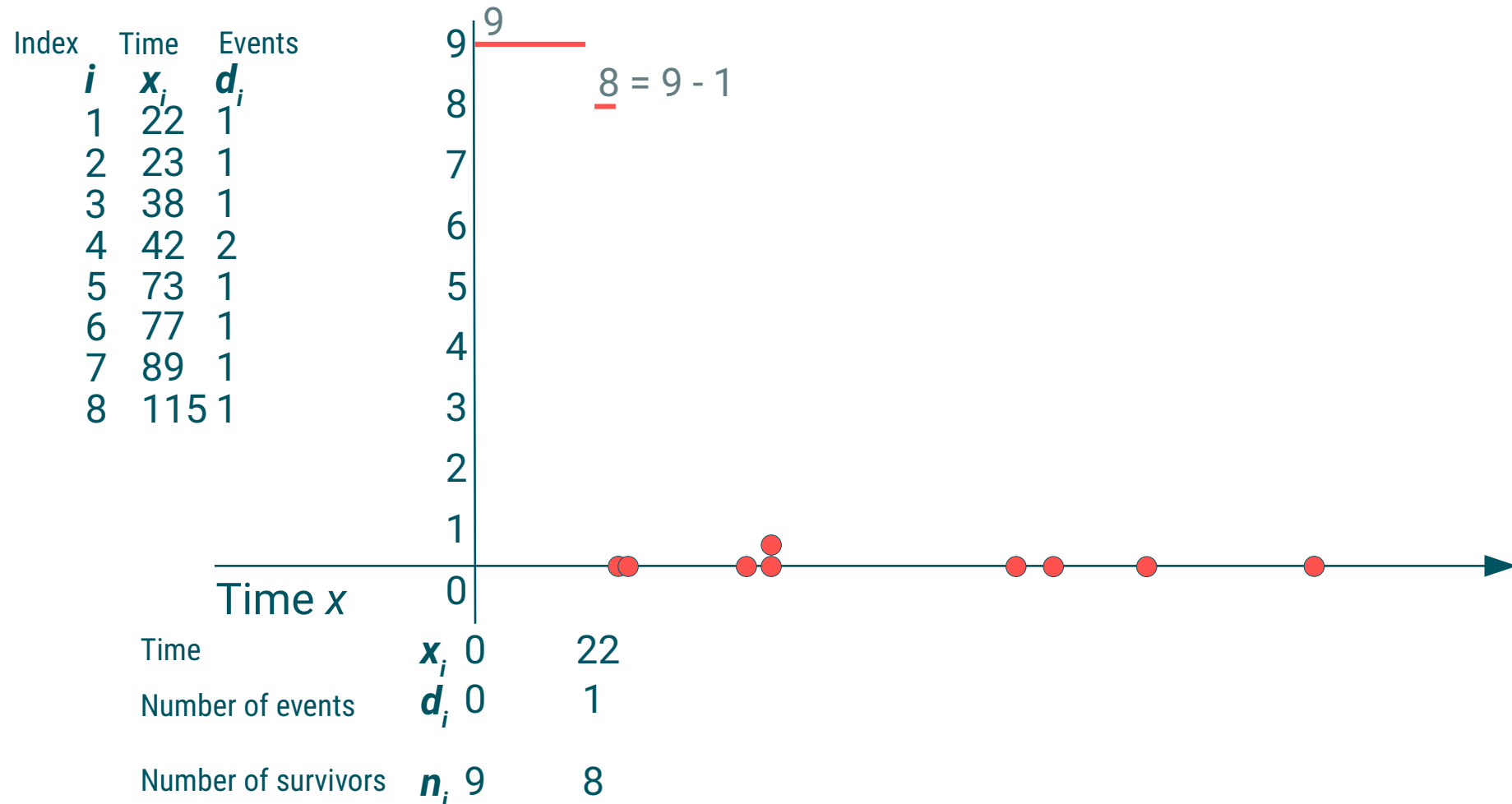
Deriving the Kaplan-Meier Estimator



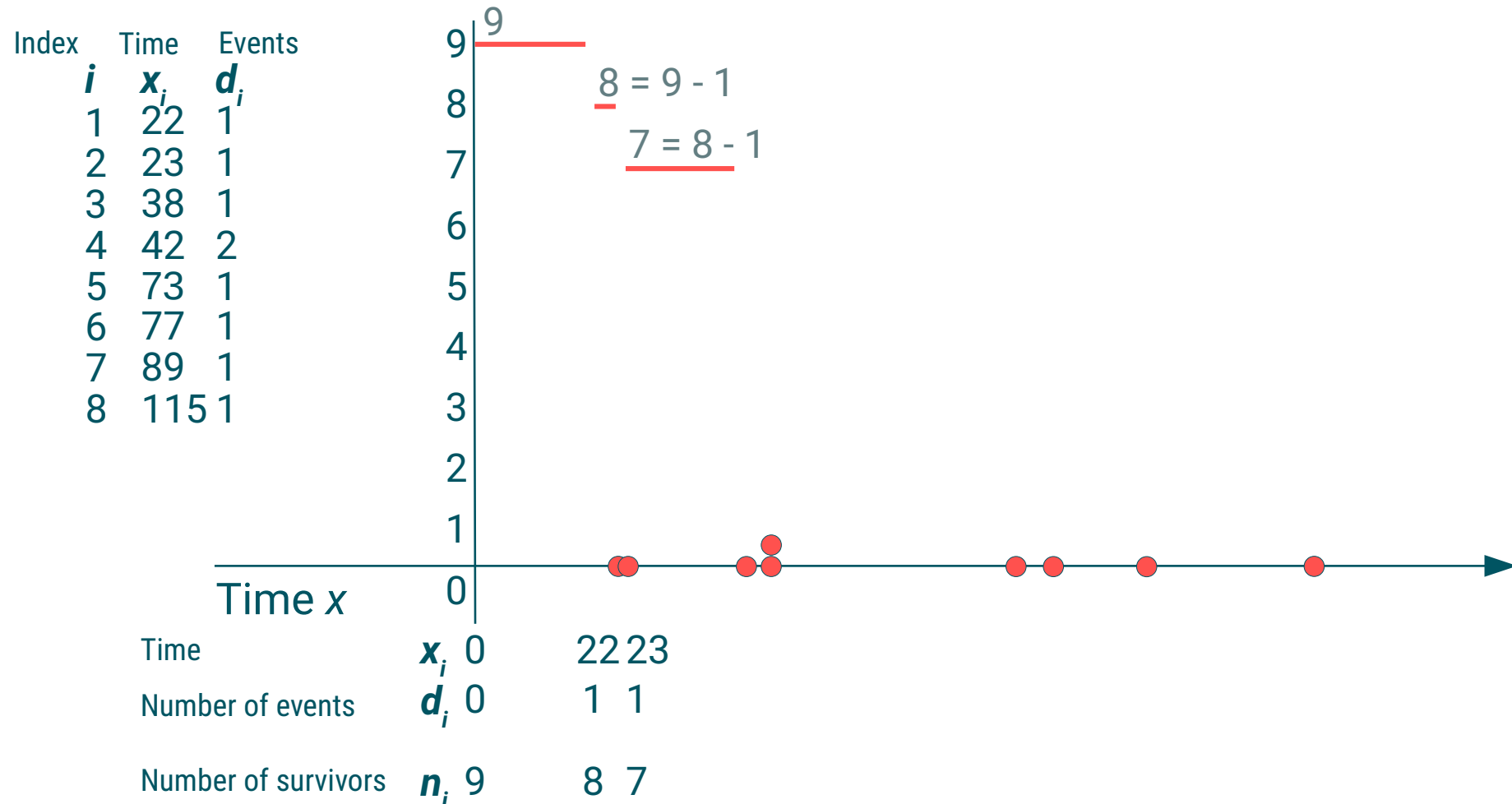
Deriving the Kaplan-Meier Estimator



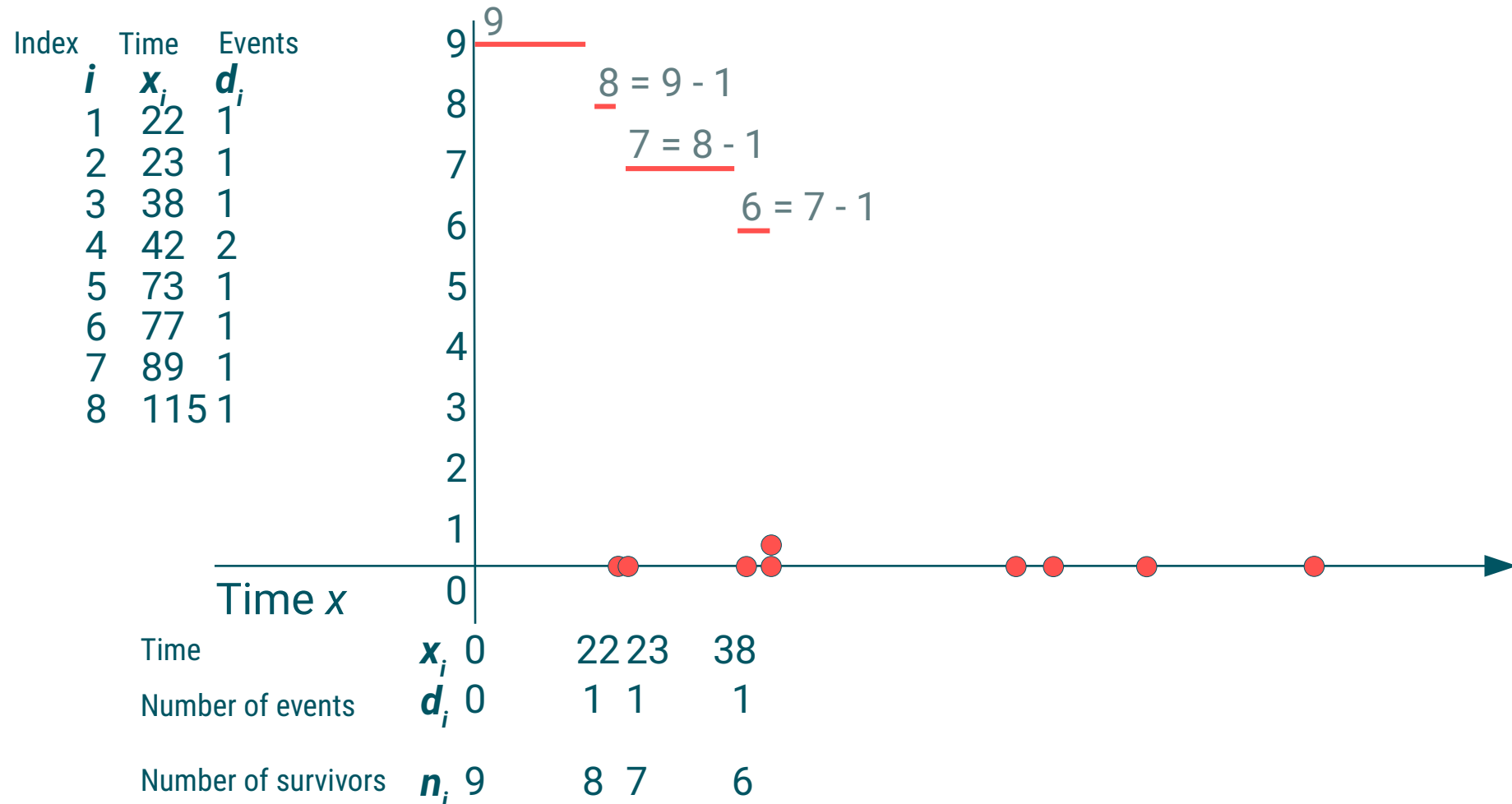
Deriving the Kaplan-Meier Estimator



