

$$\frac{d}{dt} x(t) = \lambda x(t)$$

$$\frac{d}{dt} x(t) = \lambda x(t) + \alpha$$

$$x(t) = x(0)e^{\lambda t} + \frac{\alpha}{\lambda}(e^{\lambda t} - 1)$$

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If touser functions in series w unity gain buffers, We can multiply transfer funcs

Resonance

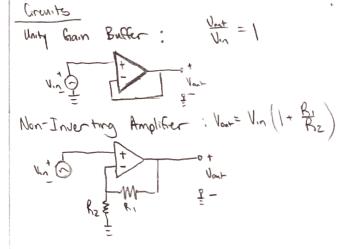
Resonance frequency: It when impedances inductor and capacitor are equal

For differential equation
$$\frac{d^2}{dt} \times dt + a \frac{d}{dt} \times dt + b \times dt = 0$$

$$\lambda^2 + a\lambda + b = 0 \qquad \lambda = -\frac{a}{2} \pm \frac{1}{2} \sqrt{a^2 - 4b}$$

- Dictically damped: a2-46=0
- 2) Undamped: a is 0
- 3) Underdamped, 02-46 LO
- 4) Overdamped a2-46>0

repeated eigenvalue, real again values purely imaginary eggenualus complex, Malanding eigenvalus purely real



Inductors = Short circuit (a)= N=0=M=0 Capacitors = open circuit

NMOS	上工	PMOS -14
High=1	0	High = 1 0 Low = 0 1

$$\cos(x) = \sin(x + \frac{\pi}{2})$$

$$\sin(x) = \cos(x - \frac{\pi}{2})$$

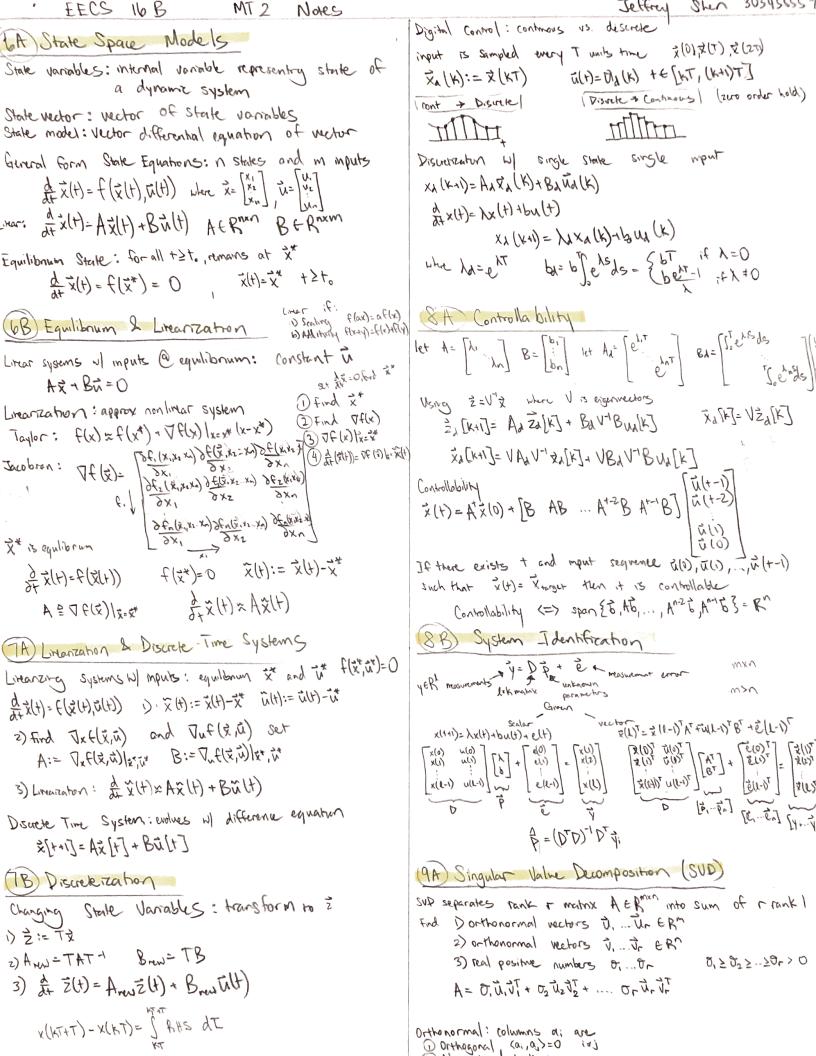
Phasors

- i) Adopt (our returne (time domain)
- 2) Transfer to phason domain :> I L-> 21= NNL N=V R=ZR-R C> ZL= vic
- 3) Cast Equations in phasor form
- 4) Solve for unknown
- 5) Transform back to Time domain = Re[Jeint] = 6 cos(wt-1050)

G= 109

$$m = 10^{-3}$$
 $K = 10^{3}$

$$h = 10^{-12}$$
 $h = 10^{9}$
 $h = 10^{-12}$ $h = 10^{12}$



(9B) Finding SVD

Very ATA

1) Find eigenvalues of ATA, L, 2/22... 2/r>0, (A-XI)=0

2) Find orthonormal expensectors V. (Plag in (A-XI) makes and Find where = 0)

3) Let 0:= Thi get in ルーナール

Using AAT

1) Find organ values of AAT

2) Find orthonormal eigenvectors V. AAT il = livi

3) Let 0:= Thi get Vi できるがん

 $I = U^T U$ VTV-I

MA) SUD Cont.

