

Exam II

November 5, 2020, 9:10am-10:25am, Pacific time

Instructions (read carefully):

1. This exam has 8 questions and 8 pages.
2. You must submit a single PDF file with your responses to the exam questions on Blackboard Learn by 10:25am pacific time on November 5, 2020.
3. If your submission is late, as determined by the Blackboard Learn timestamp, then you will be deducted 1 point for each minute your exam is late. *This will be strictly enforced.* The exam is worth 60 points and is designed to be completed in 1 hour (if you studied). This leaves 15 minutes to access the exam and upload your response; please plan accordingly.
4. The exam is open book and open notes, and you may use a calculator. You may not receive any assistance during the exam from other people or the Internet. Evidence of assistance will result in a zero on the exam. If you have questions during the exam, you may email me at holder@wsu.edu. I will be monitoring my email during the exam and will respond as soon as possible.
5. Your exam response can be created with an editor on your computer and/or scans or pictures of a written response. Make sure all responses are clearly legible and that the exam question number is clearly indicated. Again, your exam response must be a single PDF file.

- 2

3. (10 points) Consider the following first-order logic predicates.

- Breeze(x,y): there is a breeze in location (x,y)
- Pit(x,y): there is a pit in location (x,y)
- Stench(x,y): there is a stench in location (x,y)
- Wumpus(x,y): the Wumpus is in location (x,y)
- Agent(x,y): the agent is in location (x,y)
- Safe(x,y): location (x,y) is safe

Convert the following English sentences into first-order logic using only the above predicates.

- (2 points) There is at least one Safe location.
- (2 points) There is either a Breeze or a Stench (or both) in location (2,2).
- (3 points) The Wumpus and the Agent are never in the same location.
- (3 points) A location is safe if it does not contain the Wumpus or a Pit.

4. (10 points) Convert the following first-order logic sentences into Conjunctive Normal Form. There is no need to show intermediate steps.

a. (2 points) $\exists x,y \text{ Stench}(x,y)$

b. (2 points) $\forall x,y \text{ Wumpus}(x,y) \Rightarrow \neg \text{Safe}(x,y)$

c. (3 points) $\forall x,y (\text{Breeze}(x,y) \Rightarrow \exists w,z \text{ Pit}(w,z))$

d. (3 points) $\forall x (\text{Foo}(x) \vee \text{Bar}(x)) \Rightarrow \text{Baz}(x)$

5. (10 points) Given the following knowledge base, already expressed in CNF, use resolution by refutation to prove $\text{Dead}(\text{Agent})$ is true. Show each resolution step by indicated the two clauses being resolved (be sure to use unique variable names for each clause), the resulting clause (give it a new number), and any necessary variable substitutions. Also be sure to conclude your proof with a statement of what was proven.

C1: $\neg \text{Pit}(x,y) \vee \text{Safe}(x,y)$

C2: $\text{Safe}(x,y) \vee \neg \text{Agent}(x,y) \vee \text{Dead}(\text{Agent})$

C3: $\text{Pit}(3,3)$

C4: $\text{Agent}(3,3)$

6. (9 points) Suppose you are given the following full joint probability distribution over three Boolean random variables: *Breeze*, *Stench*, *Safe*. Compute the probabilities below. Show your work. *Your final answers should be real numbers – no incomplete arithmetic or fractions.*

	<i>Breeze</i> :	true		false	
	<i>Stench</i> :	true	false	true	false
<i>Safe</i> :	true	0.05	0.10	0.08	0.25
	false	0.20	0.20	0.08	0.04

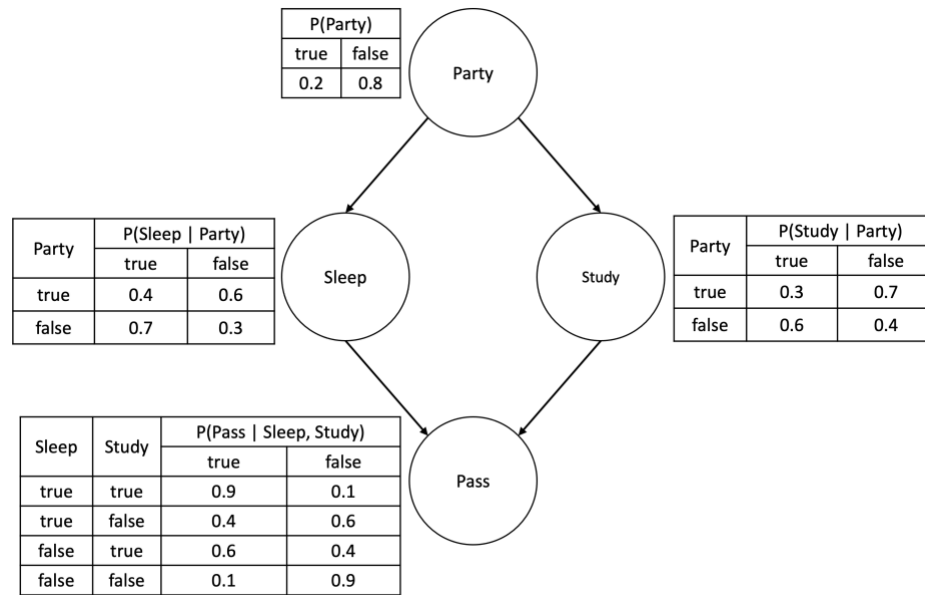
- a. (2 points) $P(\text{Breeze}=\text{true}, \text{Stench}=\text{true})$.
- b. (3 points) $P(\text{Safe}=\text{true} \mid \text{Breeze}=\text{false}, \text{Stench}=\text{false})$.
- c. (4 points) $P(\text{Safe}=\text{false} \mid \text{Breeze}=\text{true})$.

7. (6 points) Suppose we have two Boolean random variables Rain and Cloudy, and we know the following probabilities:

- $P(\text{Rain}=\text{true} \mid \text{Cloudy}=\text{true}) = 0.4$
- $P(\text{Rain}=\text{true} \mid \text{Cloudy}=\text{false}) = 0.1$
- $P(\text{Cloudy}=\text{true}) = 0.2$

Compute $P(\text{Cloudy}=\text{true} \mid \text{Rain}=\text{true})$. Show your work. *Your final answer should be a real number – no incomplete arithmetic or fractions.*

8. (15 points) Consider the Bayesian network below.



- a. (5 points) What is the most probable sample from the above network and what is its probability?
- b. (10 points) Compute the $P(\text{Party}=\text{true} \mid \text{Pass}=\text{true})$. Show your work. *Your final answer should be a real number – no incomplete arithmetic or fractions.*