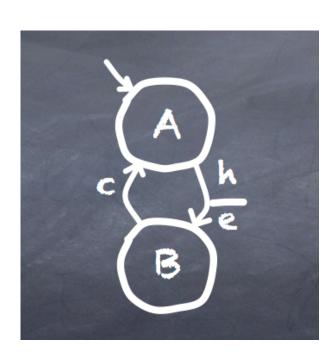
RFSM Reference Manual - 2.0

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Formal syntax of RFSM programs

This appendix gives a BNF definition of the concrete syntax RFSM programs. As stated in the introduction, this syntax is that of the so-called standard RFSM language. Variant languages will essentially differ in the definition of the $\langle type_decl \rangle$, $\langle type_expr \rangle$, $\langle expr \rangle$, $\langle constant \rangle$, and $\langle const \rangle$ syntactical categories.

The meta-syntax is conventional. Keywords are written in **boldface**. Non-terminals are enclosed in angle brackets (<...>). Vertical bars (|) indicate alternatives. Constructs enclosed in non-bold brackets ([...]) are optional. The notation E^* (resp E^+) means zero (resp one) or more repetitions of E, separated by spaces. The notation E^*_x (resp E^+_x) means zero (resp one) or more repetitions of E, separated by symbol x. Terminals lid and uid respectively designate identifiers starting with a lowercase and uppercase letter.

```
\langle program \rangle ::=
                                                  \langle \text{type\_decl} \rangle^*
                                                   \langle \text{cst\_decl} \rangle^*
                                                   \langle \text{fn\_decl} \rangle^*
                                                   \langle fsm\_model \rangle^*
                                                   \langle \text{fsm\_model} \rangle^*
                                                   ⟨global⟩*
                                                   \langle fsm inst \rangle^*
    \langle \text{type\_decl} \rangle ::= \text{type lid} = \langle \text{type\_expr} \rangle
                                                  \mathbf{type} \ \mathrm{lid} = \mathbf{enum} \ \{ \ \mathrm{uid}_{\cdot}^* \ \}
                                                  type lid = record { \langle record\_field \rangle^+ }
\langle \operatorname{record\_field} \rangle ::=
                                               lid : \langle type\_expr \rangle
                                                  \mathbf{constant} \ \mathrm{lid} \ : \langle \mathrm{type\_expr} \rangle = \langle \mathrm{const} \rangle
        \langle \text{cst\_decl} \rangle
                                     ::=
          \langle \text{fn\_decl} \rangle
                                                  function lid (\langle farg \rangle_{\bullet}^*) : \langle type\_expr \rangle { return \langle expr \rangle }
                   \langle farg \rangle
                                                  lid: \langle type\_expr \rangle
                                     ::=
                                                  fsm model \langle id \rangle [\langle params \rangle] (\langle io \rangle^*) {
  \langle fsm\_model \rangle
                                    ::=
                                                  states : \langle state \rangle^*;
                                                   [\langle vars \rangle]
                                                  trans : \langle \text{transition} \rangle_{,}^{*};
                                                  itrans : (itransition) ;
                 \langle \text{state} \rangle ::= \text{uid } [\text{where} \langle \text{outp\_val} \rangle_{\text{and}}^+]
       \langle \text{outp\_val} \rangle ::= \text{lid} = \langle \text{scalar\_const} \rangle
           \langle params \rangle ::= \langle param \rangle^* >
             \langle param \rangle ::=
                                               lid : \langle type\_expr \rangle
                        \begin{array}{rll} \langle \mathrm{io} \rangle & ::= & \mathbf{in} \ \langle \mathrm{io\_desc} \rangle \\ & | & \mathbf{out} \ \langle \mathrm{io\_desc} \rangle \\ & | & \mathbf{inout} \ \langle \mathrm{io\_desc} \rangle \end{array}
          \langle io \ desc \rangle ::= lid : \langle type \ expr \rangle
                   \langle \text{vars} \rangle ::= \text{vars} : \langle \text{var} \rangle_{\cdot}^*;
                     \langle var \rangle ::= lid_{\cdot}^{+} : \langle type\_expr \rangle
      \langle \text{transition} \rangle ::= \langle \text{rule\_prefix} \rangle \text{ uid } -> \text{ uid } \langle \text{condition} \rangle [\langle \text{actions} \rangle]
```

```
\langle \text{rule prefix} \rangle ::= | | !
          \langle \text{condition} \rangle ::= \mathbf{on} \text{ lid } [\langle \text{guards} \rangle]
                \langle \text{guards} \rangle ::= \mathbf{when} \langle \text{expr} \rangle_{+}^{+}
                \langle actions \rangle ::=
                                                       with (action)<sup>+</sup>
                  \langle action \rangle ::=
                                                       \operatorname{lid}
                                                        \langle lhs \rangle := \langle expr \rangle
                          \langle lhs \rangle ::= lid
                                              \begin{array}{c|c} | & \operatorname{lid} \left[ \left\langle \operatorname{expr} \right\rangle \right] \\ | & \operatorname{lid} \left[ \left\langle \operatorname{expr} \right\rangle : \left\langle \operatorname{expr} \right\rangle \right] \\ | & \operatorname{lid} \cdot \operatorname{lid} \end{array} 
        \langle itransition \rangle ::= | -> uid [\langle actions \rangle]
                  \langle \text{global} \rangle ::= \text{input } \langle \text{id} \rangle : \langle \text{type\_expr} \rangle = \langle \text{stimuli} \rangle
                                             output \langle id \rangle_{+}^{+} : \langle type\_expr \rangle
| shared \langle id \rangle_{+}^{+} : \langle type\_expr \rangle
                \langle \operatorname{stimuli} \rangle ::= \operatorname{\mathbf{periodic}} (\operatorname{\mathbf{int}}, \operatorname{\mathbf{int}}, \operatorname{\mathbf{int}})
                                                       sporadic (int, )
value_changes ( \( \text{value_change} \), \( \)
\langle value\_change \rangle ::= int : \langle stim\_const \rangle
           \langle \mathrm{fsm\_inst}\rangle \ ::= \ \mathbf{fsm} \ \langle \mathrm{id}\rangle = \langle \mathrm{id}\rangle \ [<\langle \mathrm{param\_value}\rangle_{,}^{+}>] \ (\ \langle \mathrm{id}\rangle_{,}^{*}\ )
(param_value)
                                                       \langle scalar\_const \rangle
       \langle type\_expr \rangle ::= event
                                                       int (int_annot)
                                                        float
                                                        char
                                                        bool
                                                        ⟨type_expr⟩ array [ ⟨array_size⟩ ]
        \langle \text{int\_annot} \rangle ::= \epsilon
                                                       \langle array\_size \rangle ::= \langle type\_size \rangle
```

```
\langle type\_size \rangle ::= int
                                                      lid
                    \langle \exp r \rangle ::=
                                                       \langle \text{simple}\_\text{expr} \rangle
                                                        \langle \exp r \rangle + \langle \exp r \rangle
                                                        \langle \exp r \rangle - \langle \exp r \rangle
                                                        \langle \exp r \rangle * \langle \exp r \rangle
                                                        \langle expr \rangle / \langle expr \rangle
                                                        ⟨expr⟩ % ⟨expr⟩
                                                        \langle \exp r \rangle = \langle \exp r \rangle
                                                        \langle \exp r \rangle ! = \langle \exp r \rangle
                                                        \langle \exp r \rangle > \langle \exp r \rangle
                                                        \langle \exp r \rangle < \langle \exp r \rangle
                                                        \langle \exp r \rangle >= \langle \exp r \rangle
                                                        \langle \exp r \rangle \ll \langle \exp r \rangle
                                                        \langle expr \rangle & \langle expr \rangle
                                                        \langle \mathrm{expr} \rangle | | \langle \mathrm{expr} \rangle
                                                        \langle \exp r \rangle \hat{} \langle \exp r \rangle
                                                        \langle \exp r \rangle >> \langle \exp r \rangle
                                                        \langle \exp r \rangle \ll \langle \exp r \rangle
                                                        \langle \exp r \rangle + . \langle \exp r \rangle
                                                        \langle \exp r \rangle -. \langle \exp r \rangle
                                                        \langle \exp r \rangle *. \langle \exp r \rangle
                                                        \langle \exp r \rangle /. \langle \exp r \rangle
                                                        \langle \text{subtractive} \rangle \langle \text{expr} \rangle
                                                       lid [\langle \exp r \rangle]
                                                      lid [ \langle \exp r \rangle : \langle \exp r \rangle ]
                                                      lid (\langle \exp r \rangle_{,}^*)
                                                      lid . lid
                                                       \langle \exp r \rangle ? \langle \exp r \rangle : \langle \exp r \rangle
                                                       \langle \exp r \rangle :: \langle type\_expr \rangle
\langle simple\_expr \rangle ::=
                                                   \operatorname{lid}
                                                       uid
                                                       \langle scalar\_const \rangle
                                                        ( \langle \exp r \rangle )
   \langle subtractive \rangle ::=
\langle scalar\_const \rangle ::=
                                                      int
                                                      bool
                                                       float
                                                       char
                  \langle const \rangle ::= \langle scalar\_const \rangle
                                                       \langle array\_const \rangle
```