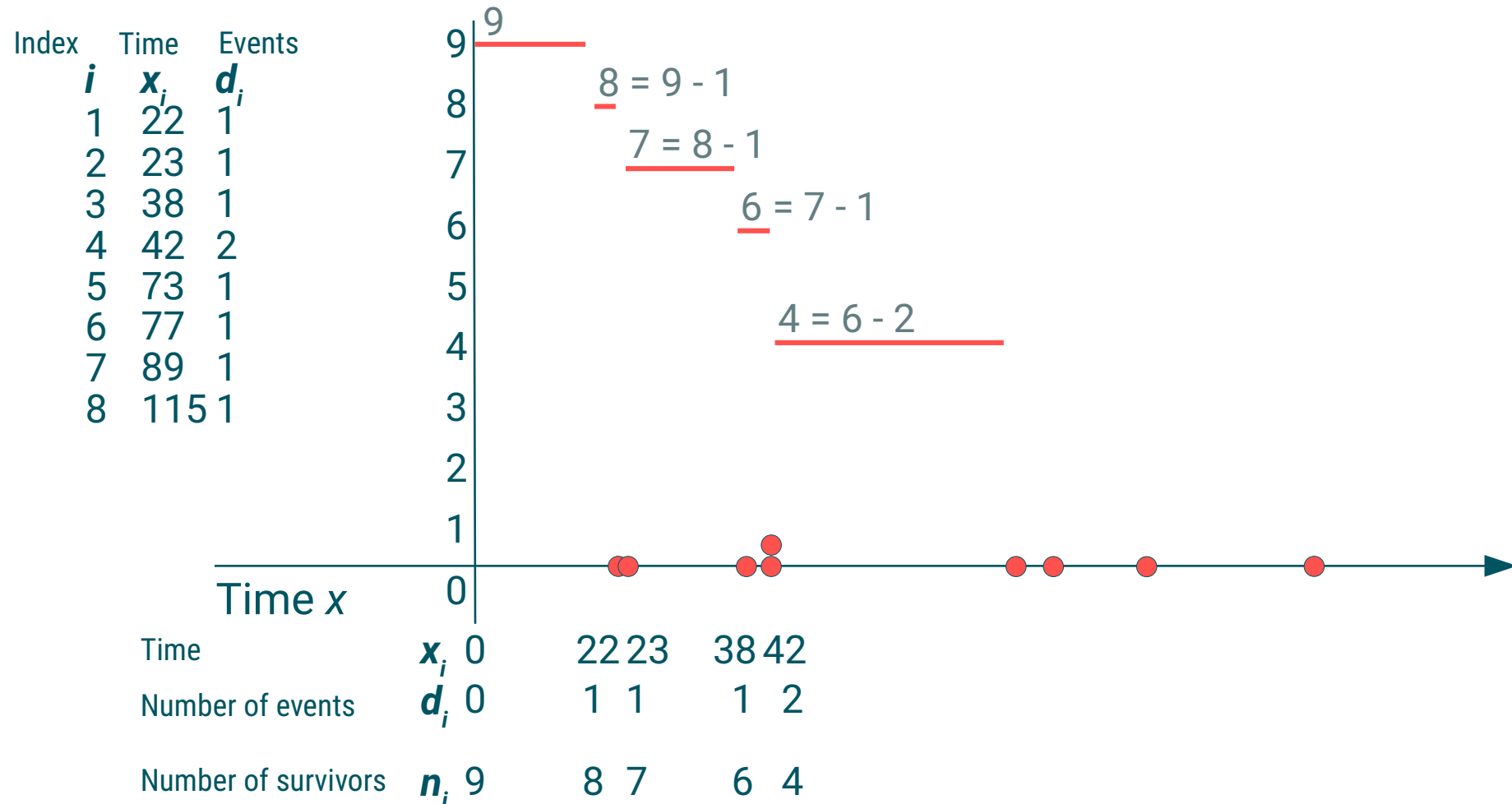
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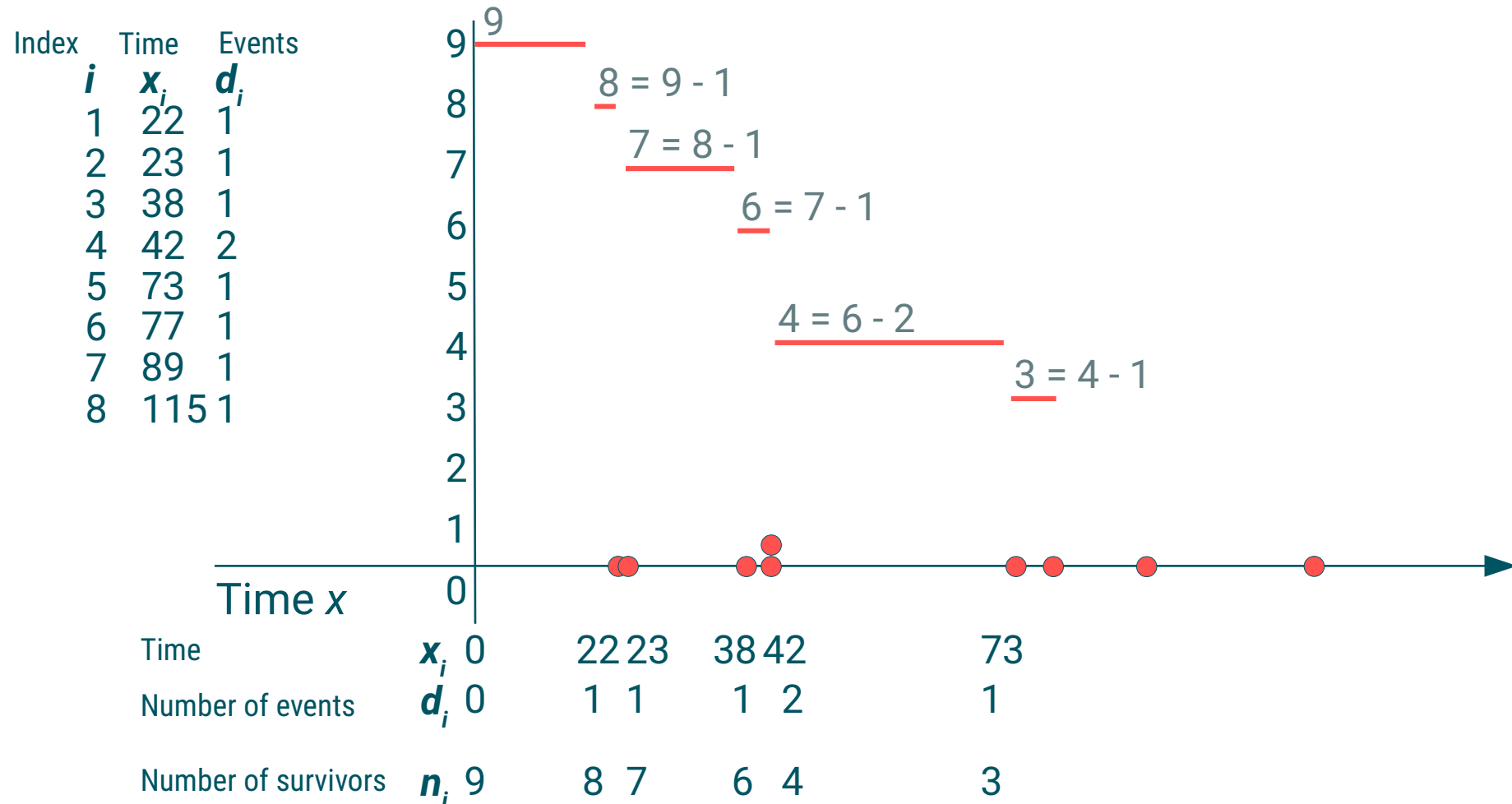
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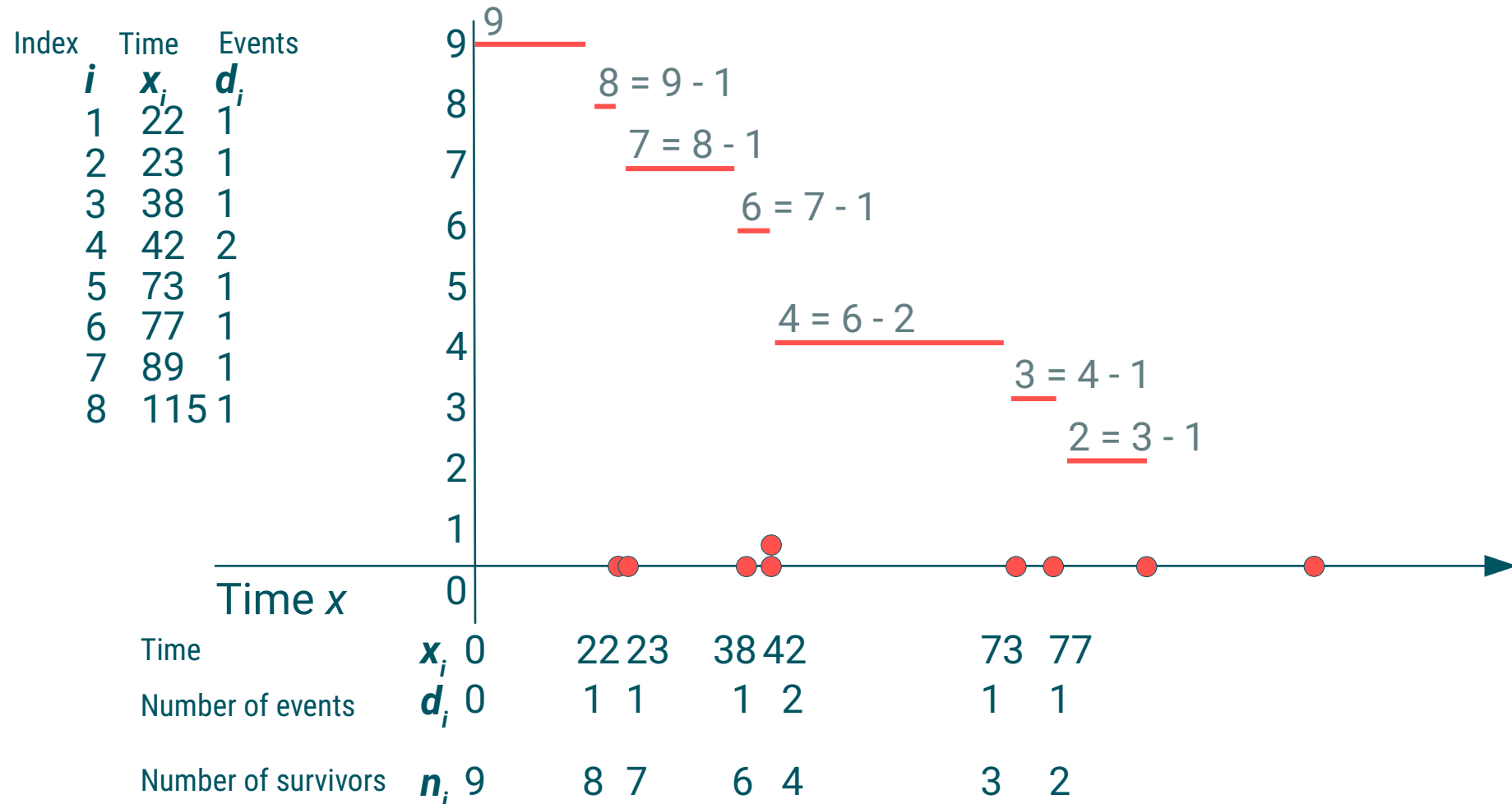
