Jeffrey Shy · EECS 16 A Midterm 1 Sheet Bystems of Lieur Equard Famisian Elim (A (18) Mector - ordered list of numbers I= [xin] This Ain Matrix - rectangular array of numbers LAm, Amn Gaussian Elm - algorithm that reduces In eq (can obtain anime sol, infinite sol, no sols)

(ZA) Vector Addition: Compart  $\overrightarrow{x}$  +  $\overrightarrow{y}$  =  $\overrightarrow{y}$  +  $\overrightarrow{x}$ Assoc.  $(\overrightarrow{x}$  +  $\overrightarrow{y})$  +  $\overrightarrow{z}$  =  $\overrightarrow{x}$  +  $(\overrightarrow{y}$  +  $\overrightarrow{z})$  add in  $\overrightarrow{x}$  +  $(-\overrightarrow{x})$  =  $\overrightarrow{0}$ For water pump: rows -represent proportion of water a reservior will draw from other reservoires columns - how water will be distributed between other reservoirs the next day Marky vector fom: Ax= 6 3 Liner dependence - redundancy one vector can be written as linear comb of another Def; vectors & V., Vz ... Vn 3 are hearly dependent if of ... of n such that of V, V, az Vz ... of n on vin = 0 and of the # 0 Lower independence - not lacri dependent dn=0 Span - span of vectors Evillary is set of all their son's 5 N. ... V3 (B) Maty Mull [an and [bil biz] = [anbin + anz bz, anbiz + anz bzz]

[an bin + anz bz] az, bin + anz bzz

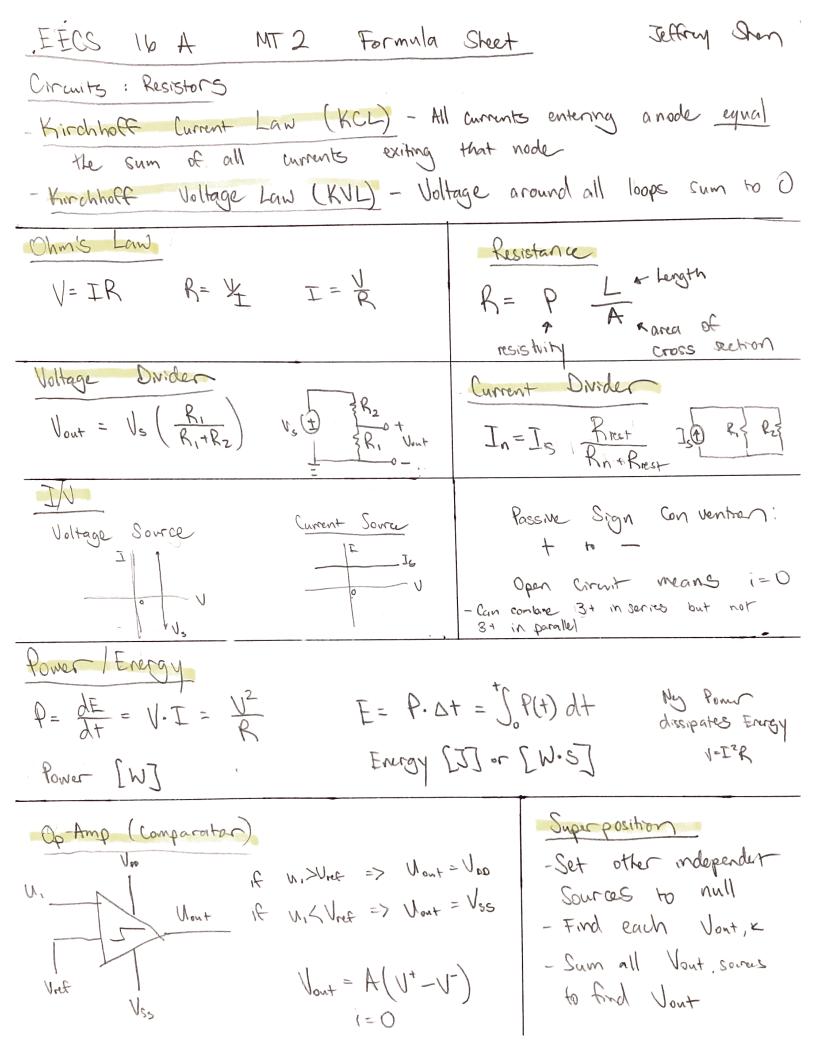
[an bin + anz bzz] az, bin + anz bzz Not Commutative AB + BA Is associate (AB) C= A(BC) @ Equivalent Car nxn A independent cols (full only) A is invertible => liverly independent d) (=> A has tourish mull space (null(A)= 803) a) A is multiple => tourish mull space e) (=) Let (A) # () Thetor spaces (D) set of vector and mo operates suts fy

Vector addition

- Assource in (1-1) = (1-1) + in - Hossorie a (PT) = (aP) in - Hossorie a (PT) = (aP) in - Multi Idney 1-1 in - Multi Idney 1-1 in a interior a confiderable in the interior and in a confiderable and in the interior and interior ana - Closure sum toto must be in as must be in I