Formal semantics

We here give the formal *static* and *dynamic* semantics for a simplified version of the RFSM language, called CORE RFSM. Compared to the "standard" RFSM language¹, it lacks type, constant and function declarations, state valuation and has only basic types. Its abstract syntax is described below. We note X^* (resp. X^+) the repetition of 0 (resp. 1) or more X. The syntax of expressions is deliberately not explicited here.

```
program fsm_model^+ io_decl^+ fsm_inst^+
program ::=
                      fsm model id inp^* outp^* state^+ var^* trans^+ itrans
fsm\_model ::=
state ::=
                      id
inp, outp, var ::= id : typ
                      \langle id, cond, action^*, id \rangle
                                                                                     \langle src\ state, cond, actions, dst\ state \rangle
trans ::=
cond ::=
                      \langle id, guard^* \rangle
                                                                                     \langle triggering \ even, guards \rangle
guard ::=
                                                                                     boolean expression
                      expr
action ::=
                       id
                                                                                     emit event
                      | id := expr
                                                                                     update local, shared or output variable
io\_decl ::=
                      io\_cat \ \mathtt{id} : typ
io \ cat ::=
                      input | input | shared
                      fsm id i^* o^*
                                                                                    model, IO bindings
fsm\ inst ::=
                      event | int | bool
typ ::=
```

2.1 Common definitions

Both the static and static semantics will use *environments*. An **environment** is a (partial) map from names to values. If Γ is an environment and x a name, we will, classically, note

- $x \in \Gamma$ if $x \in \text{dom}(\Gamma)$,
- $\Gamma(x)$ the value mapped to x in $\Gamma(\Gamma(x) = \bot$ if $x \notin \Gamma$),

¹Described in the User Manual.

- $\Gamma[x \mapsto v]$ the environment that maps x to v and behaves like Γ otherwise (possibly overriding an existing mapping of x),
- Ø the empty environment,

2.2 Static semantics

The static interpretation of a Core Resm program is a pair

$$\mathcal{H} = \langle M, C \rangle$$

where

- *M* is a set of **automata**,
- C is a context.
- ▶ A context is a 6-tuple $\langle I_e, I_v, O_e, O_v, H_e, H_v \rangle$ where
 - I_e (resp. O_e , H_e) is the set of global inputs (resp. outputs, shared values) with an event type,
 - I_v (resp. O_v , H_v) is the set of global inputs (resp. outputs, shared values) with a non-event type.
- ▶ An automaton $\mu \in M$ is a 3-tuple

$$\mu = \langle \mathcal{M}, q, \mathcal{V} \rangle$$

where

- \mathcal{M} is the associated (static) model,
- q its current state,
- \bullet \mathcal{V} an environment giving the current value of its local variables.
- ightharpoonup A model \mathcal{M} is a 6-tuple

$$\mathcal{M} = \langle Q, I, O, V, T, \tau_0 \rangle$$

where

- Q is a (finite) set of states,
- I and O are environments respectively mapping input and output names to types,
- \bullet V is an environment mapping local variable names to types,
- $I_e = \{x \in I \mid I(x) = \text{event}\} \text{ and } I_v = \{x \in I \mid I(x) \neq \text{event}\},$
- $O_e = \{x \in O \mid O(x) = \text{event}\}\ \text{and}\ O_v = \{x \in O \mid O(x) \neq \text{event}\},$
- $T \subset Q \times C \times \mathcal{S}(A) \times Q$ is a set of **transitions**, where $-C = I_e \times 2^{\mathcal{B}(I_v \cup V)}$,

- $-\mathcal{B}(E)$ is the set of boolean expressions built from a set of variables E and the classical boolean operators²,
- $-\mathcal{S}(A)$ is the set of sequences built from elements of the set A, where a sequence \vec{a} is an ordered collection $\langle a_1; \ldots; a_n \rangle^3$,
- $-A = \mathcal{U}(O_v \cup V, I_v \cup V) \cup O_e,$
- $-\mathcal{U}(E, E')$ is the set of assignations of variables taken in a set E by expressions built from a set of variable E' and the classical boolean and arithmetic operators and constants⁴.
- $\tau_0 \in Q \times \mathcal{S}(\mathcal{U}(O_v \cup V, \emptyset))$ is the initial transition.

