

Bits

- N bits is at most 2^n things
- Numerals: Binary (2), Decimal (10), Hexadecimal (16)
- ASCII: for all characters in English Language, 7 bits

Bit ConversionsBinary \rightarrow Decimal, Hex \rightarrow Decimal

- Add up powers of 2/16

$$0b101 \quad 1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0 = 5$$

Binary \leftrightarrow Hex

1. Pad left 0s to make multiple of 4
2. Read off groups of 4, using table
3. Drop any leading 0s

Decimal \rightarrow Binary, Decimal \rightarrow Hex

1. From left to right, find largest power of 2, 16
2. If it fits, subtract and repeat w/ next digit

Decimal	Hex (0x...)	Binary (0b...)
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

Overflow: number is too large to be represented, positive or negative

Bit Operations

&	AND	$x \& y$
	OR	$x y$
^	XOR (not equal)	$x \wedge y$
~	Complement (flip)	$\sim x$
<<	shift left	$x \ll n$
>>	shift right	$x \gg n$

extract bits, check neither are 1, turn off bits

combine w/ mask, check either are 1, turn on bits

flip bits w/ mask

flip bits

multiply by 2

divide by 2

$\ll n$ is
n 0s to right
of 1

Number Representations

N bits

① Sign and Magnitude

$$[-(2^{N-1}-1), 2^{N-1}-1]$$

Negation: Leftmost bit is sign bit, 0: positive 1: negative

- 2 zeros

② One's Complement

$$[-(2^{N-1}-1), 2^{N-1}-1]$$

Negation: Flip the bits

- 2 zeros, leftmost bit tells sign

③ Two's Complement

$$[-2^{N-1}, 2^{N-1}-1]$$

Negation: Flip bits and add one

④ Bias Notation

$$[b, 2^N - 1 + b]$$

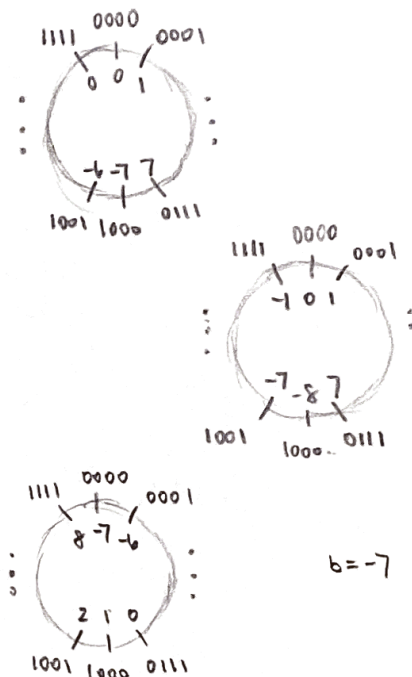
- Shift on unsigned notation

$$\begin{array}{ccccc} x & + & b & = & n \\ \uparrow & & \uparrow & & \uparrow \\ \text{unsigned} & & \text{bias} & & \text{number represented} \end{array}$$

⑤ Unsigned

$$[0, 2^N - 1]$$

- No negative numbers, max at $2^N - 1$



C

- Allows us to exploit underlying architecture, created in 1970s, C99
- Files first pass through C Pre-Processor where macros replace functions

Variable types

Ex) char: 8 bits (1 byte)

int: 32 bits (4 byte)

int *: 32 bits depending on machine [index into memory array]

False values: '0', 0, NULL

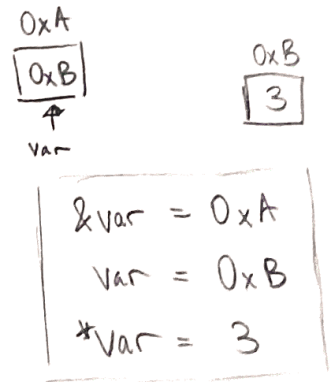
Pointer Arithmetic: incrementing sizeof(pointer-type)

Structs: structured groups of variables

sizeof: returns number of bytes

Pointers (type *var)

- Stores an address
- dereference operator (*): gets value at address
- C passes parameter by value, pass pointer
- If a variable is not initialized, it holds garbage
- Arrow Notation: $var \rightarrow x$ same as $(*var).x$