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Borsis - of vector space if (min set of vector to represent all vactors).
        D V, Jz In Inerty independent

z) stalus such that \vec{J} = \vec{d}, \vec{V}, + \vec{A}_2 \vec{V}_2 \dots
 Dimension of a vector space is number of basis vectors
(IN) is a subspace if IN is a subset of IV and
              (WiF) = vecto space
  Nullspace (A): Solutions to Ax =0
  column space of (A) = span of the columns of A
 rank - may num of heavy independent columns
 ProoSs
@ Nrite what you know and what you want to prove
3-Try smal simple example to see it you and patterns
to marphite both sides and simplify Justify count step
(9 1) constructe proofs (generate example) solution)
    5) boole på contragispou (
 Knowi AT = XT Subset A C B
 Ex) Does inverse east? make column's are likely independent, invertible, excis
       Lourndependence; Ru/K=(Rz+Rz)
    Boisis: The basis for null (A) is {[i.s]}
        hon trivial nullspace => linearly dependent => no unique sol.
 Thm: If AR= to how two or more sol, him col of A are herly diproter
    let x, x2 be mo sol
                                  Show c, a + c, a + . . c, an =0
     Axies Axz=$
                              Gumen Hi, -et, Hiz-etz
      Mx-xz)=0
      7 = x,-x2 +0
                              4 = 0, 4, 1 x 2 /2
                                  HT=H(ay, + 02 /2) = Har, + Haz /2 - 024, AHe/2=
     A[",]=0
     Y, a, + yaz ... y = 0
                                                           e(4,4,+x242)= e4
   WLOG let 4,40
       à, = 1/2 à2 + 10 7/2 àn
```



Capa citar ce

Charge [c] Capacitance [F]

E= ZCVe2

Discharging: -I(+) = CdV

Conservation of Charge

Q[+] = Q[++1] - Charge in system remains same after the Step

Therum

VTN = Voc

open arant voltage between out ports Therenn is

RTh = RNor

Way to solve: - find Vat

- Null Independent Soway

VTh = INORTH

- Find Vat B w/o taking into account A - Cale Rim

-Subtract

Norton

INO = I was

Current flowing through

output parts when ports

are shorted

Way to solve?

-connect A & B by wor and ignore in between

Inst ZRNO

# Node Voltage Analysis (NVA)

1) Label Voltages at all Nodes

- 2) Label Element Voltages and Currents & Passine Sign cont.
- 3) Write KCL Equations of Element Currents
- 4) Expressing for Element (urrents using FNL
- 5) Substitute Expressions for Element Currents into KCL

6) Solve

lips

- -Redraw ovenits if recessor
- Pay attention to units - See what variable serves

aremer is supposed to

po in

Cross-Coorelation

Def: measure of the similarity between two signals

$$\operatorname{Corr}_{x}[\sqrt[4]][x] = \sum_{i=-\infty}^{\infty} x[i] y[i-k]$$

Because of noise we want  $A\bar{x}=\bar{b}$  but to minimize noise we use €=b-Ax minimize 11è112 find smallest error

Least Squares

Def: Solves approx. systems in the presence of noise  $\tilde{\chi} = (A^TA)^{-1}A^T\tilde{b}$  where A is independent

(Note: Use for tall and thin overdetermined matrixes

Orthogonal Matching Pursuit (OMP)

Def: unmixes signals from multiple beacons, uncover messages Known: matrix M, vector , sporsity level & or threshold for norm

- 1) Find inner product for each vector, m; with e (first iter; e= y)
- 2) Add vector that had max inner prod to matrix A
- 3) Use proj/least squares to compute X=(ATA)TATÝ
- (4) Update Error Vector &= \$\vec{y} A\vec{x}\$
- & Repeat until reached sparsity level

- Linearize distance formula egs

Op Amp

U+ o T Vont

Golden Rules:

Ideal of Amp

D = - I = 0

(2) A > 00

Ideal & Negative Feedback Unity Grain Buffer

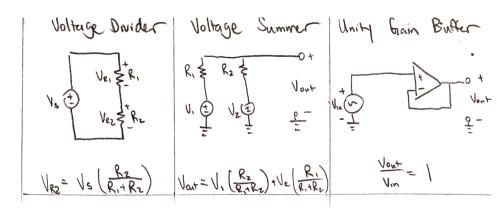
(1) Ut = U\_

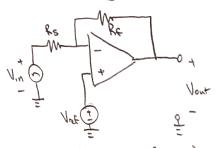
loading - small resistance causes it to draw alot of current causing large voltage drop, make it harder be it will behave differently depending on what it's connected to

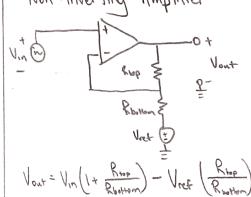
-Buffers allow us to split into blocks to analyze separately

#### Design Problem

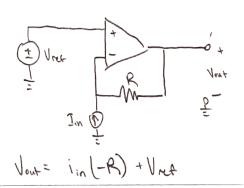
- 1) Restale important goals for design
- 2) Describe strategy wing block dragram
- 3) Implement







### Transpesistance Amplifier



## Orthonormal Matrix

Colums à: are

- 1) Orthogonal (ai, ai) = 0
- (2) Nor malred || a; || = 1

### Eigenvalues

$$A\vec{x} = \lambda \vec{x}$$

$$det(A-\lambda I) = 0$$

same, Eigenvalues squared If A squared, Eigenvectors

$$\begin{bmatrix} -4 & -3 \\ 4 & 3 \end{bmatrix} \vec{a} = 0 \quad -4 \alpha_1 - 3 \alpha_2 = 0$$

$$-4a_1 = 3a_2$$
 $a_1 = -\frac{3}{4}a_2$ 

$$\begin{bmatrix} -\frac{3}{4} \\ 1 \end{bmatrix} a_{7}$$