Having $\tau = (q, c, \vec{a}, q')$ in T means that there's a transition from state q to state q' enabled by the condition c and triggering a (possibly empty) sequence \vec{a} , where

- the condition $c \in C$ is made of
 - a trigerring event $e \in I_e$,
 - a (possibly empty) set of boolean expressions (guards), involving inputs having a non-event type or local variables,
- the actions in \vec{a} consist either in the emission of an event or the modification of an output or local variable.

The initial transition τ_0 consists in a state (the initial state) and a (possibly empty) sequence of initial actions. Contrary to actions associated to "regular" transitions, initial actions cannot not emit events and the assigned values cannot depend on inputs or local variables.

Example. The model of the automaton depicted below⁵ can be formally described as $\mathcal{M} = \langle Q, I, O, V, T, \tau_0 \rangle$ where :

•
$$Q = \{E0, E1\}$$

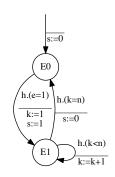
•
$$I = \{h \mapsto \mathsf{event}, e \mapsto \mathsf{bool}\}$$

•
$$O = \{s \mapsto \mathsf{bool}\}$$

•
$$V = \{k \mapsto \mathsf{bool}\}$$

•
$$T = \{ \langle E0, \langle H, \{e=0\} \rangle, \langle \rangle, E0 \rangle, \langle E0, \langle H, \{e=1\} \rangle, \langle s \leftarrow 1; k \leftarrow 1 \rangle, E1 \rangle, \langle E1, \langle H, \{k < 3\} \rangle, \langle k \leftarrow k + 1 \rangle, E1 \rangle, \langle E1, \langle H, \{k = 3\} \rangle, \langle s \leftarrow 0 \rangle, E0 \rangle \}$$

•
$$\tau_0 = \langle E0, \langle s \leftarrow 0 \rangle \rangle$$



 $^{^2{\}rm This}$ set can be formally derived from the abstract syntax.

³For example, if $A = \{1, 2\}$, then $S(A) = \{\langle \rangle, \langle 1 \rangle, \langle 2 \rangle, \langle 1; 1 \rangle, \langle 1; 2 \rangle, \langle 2; 1 \rangle, \langle 2; 2 \rangle, \langle 1; 2; 1 \rangle, \ldots \}$, where $\langle \rangle$ denotes the empty sequence.

⁴Again, this can be formally derived from the abstract syntax.

⁵This model, a calibrated pulse generator has been introduced in the *Overview* chapter of the user manual.

Rules

▶ Rule PROGRAM gives the static interpretation of a program. The static environment Γ_M (resp. Γ_I) records the (typed) declarations of models (resp. IOs).

$$\begin{split} fsm_model^+ &\to \Gamma_{\rm M} \\ io_decl^+ &\to \Gamma_{\rm I} \\ \Gamma_{\rm M}, \Gamma_{\rm I} &\vdash fsm_inst^+ \to M \\ C &= \mathcal{L}(\Gamma_{\rm I}) \\ \hline \text{program } fsm_model^+ \ io_decl^+ \ fsm_inst^+ \to M, C \end{split} \tag{Program}$$

The \mathcal{L} function builds a static context C from the IO environment $\Gamma_{\rm I}$:

$$\mathcal{L}(\Gamma_{\rm I}) = \langle I_e, I_v, O_e, O_v, H_e, H_v \rangle$$

where

$$\begin{split} I_e &= \{x \in \mathrm{dom}(\Gamma_{\!\!\mathsf{I}}) \mid \Gamma_{\!\!\mathsf{I}}(x) = \langle \mathrm{input}, \mathrm{event} \rangle \} \\ O_e &= \{x \in \mathrm{dom}(\Gamma_{\!\!\mathsf{I}}) \mid \Gamma_{\!\!\mathsf{I}}(x) = \langle \mathrm{output}, \tau \rangle, \ \tau \neq \mathrm{event} \} \\ H_e &= \{x \in \mathrm{dom}(\Gamma_{\!\!\mathsf{I}}) \mid \Gamma_{\!\!\mathsf{I}}(x) = \langle \mathrm{output}, \tau \rangle, \ \tau \neq \mathrm{event} \} \\ H_v &= \{x \in \mathrm{dom}(\Gamma_{\!\!\mathsf{I}}) \mid \Gamma_{\!\!\mathsf{I}}(x) = \langle \mathrm{shared}, \mathrm{event} \rangle \} \\ \end{split}$$

 \blacktriangleright Rule Models gives the interpretation of model declarations, giving an environment Γ_{M} .

$$\forall i \in \{1, \dots, n\} \qquad \Gamma_{\mathsf{M}}^{i-1}, \ fsm_model_i \to \Gamma_{\mathsf{M}}^i$$

$$\frac{\Gamma_{\mathsf{M}}^0 = \emptyset \quad \Gamma_{\mathsf{M}} = \Gamma_{\mathsf{M}}^n}{fsm_model_1, \dots, fsm_model_n \to \Gamma_{\mathsf{M}}}$$
(Models)

- ▶ Rule Model gives the interpretation of a single model declaration. It just records the corresponding description in the environment Γ_M , after performing some sanity checks, using the valid_model function, not detailed here. This function checks that:
 - all variable names occurring in guards are listed as input or local variable,
 - all expressions occuring in the guards of a transition have type bool,

• ... Todo: tbc

$$\frac{\mathcal{M} = \langle Q, I, O, V, T, \tau_0 \rangle \quad \mathsf{valid_model}(\mathcal{M})}{\mathsf{fsm} \; \mathsf{model} \; \mathrm{id} \; I \; O \; Q \; V \; T \; \tau_0 \to \Gamma_{\mathsf{M}}[\mathrm{id} \mapsto \mathcal{M}]} \tag{MODEL}$$