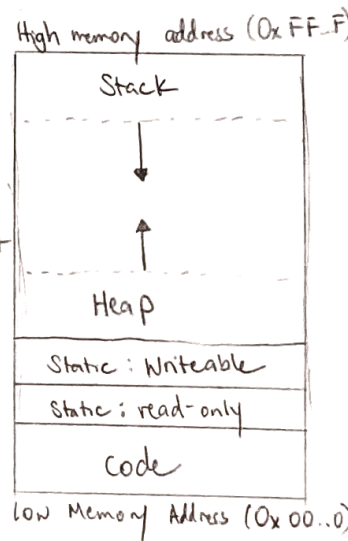


Memory Allocation

- $malloc(\text{byte-size})$: returns void * pointer, initializes with default garbage
- $free(ptr)$: must free any malloc'ed point, once
- $realloc(ptr, size)$: reallocate memory
- After allocating memory, check if pointer is NULL

Memory Management

- ① Stack: function local variables, strings allocated as arrays (LIFO)
- ② Heap: dynamically allocated memory (malloc, calloc, realloc)
Not necessarily contiguous, fragmentation is an issue, circular linked list
- ③ Static: global variables, statically allocated strings, basically permanent memory
- ④ Code: machine instructions



(NOTE:) - memory of pointers and what they point to may be in different memory

- $\text{char}^* s1 = \text{"csble"}$ $s1[0]$ is in static, read-only
- $\text{char} s2[] = \text{"csble"}$ $s2[0]$ is in stack

C Problems

- Draw out diagram w/ addresses
- Check if malloc or parameters are NULL

Tips

- $\text{strlen}(\text{char}^*)$: # chars (bytes) in string not including terminator
- Big Endian: lowest address on left
- Little Endian: lowest address on right
- "\n" after printf
- arr is pointer to first element in array

Compiler, Assembler, Linker, Loader (C411)

- Interpret a high level language when efficiency not critical to exec other programs
- Translate to lower level language to increase performance, hide source

Compiler

High level language \rightarrow Assembly Language (C \rightarrow RISC-V)

- Translates language

C program: foo.c

Compiler

Assembly program: foo.s

Assembler

Object Code: foo.o

Linker

lib.o

Executable: a.out Machine Language

Loader

Memory

Assembler

Assembly language \rightarrow object files (RISC-V \rightarrow file.o)

- Replace pseudo-instructions
- Two passes to determine offset between jumps
- Reads and uses directives (.text, .data, .string, .globl)
- Produces relocation tables (to fill in later when you link) in other files and symbol tables (list of items in this file that may be used/referenced)

Linker

object files \rightarrow executable code (file.o \rightarrow a.out)

- Fulfills missing labels in relocation symbol tables
- Combines object files into binary executable