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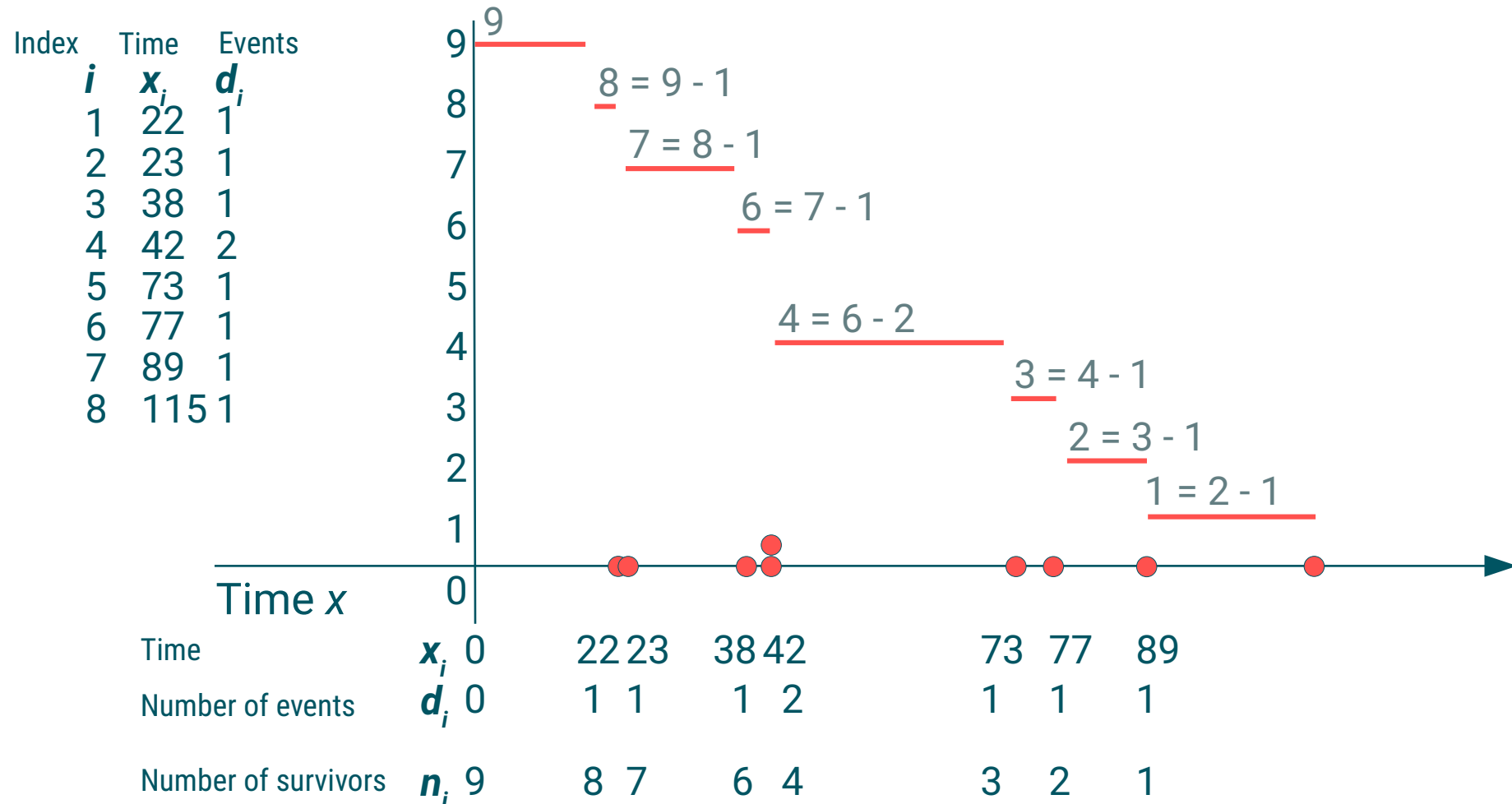
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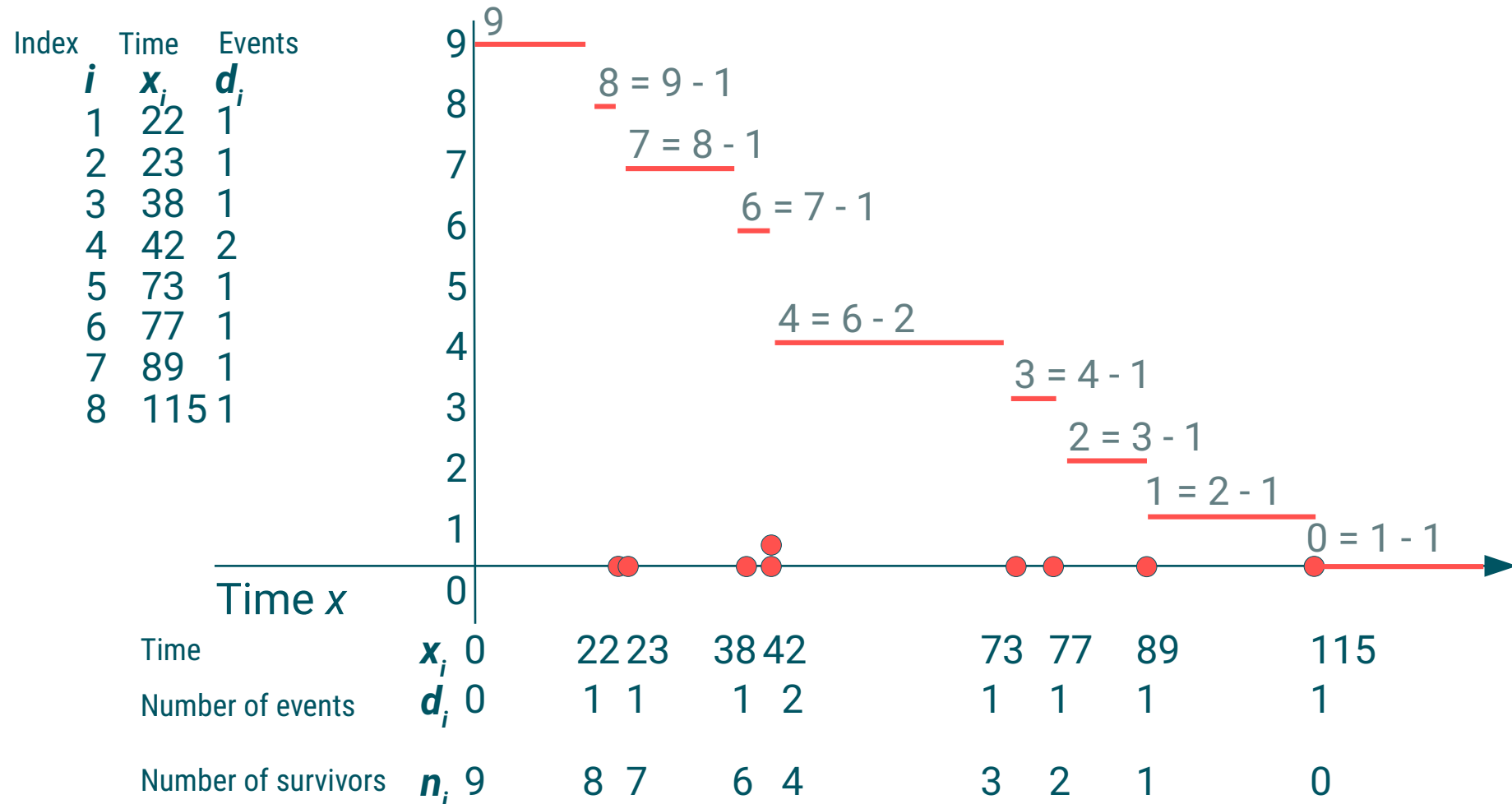
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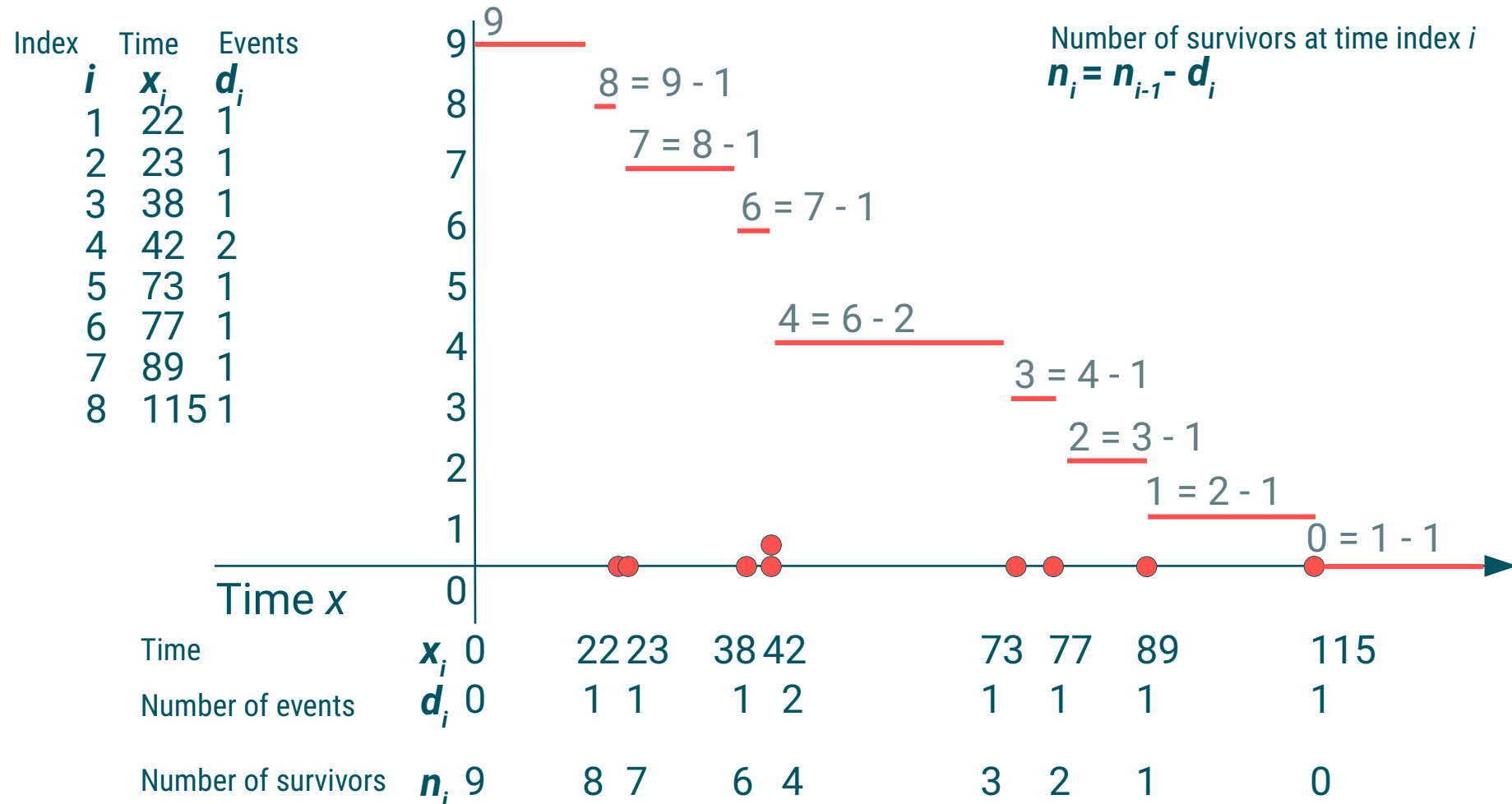