▶ Rules IOs and IO give the interpretation of IO declarations, producing an environment Γ_l binding names to a pair $\langle io_cat, typ \rangle$.

$$\frac{\forall i \in \{1, \dots, n\} \qquad \Gamma_{\mathbf{l}}^{i-1}, \ io_decl_i \to \Gamma_{\mathbf{l}}^i}{\Gamma_{\mathbf{l}}^0 = \emptyset \quad \Gamma_{\mathbf{l}} = \Gamma_{\mathbf{l}}^n} \\
\frac{\Gamma_{\mathbf{l}}^0 = \emptyset \quad \Gamma_{\mathbf{l}} = \Gamma_{\mathbf{l}}^n}{io \quad decl_1, \dots, io \quad decl_n \to \Gamma_{\mathbf{l}}} \tag{IOs}$$

$$\frac{}{\Gamma_{l}, cat id: typ \to \Gamma_{l}[id \mapsto \langle cat, typ \rangle]}$$
 (IO)

▶ Rules Insts gives the interpretation of FSM instance declarations.

$$\forall i \in \{1, \dots, n\} \qquad \Gamma_{\mathsf{M}}, \Gamma_{\mathsf{I}} \vdash fsm_inst_i \to \mu_i$$

$$M = \langle \mu_1; \dots; \mu_n \rangle$$

$$fsm_inst_1, \dots, fsm_inst_n \to \mathcal{H} = \langle M, C \rangle$$

$$(Insts)$$

▶ Rule Inst gives the interpretation of a single FSM instance as an automaton.

$$\begin{split} \Gamma_{\mathsf{M}}(\mathrm{id}) &= \langle \langle i_1' : \tau_1', \dots ; i_m' : \tau_m' \rangle, \langle o_1' : \tau_1'', \dots ; o_n' : \tau_n'' \rangle, Q, V, T, \langle q_0, \vec{a_0} \rangle \rangle \\ \Phi &= \{i_1' \mapsto i_1, \dots, i_m' \mapsto i_m, o_1' \mapsto o_1, \dots, \emptyset_n' \mapsto o_n\} \\ \forall i \in \{1, \dots, m\} \quad \Gamma_{\mathsf{I}}(i_i) &= \langle \mathrm{cat}_i, \tau_i \rangle, \ \mathrm{cat}_i \in \{\mathrm{input}, \mathrm{shared}\} \wedge \tau_i = \tau_i' \\ \forall i \in \{1, \dots, n\} \quad \Gamma_{\mathsf{I}}(o_i) &= \langle \mathrm{cat}_i, \tau_i \rangle, \ \mathrm{cat}_i \in \{\mathrm{output}, \mathrm{shared}\} \wedge \tau_i = \tau_i'' \\ \mathcal{M}' &= \langle \langle i_1 : \tau_1', \dots ; i_m : \tau_m' \rangle, \langle o_1 : \tau_1'', \dots ; o_n : \tau_n'' \rangle, Q, V, \Phi_T(T), \langle q_0, \Phi_A(\vec{a_0}) \rangle \rangle \\ &= \frac{\mu}{\langle \mathcal{M}', q_0, \mathcal{I}(V) \rangle} \\ \Gamma_{\mathsf{M}}, \Gamma_{\mathsf{I}} \vdash \ \mathsf{fsm} \ \mathrm{id} \ \langle i_1; \dots ; i_m \rangle \ \langle o_1; \dots ; o_n \rangle \to \mu \end{split} \tag{INST}$$

Rule INST checks the arity and the type conformance of the inputs and outputs supplied to the instanciated model. The rule builds a *substitution* Φ for binding *local* input and output names to *global* ones. This substitution is applied to each transition (including the initial one) of the resulting automaton using the derived functions Φ_T and Φ_A (not detailed here). The \mathcal{I} function builds an environment from a set of names, initializing each binding with the \bot ("undefined") value:

$$\mathcal{I}(\{x_1,\ldots,x_n\}) = \{x_1 \mapsto \bot,\ldots,x_n \mapsto \bot\}$$

2.3 Dynamic semantic

The dynamic semantics of a Core Rfsm program will be given in terms of (instantaneous) reactions.

$$\mathcal{C} \vdash M, \ \Gamma \xrightarrow{\sigma} M', \ \Gamma'$$

meaning

"in the static context C and given a (dynamic) environment Γ , a set of automata M reacts to a stimulus σ leading to an updated set of automata M', an updated environment Γ' and producing a response ρ "

Definitions

▶ Given an expression e and an environment Γ , $\mathcal{E}_{\Gamma}\llbracket e \rrbracket$ denotes the value obtained by **evaluating** expression e within environment Γ . For example

$$\mathcal{E}_{\{x\mapsto 1,y\mapsto 2\}}[\![x+y]\!]=3$$

▶ An **event** e is either the occurrence of a *pure event* e or the assignation of a **value** v to a **name** (input, output or local variable):

$$e = \begin{cases} \epsilon \\ x \leftarrow v \end{cases}$$

 \blacktriangleright An **event set** E is a dated set of events

$$E = \langle t, \{e_1, \dots, e_n\} \rangle$$

where t gives the occurrence **time** (logical instant).

For example $E = \langle 10, \{h, e \leftarrow 0\} \rangle$ means

"At time t=10, event h occurs and (input) e is set to 0".

The union of event sets is defined as

$$\langle t, e \rangle \cup \langle t', e' \rangle = \begin{cases} \langle t, e \cup e' \rangle & \text{if } t = t' \\ \bot & \text{otherwise} \end{cases}$$

 \blacktriangleright A stimulus σ (resp. response ρ) is just an event set involving inputs (resp. outputs).

TODO: Input et output par rapport à quoi : automate ou contexte?