Loader

executable file \rightarrow program run

- Reads header and creates memory space, set up for execution

Combinational Logic



NOT

flips input



AND

1: both inputs 1
0: otherwise



OR

1: at least one input 1
0: otherwise



XOR

1: inputs different
0: otherwise



MUX

pick among inputs
Select selects one of 2's

Boolean Algebra

+ : OR

* : AND

and : NOT

$$x + yz = (x + y)(x + z)$$

$$xy + \bar{x} = x$$

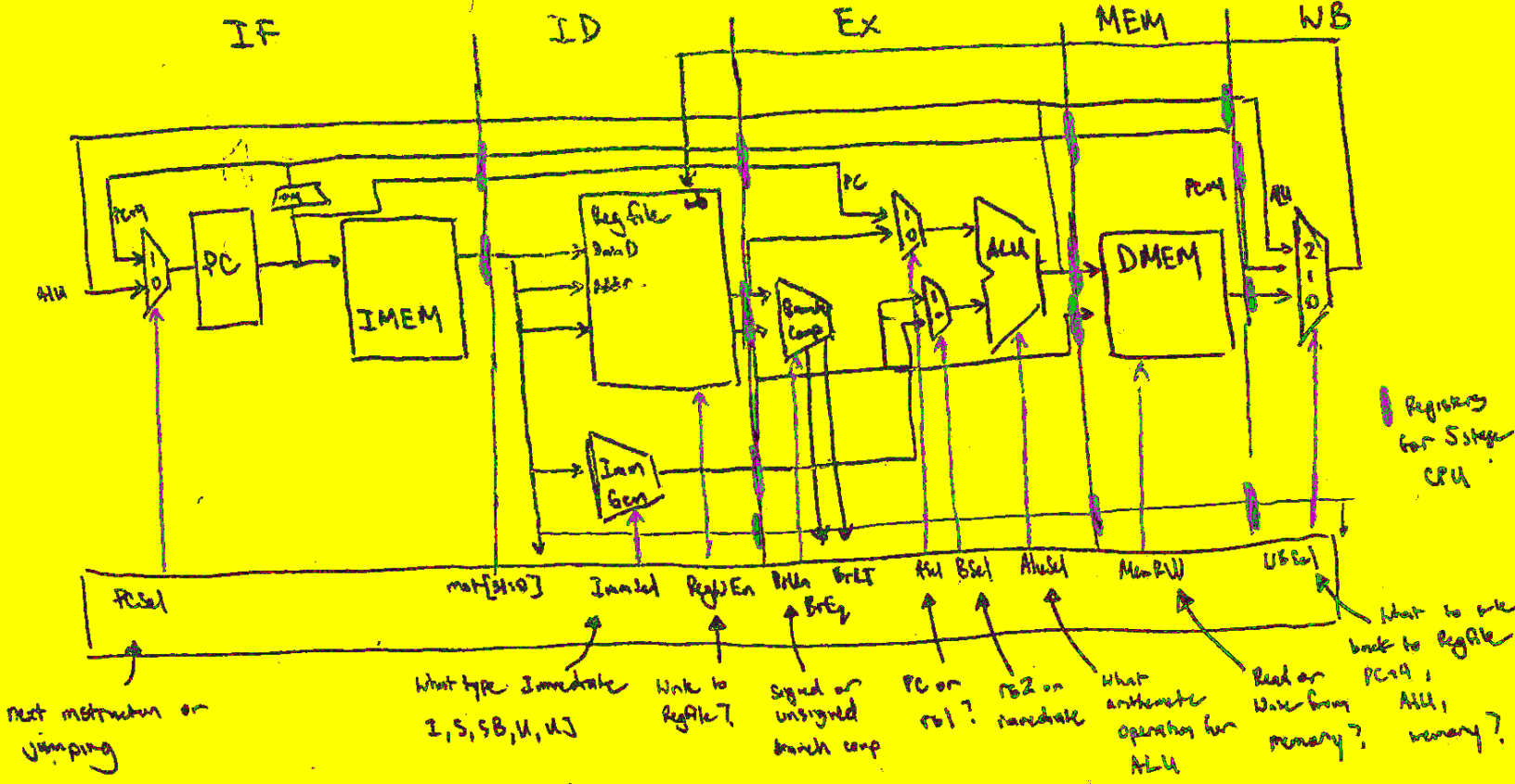
$$\overline{x \cdot y} = \bar{x} + \bar{y}$$

$$(x + y)x = x$$

$$\overline{(x + y)} = \bar{x} \cdot \bar{y}$$

distributing
uniting theorem

DeMorgan's Law ③



Critical Path for single cycle = $t_{PCsel} + t_{Imm} + t_{Rn} + t_{Rm} + t_{ALU} + t_{Mem} + t_{WBuf}$

Clock frequency = $\frac{1}{\text{critical path}}$

Pipelining: Add registers between stages to speed up

Latency: time for 1 instruction to finish

Throughput: # instructions processed per unit of time

Pipelining increases throughput but also latency

Pipelining Hazards

1. Structural Hazards

- more than one instruction needs to use resource
- caused by: register file ID, WB, Memory IMEM, DMEM
- solved by: hardware

2. Data Hazards

- data dependences between instructions
- caused by: instruction reads register before prev finished writing
- solved by:
 1. Forwarding: result of EX, MEM sent to EX for next
 2. Stalls (lw) map to stall

3. Control Hazards

- jump and branch and return of next PC

caused by : jump and branch instructions

solved by : 1. Branch prediction : predict where to go from prev

inst. + misprediction if not taken

2. Stall

Double Pumping : allows writing and reading from reg file in one stage