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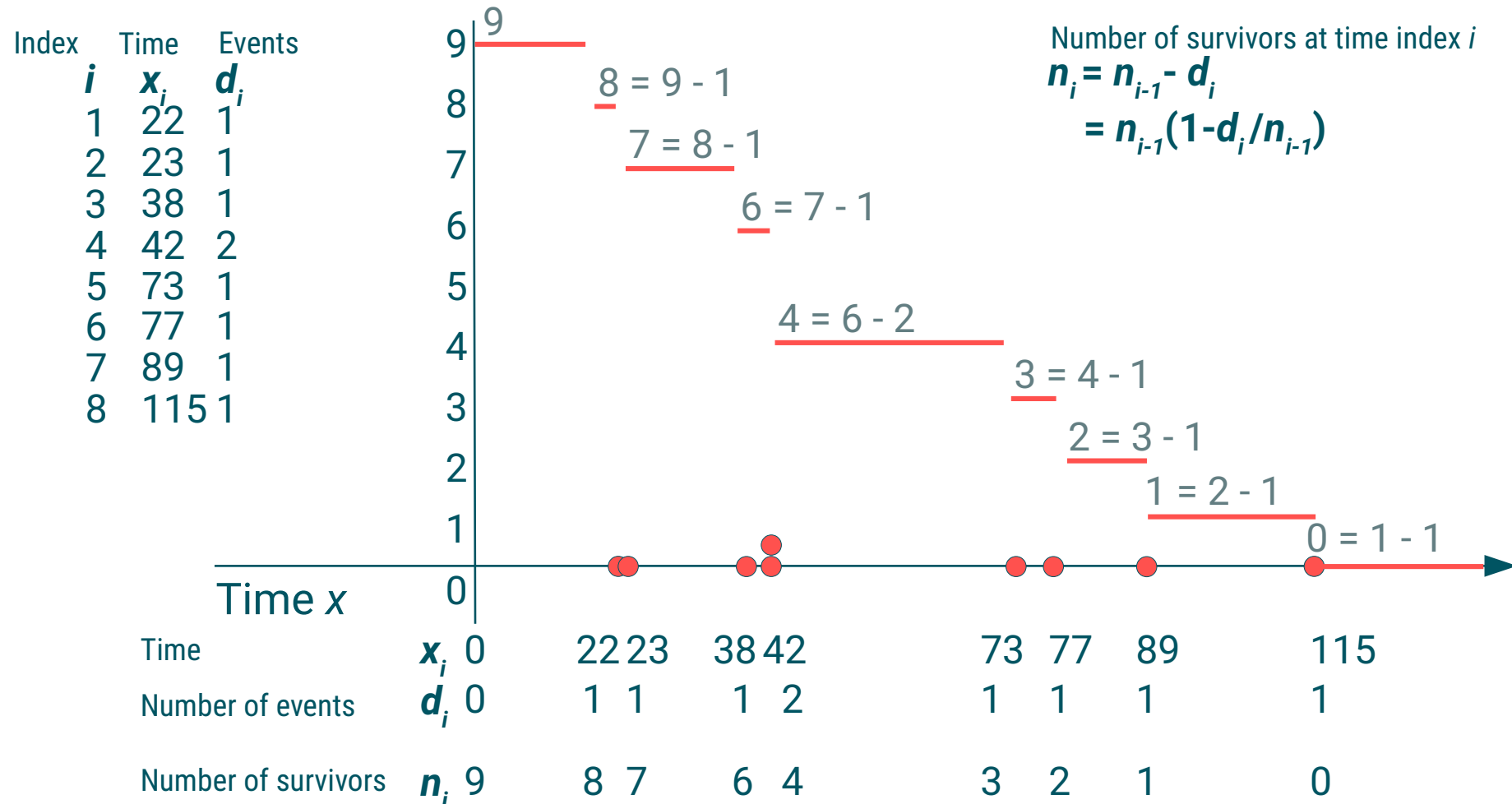
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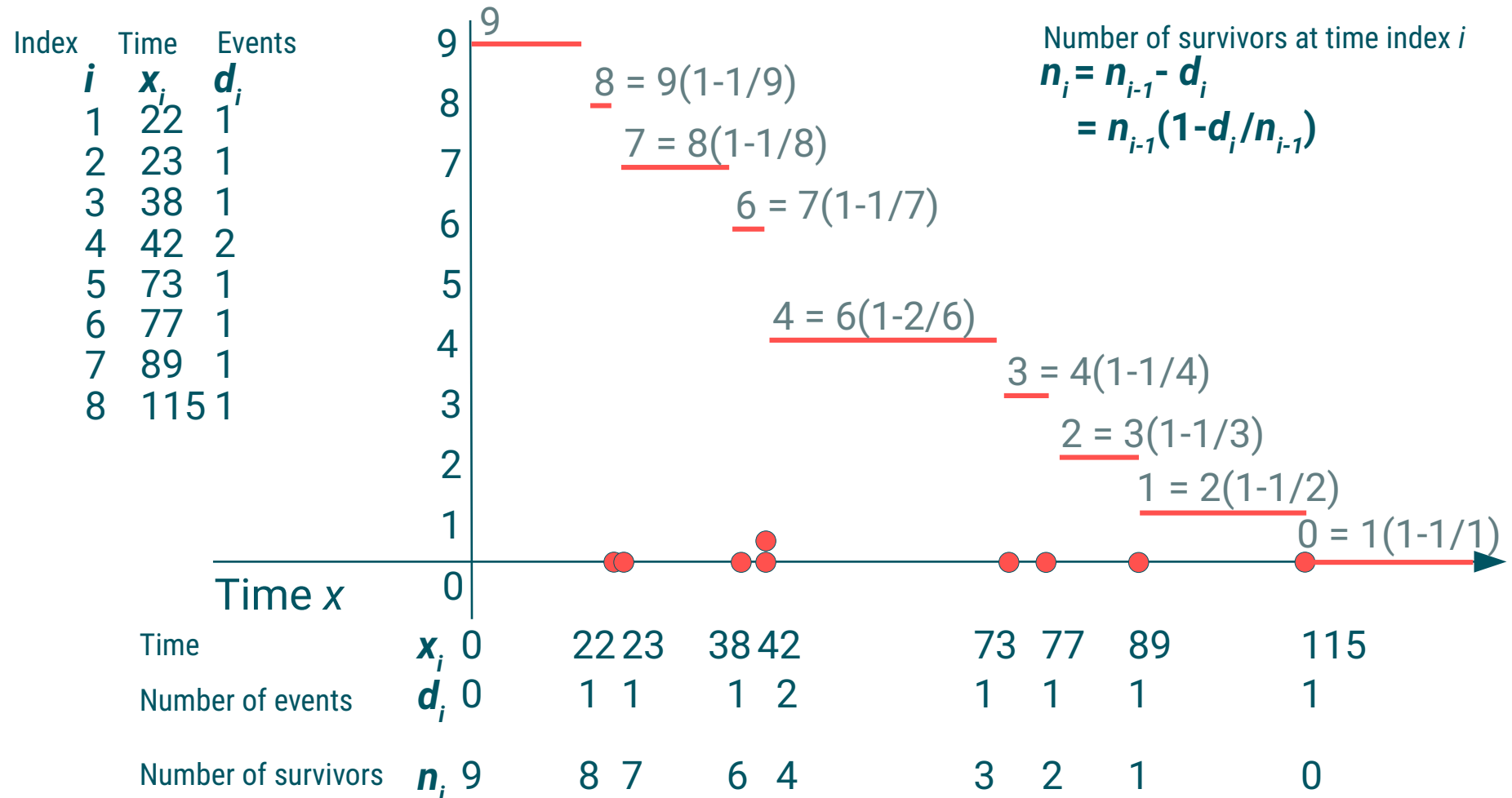