Rules

▶ Given a static description $\mathcal{H} = \langle M, C \rangle$ of a program, the **execution** of this program submitted to a sequence of stimuli $\vec{\sigma} = \sigma_1, \dots, \sigma_n$ is formalized by rule EXEC

$$\frac{C \vdash M \to M_0, \ \Gamma_0}{C \vdash M_{i-1}, \ \Gamma_{i-1} \xrightarrow{\sigma_i} M_i, \ \Gamma_i} \\
\frac{\forall i \in \{1, \dots, n\} \qquad C \vdash M_{i-1}, \ \Gamma_{i-1} \xrightarrow{\sigma_i} M_i, \ \Gamma_i}{\vec{\rho} = \langle M, C \rangle} \xrightarrow{\vec{\sigma} = \langle \sigma_1; \dots; \sigma_n \rangle} M_n, \ \Gamma_n$$
(EXEC)

In other words, the execution of the program is described as as a sequence of **instantaneous** reactions, which can be denoted as 6 :

$$M_0, \ \Gamma_0 \xrightarrow[\rho_1]{\sigma_1} M_1, \ \Gamma_1 \to \dots \xrightarrow[\rho_n]{\sigma_n} M_n, \ \Gamma_n$$

where

- the global environment Γ here records the value of inputs and shared variables⁷,
- ρ_1, \ldots, ρ_n is the sequence of responses,
- M_n and Γ_n respectively give the final state of the automata and global environment.
- ▶ Rule Init describes how the initial set of automata M_0 and global environment Γ_0 are initialized by executing the initial transition of each automaton (producing a set of initial responses ρ_0 .

⁶Omitting context C, which is constant during an execution.

⁷This environment is required to handle events describing modifications of these values, as described below (see rule REACTUPD).

$$\forall i \in \{1, \dots, n\} \quad \mu_i = \langle \mathcal{M}_i, q_i, \mathcal{V}_i \rangle \quad \mathcal{M}_i = \langle \dots, \dots, \dots, \langle \dots, \vec{a_i} \rangle \rangle \quad C \vdash \mathcal{V}_i, \ \gamma_{i-1} \xrightarrow{\vec{a_i}, 0} \mathcal{V}_i', \ \gamma_i \quad \mu_i' = \langle \mathcal{M}_i, q_i, \mathcal{V}_i' \rangle$$

$$C = \langle \dots, I_v, \dots, O_v, \dots, H_v \rangle \quad \gamma_0 = \mathcal{I}(I_v \cup O_v \cup H_v)$$

$$C \vdash M = \{\mu_1, \dots, \mu_n\} \rightarrow M_0 = \{\mu_1', \dots, \mu_n'\}, \ \Gamma_0 = \gamma_n$$
(INIT)

where the I_v , O_v and H_v sets, taken from the static context C, respectively give the name of inputs, outputs and shared variables.

Note. Rule INIT does *not* produce any response ρ . This is because the initial actions of an automaton cannot emit events hence can only update the its local environment or the global one.

▶ Rule Acts describes how a sequence of actions \vec{a} (at time t) updates the local and global environments, possibly emitting a set of responses⁸.

$$\forall i \in \{1, \dots, n\} \qquad C \vdash \mathcal{V}_{i-1}, \ \Gamma_{i-1} \xrightarrow{a_i, t \atop \rho_i} \mathcal{V}_i, \ \Gamma_i$$

$$\frac{\mathcal{V}_0 = \mathcal{V} \quad \Gamma_0 = \Gamma \quad \rho_e = \bigcup_{i=1}^n \rho_i}{C \vdash \mathcal{V}, \ \Gamma \xrightarrow{\langle a_1; \dots; a_n \rangle, \ t \atop \rho_e} \mathcal{V}_n, \ \Gamma_n}$$
(ACTS)

Note. The definition of rule ACTS given above enforces a *sequential interpretation* of actions. For example

$$\{x \mapsto 1, \ s \mapsto \bot\}, \ \Gamma \xrightarrow{\langle x \leftarrow x + 1; s \leftarrow x \rangle, t} \{x \mapsto 2, \ s \mapsto 2\}, \Gamma$$

Rule ACTS could easily be reformulated to describe other interpretations, such as a *synchronous* one, in which all RHS values are first evaluated and then assigned to LHS in parallel⁹.

▶ Rules ACTUPDL and ACTUPDG respectively describe the effect of an action updating a local or global variable (shared variable or output)¹⁰.

$$\frac{x \in \text{dom}(\mathcal{V}) \quad v = \mathcal{E}_{\mathcal{V} \cup \Gamma}[\![e]\!]}{C \vdash \mathcal{V}, \ \Gamma \xrightarrow{x \leftarrow e, \ t} \mathcal{V}[x \mapsto v], \ \Gamma} \text{ (ACTUPDL)} \qquad \frac{x \in \text{dom}(\Gamma) \quad v = \mathcal{E}_{\mathcal{V} \cup \Gamma}[\![e]\!]}{C \vdash \mathcal{V}, \ \Gamma \xrightarrow{x \leftarrow e, \ t} \mathcal{V}, \ \Gamma[x \mapsto v]} \text{ (ACTUPDG)}$$

▶ Rule React describes how a program M within a global environment Γ (instantaneously) reacts to a stimulus (event set) σ , producing a response (event set) ρ , an updated program M' and an updated environment Γ' .

$$\frac{\sigma_{e}, \sigma_{v} = \Sigma(\sigma) \qquad C \vdash M, \ \Gamma \xrightarrow{\sigma_{v}} M, \ \Gamma_{v} \qquad C \vdash M, \ \Gamma_{v} \xrightarrow{\sigma_{e}} M', \ \Gamma'}{C \vdash M, \ \Gamma \xrightarrow{\rho_{e}} M', \ \Gamma'}$$
(REACT)

where the function Σ partitions a *event set* into one containing the stimuli corresponding to *pure* events (ϵ) and another containing those corresponding to updates to global inputs :

⁸This set of responses is always empty when rule ACTS is invoked in the context of INIT.

⁹As happens in hardware synchronous implementations for example.

¹⁰The effect of an action emitting an event will be described by rules ACTEMITS and ACTEMITG, given latter.

$$\Sigma(\langle t, \{e_1, \dots, e_n\} \rangle) = \langle t, \{e_i \mid e_i = \epsilon_i\} \rangle, \quad \langle t, \{e_i \mid e_i = x_i \leftarrow v_i\} \rangle$$

▶ Rule Reacture describes how a program M within a global environment Γ reacts to set of events describing updates to global inputs. These updates are just recorded in the environment and do not produce responses, nor trigger any reaction of the automata:

$$\frac{}{C \vdash M, \ \Gamma \xrightarrow{\sigma_v = \langle t, \{x_1 \leftarrow v_1, \dots, x_m \leftarrow v_m\} \rangle} M, \ \Gamma[x_1 \mapsto v_1] \dots [x_m \mapsto v_m]}$$
(REACTUPD)

▶ Rule Reactev describes how a program reacts to a set of pure events.

