

```

In[63]:= img1 = Import["/Users/rhariadi/Downloads/NonPurified_6hx001.xlsx"];
(*img2=Import["/Users/rhariadi/Downloads/Purified_6hx001.xlsx"];*)

In[64]:= data1 = Flatten[img1[[1]]];
(*data2=Flatten[img2[[1]]];*)

In[65]:= (*ListDensityPlot[img1[[1]]];*)

In[66]:= sortedData1 = Sort[data1];
(*sortedData2=Sort[data2];*)

In[67]:= n = Length[sortedData1]

Out[67]= 262 144

In[68]:= cdfData1 = Table[{sortedData1[[i]] 109,  $\frac{i}{n}$ }, {i, n}];
(*cdfData2=Table[{sortedData2[[i]] 109,  $\frac{i}{n}$ }, {i, n}];*)

In[69]:= nlm = NonlinearModelFit[cdfData1,
  {a CDF[NormalDistribution[ $\mu$ 1,  $\sigma$ 1], x] + (1 - a) CDF[NormalDistribution[ $\mu$ 2,  $\sigma$ 2], x],
  10 >  $\mu$ 2 >  $\mu$ 1 > -5, 0 < a < 1}, {{a, 0.5}, { $\mu$ 1, -1}, { $\sigma$ 1, 2}, { $\mu$ 2, 1}, { $\sigma$ 2, 3}}, x]

Out[69]= FittedModel[ $0.185334 \operatorname{Erfc}[4.40401 \times (-0.758575 - x)] + 0.314666 \operatorname{Erfc}[1.33745 \times (0.399374 - x)]$ ]

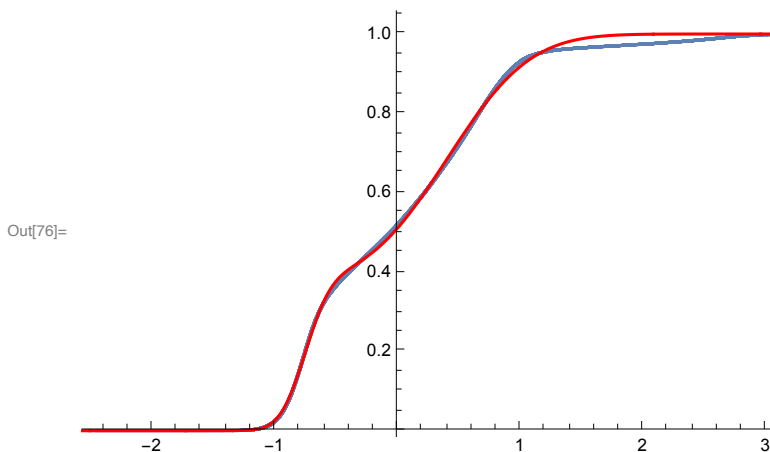
In[70]:= nlm["BestFitParameters"]

Out[70]= {a → 0.370668,  $\mu$ 1 → -0.758575,  $\sigma$ 1 → 0.16056,  $\mu$ 2 → 0.399374,  $\sigma$ 2 → 0.528696}

In[71]:= aFit = nlm["BestFitParameters"][[1, 2]];
 $\mu$ 1Fit = nlm["BestFitParameters"][[2, 2]];
 $\sigma$ 1Fit = nlm["BestFitParameters"][[3, 2]];
 $\mu$ 2Fit = nlm["BestFitParameters"][[4, 2]];
 $\sigma$ 2Fit = nlm["BestFitParameters"][[5, 2]];

In[76]:= Show[ListLinePlot[cdfData1], Plot[aFit CDF[NormalDistribution[ $\mu$ 1Fit,  $\sigma$ 1Fit], x] +
  (1 - aFit) CDF[NormalDistribution[ $\mu$ 2Fit,  $\sigma$ 2Fit], x], {x, -10, 10}, PlotStyle → Red]]