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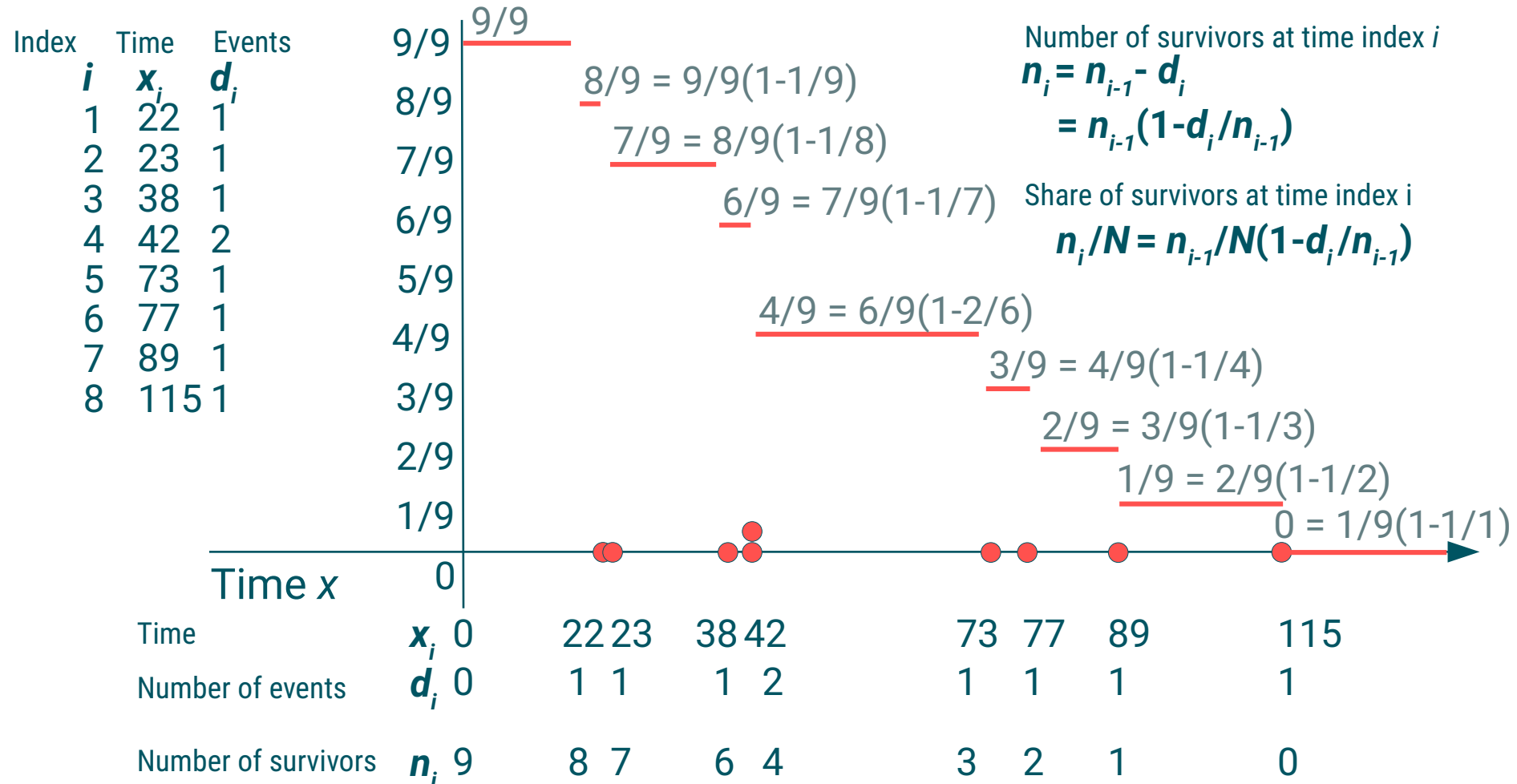
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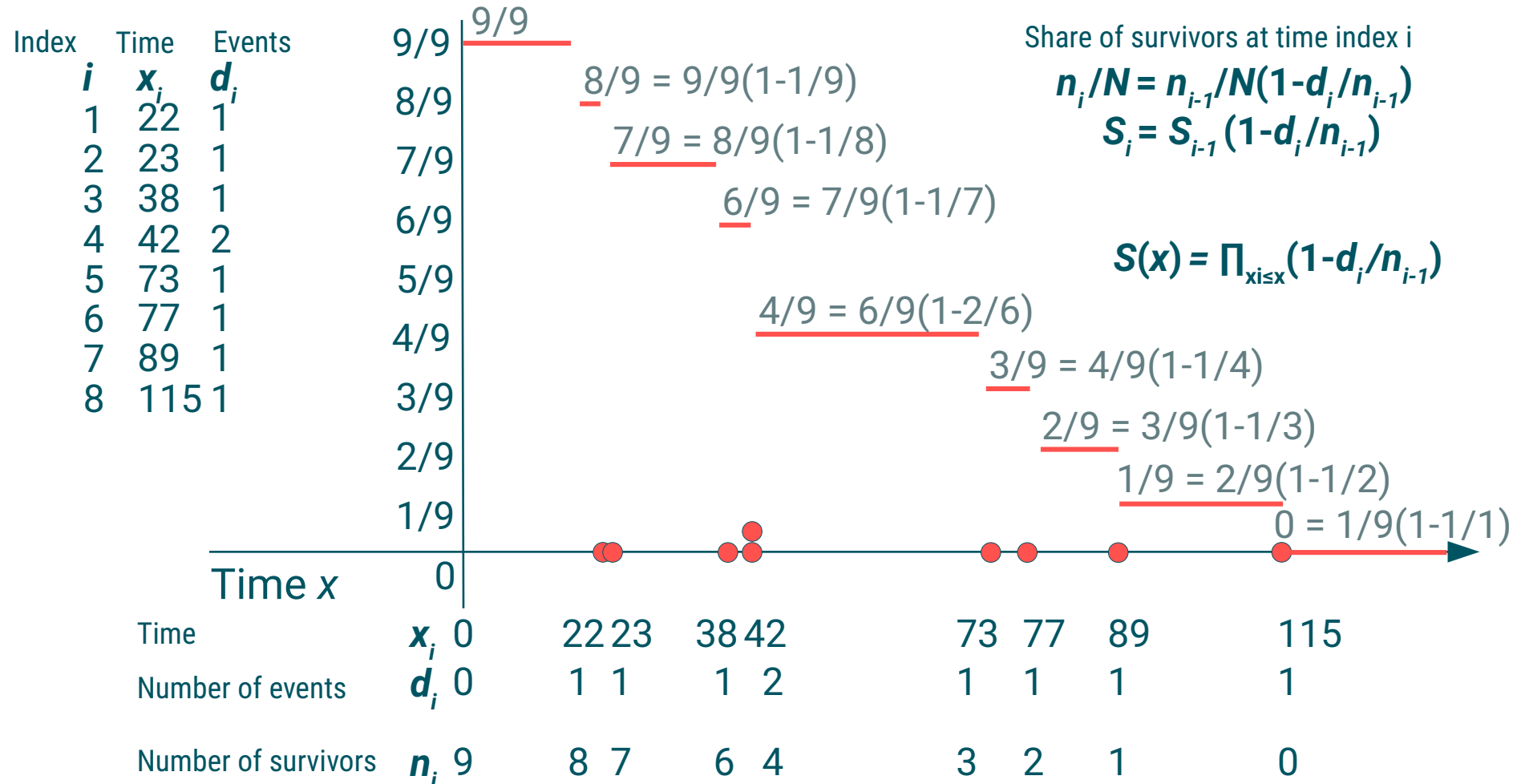
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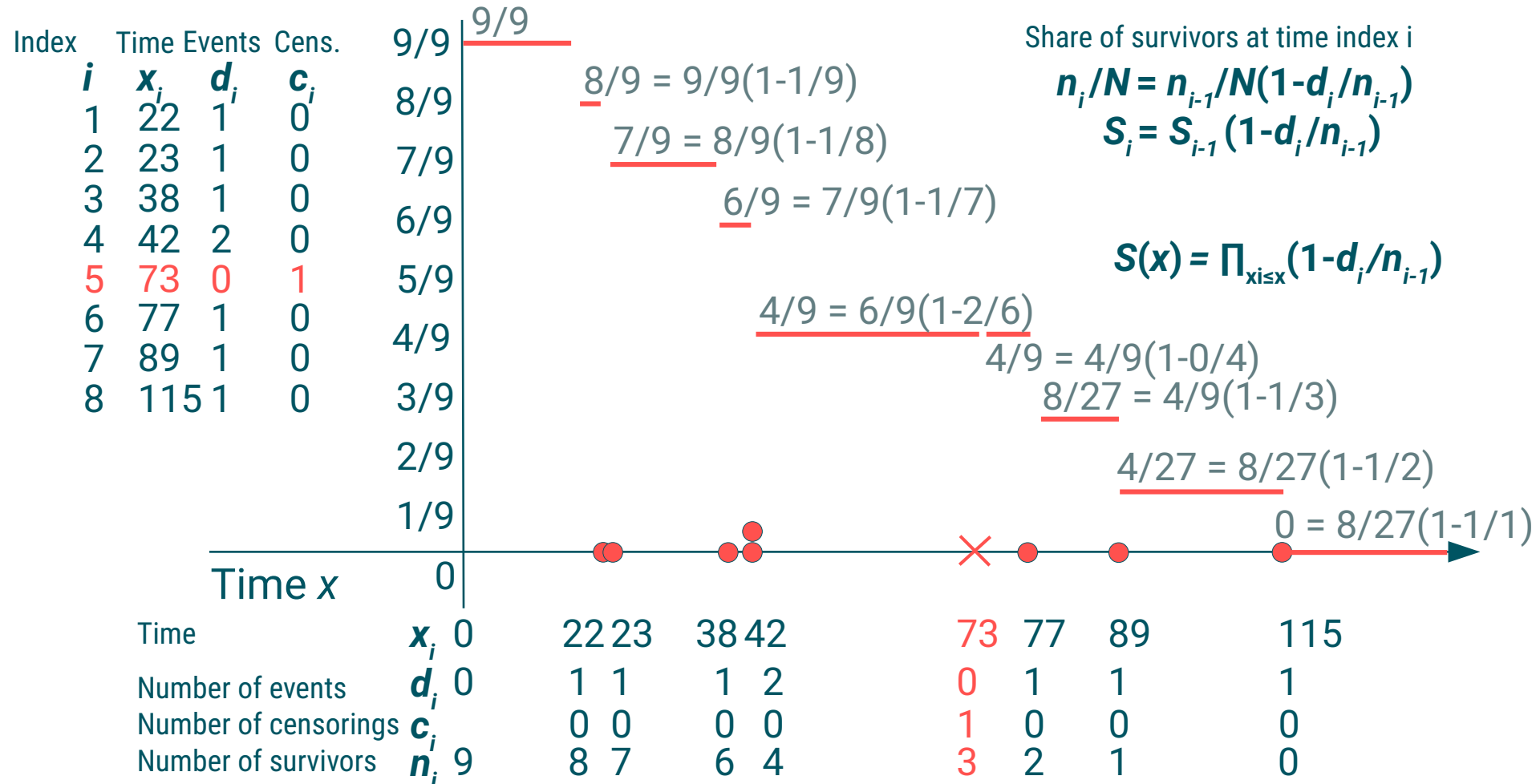
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Recap

For the Kaplan-Meier Estimator read

Klein & Moeschberger (2003). Survival Analysis. pp. 91–93.

Homework

Using R, produce a Kaplan-Meier plot related to the topic of your eventual seminar paper (“Hausarbeit”).

You don't need to have all the data for your topic yet, but you need to find “some” related data. Be prepared to present your plot to the group. Think about study time start and end, event of interest, and censoring. You may compare multiple groups, but a KM-plot for a single group is fine as well.

Materials for this lecture

github.com/jschoeley/survival_analysis-ur-ss22

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