$$\forall i \in \{1, \dots, n\} \quad C \vdash \mu_{\pi(i)}, \ \Gamma_{i-1} \xrightarrow{\sigma_i} \mu'_{\pi(i)}, \ \Gamma_i \qquad \sigma_i = \sigma_{i-1} \cup \rho_i$$

$$\Gamma_0 = \Gamma \qquad \sigma_0 = \sigma_e \qquad \rho_e = \bigcup_{i=1}^n \rho_i \qquad \Gamma' = \Gamma_n$$

$$C \vdash M = \{\mu_1, \dots, \mu_n\}, \Gamma \xrightarrow{\sigma_e = \langle t, \{\epsilon_1, \dots, \epsilon_m\} \rangle}_{\rho} M' = \{\mu'_1, \dots, \mu'_n\}, \ \Gamma'$$
(REACTEV)

Each automaton reacts separately but in a specific order. This order is derived from the dependencies between automata. We say that an automaton μ' depends on another automaton μ at a given instant t, and note

$$\mu < \mu'$$

if the reaction of μ at this instant can trigger or modify the reaction of μ' at the same instant. Concretely, this happens when μ and μ' are respectively in states q and q' and there's (at least) one pair of transitions (τ, τ') starting respectively from q and q' so that

- τ' is triggered by an event emitted by τ , or
- a variable occurring in the guards associated to τ' is written by the actions associated to τ .

The function π used in REACTEV is a permutation of $\{1,\ldots,n\}$ defined so that

$$\mu_{\pi(1)} \le \mu_{\pi(2)} \le \ldots \le \mu_{\pi(n)}$$

Having the automata of M react in the order $\pi(1), \ldots, \pi(n)$ ensures that any event emitted or local variable update performed by an automaton during a given reaction is effectively perceived by any other automaton at the same reaction, a principle called instantaneous broadcats.

The permutation π can easily be computed by a topological sort of the dependency graph derived from the conditions expressed above. In practice, this will be carried out by a static analysis of the program.

▶ Rules REACT1, REACT0 and REACTN describe how a single automaton reacts to a set of pure events, updating both its internal and global states and producing another set of (pure) events in response.

$$\frac{\Delta_{\Gamma \cup \mathcal{V}}(\mathcal{M}, q, e) = \{\tau\}}{C \vdash \mu, \ \Gamma \xrightarrow{\frac{\tau, \ t}{\rho_e}} \mu', \Gamma'} (\text{REACT1}) \qquad \frac{\Delta_{\Gamma \cup \mathcal{V}}(\mathcal{M}, q, e) = \emptyset}{C \vdash \mu = \langle \mathcal{M}, q, \mathcal{V} \rangle, \ \Gamma \xrightarrow{\frac{\sigma_e = \langle t, e \rangle}{\rho_e}} \mu', \ \Gamma'} (\text{REACT1})$$

$$\Delta_{\Gamma \cup \mathcal{V}}(\mathcal{M}, q, e) = \{\tau_1, \dots, \tau_n\}$$

$$\tau = \text{choice}(\{\tau_1, \dots, \tau_n\})$$

$$C \vdash \mu, \Gamma \xrightarrow{\tau, t} \mu', \Gamma'$$

$$C \vdash \mu = \langle \mathcal{M}, q, \mathcal{V} \rangle, \Gamma \xrightarrow{\sigma_e = \langle t, e \rangle} \mu', \Gamma'$$
(REACTN)

Given a automaton modelised by \mathcal{M} and currently in state q, $\Delta_{\Gamma}(\mathcal{M}, q, e)$, where $e = \{\epsilon_1, \ldots, \epsilon_n\}$, returns the set of *fireable* transitions, *i.e.* all the transitions triggered by the event set e starting from q and for which the all the associated boolean guards evaluate, in environment Γ , to true.

$$\Delta_{\Gamma}(\mathcal{M}, q, \{\epsilon_1, \dots, \epsilon_n\}) = \bigcup_{i=1}^n \Delta_{\Gamma}(\mathcal{M}, q, \epsilon_i)$$

where

$$\Delta_{\Gamma}(\langle .,.,.,T,.\rangle,q,\epsilon) = \{(q_s,c,a,q_d) \in T \mid q = q_s \land c = \langle \epsilon, \{e_1,\ldots,e_n\} \rangle \land \forall i \in \{1,\ldots,n\} \quad \mathcal{E}_{\Gamma}[\![e_i]\!] = \mathsf{true}\}$$

Rule React1 describes the case when the set of events triggers exactly *one* transition of the automaton. Its state and local variables are updated according to the actions listed in the transition and the remaining actions are used to generated the set of responses.

Rule React0 describes the case when the set of events does not trigger any transition. The automaton and the global environment are left unchanged.

Rule REACTN describes the case when the set of events triggers more than one transition. This situation corresponds to a non-deterministic behavior of the automaton. The function choice is here used to choose one transition¹¹.

▶ Rule Trans describes the effect of performing a transition, updating the automaton local and global states and returning a set of (pure) events as responses.

$$\mu = \langle \mathcal{M}, q, \mathcal{V} \rangle \qquad \tau = \langle q, c, \vec{a}, q' \rangle$$

$$C \vdash \mathcal{V}, \Gamma \xrightarrow{\vec{a}, t} \mathcal{V}', \Gamma'$$

$$\frac{\mu' = \langle \mathcal{M}, q', \mathcal{V}' \rangle}{C \vdash \mu, \Gamma \xrightarrow{\tau, t} \mu', \Gamma'}$$
(Trans)

▶ Rules ACTEMITS and ACTEMITG complement the rules ACTUPDL and ACTUPDG given previously by describing the effect of an action emitting a shared or output event. The H_e set, taken from context C, is here used to distinguish between to to. The formers can trigger the reaction of other(s) automaton(s), the latters are just ignored here (see note below).

$$\frac{C = \langle ., ., ., ., H_e, . \rangle \quad \epsilon \in H_e}{C \vdash \mathcal{V}, \ \Gamma \xrightarrow{\langle t, \{\epsilon \} \rangle} \mathcal{V}, \ \Gamma} \text{(ACTEMITS)} \qquad \frac{C = \langle ., ., ., H_e, . \rangle \quad \epsilon \notin H_e}{C \vdash \mathcal{V}, \ \Gamma \xrightarrow{\langle t, \emptyset \rangle} \mathcal{V}, \ \Gamma} \text{(ACTEMITG)}$$

Note. The semantics described here only defines how a program execution progresses, from the initial program to the final program state M. In practice, an interpreter will also build a trace of such an execution, recording all significant events (stimuli, responses, state moves, etc.). Building such a trace is easily performed by modifying the semantic rules given above. It has not been done here for the sake of simplicity.