```



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In[77]:= nlm = NonlinearModelFit[cdfData1,
  {a CDF[NormalDistribution[μ1, σ1], x] + (b) CDF[NormalDistribution[μ2, σ2], x] +
    (c) CDF[NormalDistribution[μ3, σ3], x], 10 > μ3 > μ2 > μ1 > -1,
    0 < μ3 < 4,
    a + b + c == 1,
    0 < a < Min[{1.2 aFit, 1}],
    0 < b < Min[{1.2 × (1 - aFit), 1}],
    0.005 < c < 0.1,
    1.2 σ1Fit > σ1 > 0.8 σ1Fit,
    1.2 σ2Fit > σ2 > 0.8 σ2Fit,
    2 > σ3 > 0,
    0.8 μ2Fit < μ2 < 1.2 μ2Fit,
    0.8 μ1Fit > μ1 > 1.2 μ1Fit},
  {{a, aFit}, {μ1, μ1Fit}, {σ1, σ1Fit},
    {b, 1 - aFit}, {μ2, μ2Fit}, {σ2, σ2Fit}, {μ3, 2}, {σ3, σ1Fit}, c}, x]
```

```
Out[77]= FittedModel [ 0.188077 Erfc[4.34424 × (-0.756952 - x)] + <<19>> <<1>> + 0.00437168 Erfc[6.33799 × (2.84343 - x)] ]
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In[78]:= Min[{1, 2}]
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Out[78]= 1
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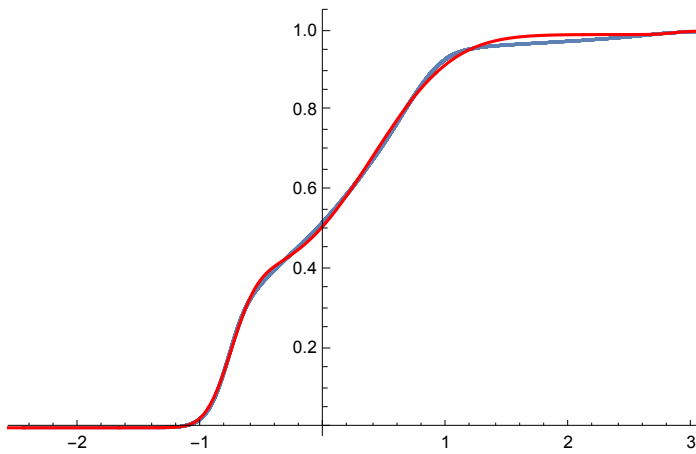
```
In[79]:= nlm["BestFitParameters"]
```

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Out[79]= {a → 0.376154, μ1 → -0.756952, σ1 → 0.162769, b → 0.615102,
  μ2 → 0.395529, σ2 → 0.512496, μ3 → 2.84343, σ3 → 0.111566, c → 0.00874336}
```

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In[80]:= aFit = nlm["BestFitParameters"][[1, 2]];
μ1Fit = nlm["BestFitParameters"][[2, 2]];
σ1Fit = nlm["BestFitParameters"][[3, 2]];
bFit = nlm["BestFitParameters"][[4, 2]];
μ2Fit = nlm["BestFitParameters"][[5, 2]];
σ2Fit = nlm["BestFitParameters"][[6, 2]];
μ3Fit = nlm["BestFitParameters"][[7, 2]];
σ3Fit = nlm["BestFitParameters"][[8, 2]];
cFit = nlm["BestFitParameters"][[9, 2]];
```

```
In[89]:= Show[ListLinePlot[cdfData1], Plot[aFit CDF[NormalDistribution[ $\mu$ 1Fit,  $\sigma$ 1Fit], x] +
  (bFit) CDF[NormalDistribution[ $\mu$ 2Fit,  $\sigma$ 2Fit], x] +
  (cFit) CDF[NormalDistribution[ $\mu$ 3Fit,  $\sigma$ 3Fit], x], {x, -10, 10}, PlotStyle → Red]]
```

Out[89]=



```
In[90]:= Show[Histogram[sortedData1 109],
  Plot[40 000 aFit PDF[NormalDistribution[ $\mu$ 1Fit,  $\sigma$ 1Fit], x] +
    40 000 (bFit) PDF[NormalDistribution[ $\mu$ 2Fit,  $\sigma$ 2Fit], x] +
    40 000 (cFit) PDF[NormalDistribution[ $\mu$ 3Fit,  $\sigma$ 3Fit], x],
  {x, -10, 10}, PlotStyle → Red, PlotRange → All]]
```

General:  $15046.21660130587728 \times 10^{-700}$  is too small to represent as a normalized machine number; precision may be lost.

General:  $349.7341016434372514 \times 10^{-2877}$  is too small to represent as a normalized machine number; precision may be lost.

Out[90]=

