Ing Identities William Mille

Sin(x+y) = Sinx cosy + Cosxsiny cos(x+y) = cos x cos y - sinx siny tanx + tany tan (x+y)= 1-tan x tany

 $S_{in}(2x) = 2s_{in}x cosx$ $\cos(2x) = \cos^2 x - \sin^2 x$ $= 2\cos^2 x - 1$ = 1-2sin2X tan(2x) = 2tanx 1-tan2x

Chapter 10 Parametre Eq. Polar 以第二次第一次 't x= f(+) 4= O(+) Area = (g(+) (+) d+ X F F F B

Are length = [[(\frac{1}{2})^2 + (\frac{1}{2})^2 dt = [NUV]dt

Surface Area = 27) x ((2x)2+(2x)2 d+

X= rcoso y= r sind r2=x2+y2 +=n 0= \$

tongent of . dy = de sind + (cost)
Polar dy = de cost - rsint tangent of.

Cardioid/Limacon: r= a + b cost, r= a + bsint

Roses: $r = a \cos(n\theta)$ $r = a \sin(n\theta)$ old: petals=n even: petals = 2n

Area Polar = 1 1 12 do Arc length = I / r2+ (10)2 do

Chapter 12 Mille Vectors, Space Mille $\alpha \cdot \beta = |\alpha| |\beta| \cos \theta$ $0 \leq \theta \leq a$

comp. 6 = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}|} \proj_a \vec{b} = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}|^2} \vec{a}

1287 = 12/18/2018 DEAZT

Vol of parallel pped = | a. (bxc)

Dist from point to place [Ax, + By, + Cz, + D]

Dist from port to line: he LAB + API

Intersections

Ocheck of director sector porallel

in turns of t and s

Find distance between Ires using cross product and comp. 6

Ellazoig: 8 + 7 + 5 = /

Elliphe !

= X - Y= Hyperbole of 三二 2 + 光 Cone.

Hyperboloid on Sheet

TWO SHEETS , - QE - YE + ZE = / Hyperboloid

Ost X=XZ, Y, = Yz, ===Zz

Parallel a, b

Chapter 13 Vector Fune 1/1/2

Arc length = 5 (71/t) dt

foranchize in terms of 5 r(+) => r(5)

1) Solve for s

@ Use of to solve for + in terms of s

3 Plug + equation into +(+)

Nort Target: 7(+) = (2'(+))

が(H)= デ(H) B(H) デェル

(unvature : KE (+1(+)) = (1(+) x (1)(+))

radus of osculating plane: 1= x

a= 11/7 + KT2 N where T= 101 $0.4 = \frac{\langle (t) \cdot C_n(t) \rangle}{\langle C_n(t) \rangle}$ $var = \frac{\langle C_n(t) \times C_n(t) \rangle}{\langle C_n(t) \rangle}$

Chapter 14 Markals White

lim f(x,y) = L @ Approach from dit lines Probability: 3 convert to polar men

Tangent: 2-2-= Fx(x0,40) (x-x0)+ Fy(x0,40) (4-40)

FARCE ofbox: F(xA)= f"(x-x0) + fd(A-d0) +50 (ase T: 2= f(x,y) x=g(t) y=h(t)

提着, 強 強 張

(Case 2: z=f(xiy) x=g(e,t) y=h(e,t) dz = dx ds + dz dy de dt ...

A = - Fx 3x = - Fx 3x = Fx

Dufley) = Af. is in direction unit wester is wex Det = 1 16/ DE(x4) = (Ex, Ex)

Tis is of tengent or outh = AP - proper I lu-rately-rad =0

Max/Min

Critical point fr- Ey= D or one DNE D= txx (o'p) th (o'p) - [txh (o'p)]_s

1) DDO, Fix >0 => local min (2) D>0, Fxx <0 => weal max

(3) D<0 => not min on max (could be point)

(A) D=0=> no info, any

Find vale of f at entiral points (2) Find extense values on Boundary D

(5) larguet max smallest min

Lagrange: maxlmn: f constrant: , 9 = k 1 f(x,y,z)= / 2 (x,y,z)

Chapter 15 Mult Integrals

V= SS F(x,y) dA

Ag vote = 12 F(x,y) dA = Volume
and of R = Area

Ob The (Grass, cons) I de do

Applications

M= SS p(x,y) dA p lamma Moment = SSS p(x,y,z) dV

Mx = SI y p(xy) dA

Ab (4.x) q x) = +M

x = my = = 1 (1 x p(x,y) dA

7 = mx = in sqyp(x,y) dA

Moment of Inertia:

Ix = [] y2 p(xiy) dA

In = 1/2 x 8 (x,y) dA

I. (orgin) = [[(x24/2) p(x4) dA

f(x,y)≥0 P= [] f(x,y) dA = 1

Triple Enlegals

Cylindrical

(x,y,z) rdzdrdd

X= rcost 4= reind z=Z

K= PEmB (080) 4= psind sind

== 6 cosy x3+1/2+2= 02

If
$$f(x,y)$$
 $dA = \iint f(x(u,y), y(u,y)) \frac{\partial(x,y)}{\partial(u,y)} dudy$

The harm $x = J(u,y)$ $y = h(u,y)$
 $\frac{\partial(x,y)}{\partial(u,y)} = \frac{\partial x}{\partial x} \frac{\partial x}{\partial y} = \frac{\partial x}{\partial y} \frac{\partial y}{\partial y} - \frac{\partial x}{\partial y} \frac{\partial y}{\partial y}$

Dend we we mental

Find $x = y = 0$

The form of $x = 0$

In the form of $x = 0$

Find $x = 0$

Find $x = 0$

Find $x = 0$

Then

Cond

Officer of $x = 0$

Th

open region

```
16.5 Curl and Divergence
curl F = VXF
dNF = D.F
                                 curl (at) = 0
Fun 3 vacs continous partiols =>
                                  curl (F) =0
   F conservative
                                 F not conservative
    (url(F) $0
curl(F)=0 & simply connected & => F conservative
   continous Partials
                            => div (curl (F)) =0
his second partials
                             => F not a curl
 div (F) +0
16.6 Parametric Surfaces and Arens
Para metre Surface: r(u,v)=(x(u,v),y(u,v),z(u,v))
Surface of Revolution: X=X y=f(x)cost z=f(x) sint
   (about x-axis)
Normal Vector to tengent place is CaxCu
Surface Area: A(s) = SS Iruxrol dA = ST [+(dz)2+(dz)2 dA
16.7 Surface Integrals
Surface Entegral / Flux:
 4. F. ds = 55 F.nds = 55 F. (r.xr) dA = 5 (-P 2 - 22 + R) dA
16.8 Stokes Theorem = 15 f(r(u,u)) (r,xr) AA = 15 f(xy,g(x,y) (x) (x) (x) 11.
O S is precevise smooth surface
                                   J.F.dr =
@ Bounded by simple, closed
   pieceuse - smooth boundary
                                 Scurl F. ds
  curve C 4) positive orientators
(3) Continous partial denuatures
16.9 Divergence Theorem
1) E is comple solid region
                                   15 F. ds =
(2) S is boundary surface of E
   4) positive outward orientation
                                     SSS dn F dV
3 continues portals on open
  region contains E
Vd (Sphere) = = 1113
```