¹¹This can done, for example, by adding a *priority* to each transition.

Compiler options

```
Compiler usage: rfsmc [options...] files
                            set prefix for the generated main files
                            dump typed representation of model(s)/program to stdout
    -dump\_typed
    -dump_static
                            dump static representation of model(s)/program to stdout
    -target dir
                            set target directory (default: .)
                            set location of the support library (default: jopam_prefix;/share/rfsm)
    -lib
                            generate .dot representation of model(s)/program
    -dot
    -sim
                            run simulation (generating .vcd file)
    -ctask
                            generate CTask code
                            generate SystemC code
    -systemc
    -vhdl
                            generate VHDL code
                            print version of the compiler and quit
    -version
    -show models
                            generate separate representations for uninstanciated FSM models
                            print qualified identifiers in DOT representations
    -dot_qual_ids
                            generate report and error messages for interacting with rfsm-light
    -gui
                            Remove captions in .dot representation(s)
    -dot no captions
    -dot short trans
                            Print single-line transition labels (default is multi-lines)
                            Print abbreviated types (default is to print definitions)
    -dot_abbrev_types
    -dot boxed
                            Draw FSM instances in boxes
    -sim trace
                            set trace level for simulation (default: 0)
    -vcd int size
                            set default int size for VCD traces (default: 8)
    -synchronous_actions
                            interpret actions synchronously
                            set time unit for the SystemC test-bench (default: SC_NS)
    -sc\_time\_unit
    -sc\_trace
                            set trace mode for SystemC backend (default: false)
    -stop\_time
                            set stop time for the SystemC and VHDL test-bench (default: 100)
                            implement float type as C++ double instead of float (default: false)
    -sc\_double\_float
    -vhdl trace
                            set trace mode for VHDL backend (default: false)
                            set time unit for the VHDL test-bench
    -vhdl time unit
    -vhdl_ev_duration
                            set duration of event signals (default: 1 ns)
    -vhdl rst duration
                            set duration of reset signals (default: 1 ns)
    -vhdl numeric std
                            translate integers as numeric std [un]signed (default: false)
    -vhdl_bool_as_bool
                            translate all booleans as boolean (default: false)
    -vhdl_dump_ghw
                            make GHDL generate trace files in .ghw format instead of .vcd
```

Building language variants

Following the approach described in [1] for example, the RFSM compiler is implemented in a modular way. The language is split into a host language, describing the general structure and behavior of FSMs (states, transitions, ...) and a guest language¹ describing the syntax and semantics of expressions used in transition guards and semantics. Technically, this "separation of concern" is realized by providing the host language in the form of a functor taking as argument the module implementing the guest language.

This approach makes it fairly easy to produce variants of the "standard" RFSM language – with dedicated type systems and expression languages typically – by simply defining the module defining the guest language and applying the aforementioned functor. Actually, the "standard", RFSM language was designed using this approach, starting from a very simple "core" guest language gradually enriched with new features at the expression level².

The directory src/guests/templ in the distribution provides the basic structure for deploying this approach. In practice, to implement a language variant, one has to

- write the implementation of the guest language in the form of a collection of modules in the lib subdirectory³,
- write the lexer and the parser for this guest language (expressions, type expressions, ...),
- build the compiler by simply invoking make

To illustrate this process, we describe in the sequel the implementation of a very simple language language for which the guest language has only two types, 'event' and 'bool', and expressions are limited to boolean constants and variables⁴. We focus here on the most salient features. The Readme file in the templ directory describes the procedure in details. Other examples, given in src/guests/core and src/guests/others⁵, can also be used as guidelines.

4.1 Implementing the Guest module

The module implementing the guest language must match the following signature:

¹ "Base" in the terminology of [1].

²Traces of the incremental design process can be found in the srs/guests/core, src/guests/others/szdints and src/guests/others/szvars directories for example.

³These modules will be encapsulated in a single module and the latter will be passed to the host functor to build the target language.

⁴This language is essentially that provided in src/guests/others/mini.

⁵And, of course, in src/guests/std.

```
module type T = sig
  module Info : INFO
  module Types : TYPES
  module Syntax : SYNTAX with module Types = Types
  module Typing: TYPING with module Syntax = Syntax and module Types = Types
  \label{eq:module_value} \mathbf{module} \ \ \mathrm{Value} \ : \ \mathrm{VALUE} \ \mathbf{with} \ \ \mathbf{type} \ \ \mathrm{typ} \ = \ \mathrm{Types.typ}
  module Static : STATIC with type expr = Syntax.expr and type value = Value.t
  module Eval : EVAL with module Syntax = Syntax and module Value = Value
  module Ctask: CTASK with module Syntax = Syntax
  module Systemc: SYSTEMC with module Syntax = Syntax and module Static = Static
       and type value = Value.t
  module Vhdl: VHDL with module Syntax = Syntax and module Static = Static and
      type value = Value.t
  module Error : ERROR
  module Options: OPTIONS
end
```

where

- module Info gives the name and version of the guest language,
- module Syntax describes the (abstract) syntax of the guest language,
- modules Types and Typing respectively describe the types and the typing rules of the guest language,
- module Static describes the static semantics of the guest language (basically, the interpretation of model parameters),
- modules Value and Eval respectively describe the values and the dynamic semantics manipulating these values.
- modules CTask, Systemc and Vhdl respectively describe the guest-level part of the C, SystemC and VHDL backends,
- module Error describes how guest-specific errors are handled,
- module Options describes guest-specific compiler options.

Listings 4.1, 4.2, 4.4 and 4.6 respectively show the contents of of the Types, Syntax, Value and Eval modules for the mini language. The definition of non essential functions has been omitted⁶.

Listing 4.1: Module Guest. Types (excerpt)

```
type typ =
  | TyEvent
  | TyBool
  | TyUnknown

let no_type = TyUnknown

let is_event_type (t: typ) = match t with TyEvent -> true | _ -> false
let is_bool_type (t: typ) = match t with TyBool -> true | _ -> false
let pp_typ ?(abbrev=false) fmt (t: typ) = ...
```

⁶See the corresponding source files in src/guests/others/mini/lib for a complete listing.

In module Types, the key definition is that of type typ, which describes the guest-level types, *i.e.* the types which can be attributed to guest-level expressions and variables. The type TyUnknown is used to define the value no type which is attributed by the host language to (yet) untyped syntax elements.