BU and I must be orthogenal so apperd orthonormal busis if media

beonetic Interpretation:

Ax composition of

) VIX : receiverts x w/o changing length

2) EVTX: Stretches along axis w/ singular value

3) USVTX: recognits vector who changing length

 $||\vec{x}||=|$ then $||A\vec{x}|| \le \overline{\sigma}$, $||G_{rr}\vec{x}|| = \overline{\sigma}$, $||A\vec{x}|| = \theta$,

Symmetric Matrices: $Q = Q^T$ (Spectral Theorem)

Symmetric Matrix has in

- real eigen values

- real orthonormal eigenvectors

- diagonalizable (A=VNT)

Rank-Nullity Theorem:

FOR A= NXM rank (A) + Null (A) = m

 $(AB)^T = B^T A^T$

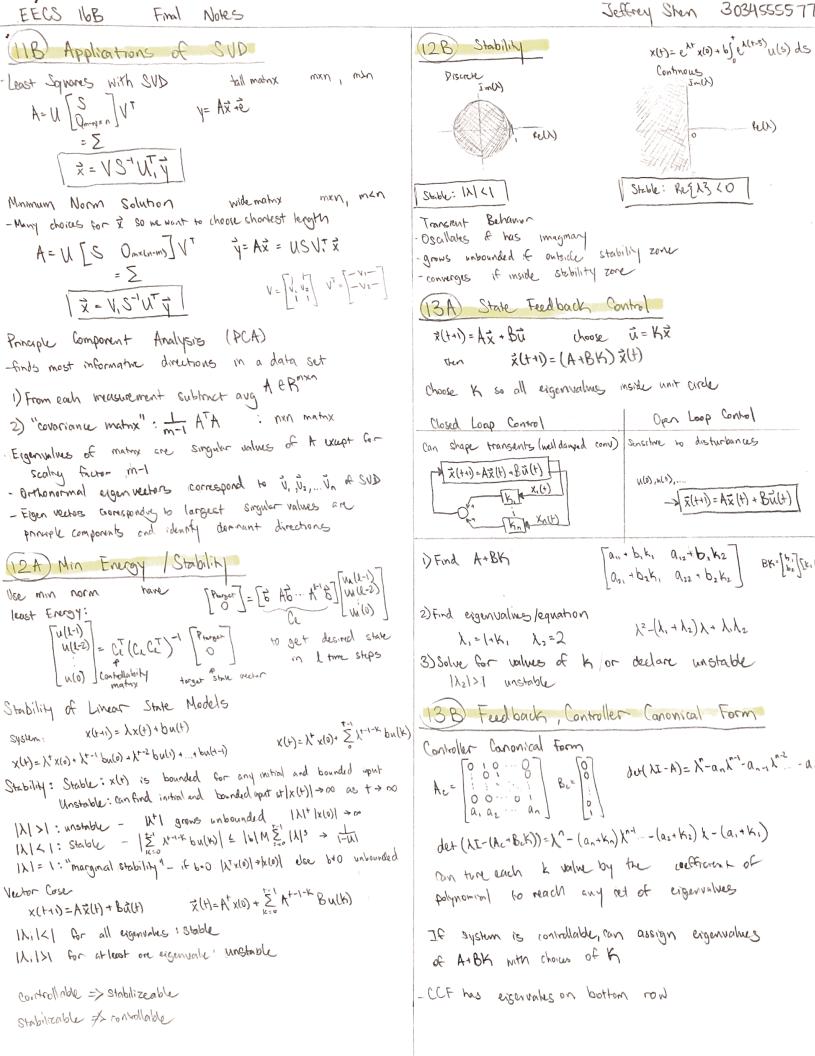
If a can be written as a= RFR for some R, elgenvalues are nonegative

Gerera)

- Stable it eigenvalue 21 - Plugging into X with a when [cite] gover eigen veldors -inverse of orthogonal matrix a same as tempore

Controllability

To reach X(n):



(14A) Upper Triangularization

- NXN makes is diagonizable (values only in diagonal) it it has a literally independent eigenvectors, distinct eigenvectors

- Any squar matry an be upper triangular - Uppertrangular matrix has eigenvalues along draggard

Gram-Schmidt Process

Algo takes liverly independent vectors &s.,...s. and generates an orthonormal set of vector's &g.,...g.m3 that span same space

) Find unit vector \vec{q} , span($\{q_i\}$) = Span($\{s_i\}$) $\vec{q}_i = \frac{\vec{s}_i}{\|\vec{s}_i\|}$

2) Find 7/2

Ospan same

(2) orthogond (5) normal

22=\$2-09, 0
gut orthogord vector with OMP
proj q. \$2= 9. \$2 9. & 22= \$2-9. \$29.

 $\vec{q}, \quad \frac{\vec{z}_1}{\sqrt{\vec{z}_2}}$

Algo 3.

for $i=2 \rightarrow n$: $\vec{z}_{i}^{2} = \vec{s}_{i} - \sum_{j=1}^{2i} (\vec{s}_{i}^{2} \vec{q}_{j}) \vec{q}_{j}$ $\vec{q}_{j} = \frac{\vec{z}_{i}}{||\vec{z}_{i}^{2}||}$

Conceptua)

PCA: How to approx higher dimension data into lower of dimension essence. First Principle Component is which ND Ime lest approx, by presenting data points onto it

SVD: Decompose Ainto sum of rank I matrices
ith rank I matrix formed from taking outer
product of normalized rolumn vectors it; and
normalized row vectors it; scaled by it;
Addry each matrix for singular value on top
of each other

Phasors: By converting to phasor doman, your take snapshot of time domain, solve it relative to snapshot and phasor extends to all phases so you an convert back to time domain, and result all becarbe solution