Listing 4.2: Module Guest.Syntax (excerpt)

```
module Types = Types
module Location = Rfsm. Location
module Annot = Rfsm.Annot
module Ident = Rfsm. Ident
let mk ~loc x = Annot.mk ~loc ~typ: Types.no_type x
(* Type expressions *)
type type_expr = (type_expr_desc, Types.typ) Annot.t
and type_expr_desc = TeConstr of string (* name, no args here *)
let is_bool_type (te: type_expr) = ...
let is_event_type (te: type_expr) = ...
let pp_type_expr fmt (te: type_expr) = ...
(* Expressions *)
type expr = (expr_desc, Types.typ) Annot.t
and expr desc =
   EVar of Ident.t
   EBool of bool
let vars_of_expr (e: expr) = ...
and pp_expr fmt (e: expr) = ...
(* LHSs *)
type lhs = (lhs_desc, Types.typ) Annot.t
and lhs\_desc = Ident.t
let lhs_var (l: lhs) = ...
let vars_of_lhs(l: lhs) = ...
let is_simple_lhs (1: lhs) = true
let mk_simple_lhs (v: Ident.t) =
  Annot. { desc=v; typ=Types.no_type; loc=Location.no_location }
let pp_lhs fmt l = ...
```

The module Syntax use the modules Location, Annot and Ident provided by the Rfsm host library. These modules provide types and functions to handle source code locations, syntax annotations and identifiers respectively. The type ('a,Types.typ) Annot.t is associated to syntax nodes of type 'a. The types type_expr, expr and 1hs respectively describe guest-level type expressions, expressions and left-hand-sides (LHS). LHS are used in the definition of actions. In this language they are limited to simple identifiers (ex: x:=<expr>) but the guest language can use other forms (like in the RFSM "standard" language which support arrays and records in LHS).

Listing 4.3: Module Guest. Values (excerpt)

```
type typ =
   | TyEvent
   | TyBool
   | TyUnknown

let no_type = TyUnknown

let is_event_type t = match t with TyEvent -> true | _ -> false
let is_bool_type t = match t with TyBool -> true | _ -> false
let mk_type_fun ty_args ty_res = ...

let pp_typ ?(abbrev=false) fmt t = ...
```

Listing 4.4: Module Guest. Value (excerpt)

```
type t =
    | Val_bool of bool
    | Val_unknown

let default_value ty = match ty with
    | _ -> Val_unknown

exception Unsupported_vcd of t

let vcd_type (v: t) = match v with
    | Val_bool _ -> Rfsm.Vcd_types.TyBool
    | _ -> raise (Unsupported_vcd v)

let vcd_value (v: t) = match v with
    | Val_bool v -> Rfsm.Vcd_types.Val_bool v
    | _ -> raise (Unsupported_vcd v)
let pp fmt (v: t) = ...
```

The module Guest.Value define the values, associated to guest-level expressions by the dynamic semantics. The value Val_unknown is used to represent undefined or unitialized value. The functions vcd_type and vcd_value provide the interface to the VCD backend, generating simulation traces: they should return a VCD compatible representation (defined in the host library Vcd_types module) of a value.

Listing 4.5: Module Guest.Eval (excerpt)

```
module Syntax = Syntax
module Value = Value
module Env = Rfsm.Env
module Annot = Rfsm.Annot

type env = Value.t Env.t

exception Illegal_expr of Syntax.expr
exception Uninitialized of Rfsm.Location.t

let mk_env () = Env.init []
```

The module Guest.Eval defines the guest-level dynamic semantics, *i.e.* the definition of the dynamic environment env, used to bind identifiers to values and of the functions eval_expr and exal_bool used to evaluate guest-level expressions. The presence of a distinct, eval_bool function is required because the boolean type and expressions are not part of the host-level syntax. The definition of the env type here uses that provided by the host library but any definition matching the corresponding signature would do.

4.2 Implementing the Guest parser

The parser for the guest language defines the concrete syntax for guest-level type expressions, expressions and LHS. It is written in a separate .mly file which will be combined with the parser for the host language⁷. There are only two guest specific tokens here, denoting the boolean constants true and false. The open directive in the prologue section gives access to the abstract syntax definitions given in Guest.Syntax module. The function mk, defined in this module, builds annotated syntax nodes, inserting the source code location.

Listing 4.6: File guest_parser.mly

```
%token TRUE
%token FALSE

%{
  open Mini.Top.Syntax
  %}

%

public type_expr:
  | tc = LID { mk ~loc:$sloc (TeConstr tc) }

%public lhs:
  | v = LID { mk ~loc:$sloc (mk_ident v) }

%public expr:
```

⁷Using menhir facility to split parser specifications into multiple files.

```
| v = LID { mk ~loc:$sloc (EVar (mk_ident v)) }
| c = scalar_const { c }

%public scalar_const:
| TRUE { mk ~loc:$sloc (EBool true) }
| FALSE { mk ~loc:$sloc (EBool false) }

%public const:
| c = scalar_const { c }

%public stim_const:
| c = scalar_const { c }
```

4.3 Implementing the Guest lexer

The ocamllex tool, used for defining the lexer, does not support multi-file definitions. The lexer for the guest-specific part of the target language is therefore supplied in the form of code fragments to be inserted in the host lexer definition file⁸. These fragments are listed in two separate files, present in the bin subdirectory of the guest directory:

- the file guest km contains the lexer definition of the guest-specific keywords,
- the file guest_rules contains the guest-specific rules.

In the case of the mini language defined here, the latter is empty and the former only contains the two following lines.

```
"true", TRUE;
"false", FALSE;
```

4.4 Building the compiler

Defining the target language implementation and building the associated compiler is then simply obtained by the two following functor applications 9 :

```
module L = Rfsm. Host.Make(Mini.Top)

module Compiler =
   Rfsm.Compiler.Make
   (L)
    (Lexer)
   (struct include Parser type program = L.Syntax.program end)
```

Invoking the compiler now boils down to executing

```
let _ = Printexc.print Compiler.main ()
```

 $^{^8{\}rm Technically},$ this insertion is performed using the ${\sf cppo}$ tool.

⁹For technical reasons, these two statements are placed in distinct files, binlang.ml and binrfsmc.ml.

Bibliography

[1] X. Leroy. A Modular Module System. J. Functional Programming, 10(3):269-303, 2000.