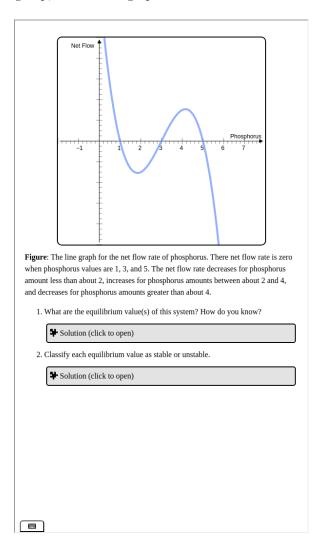
1 Stability Re-visited

In your group, use the line graph of the net flow rate for this stock to answer the following questions.





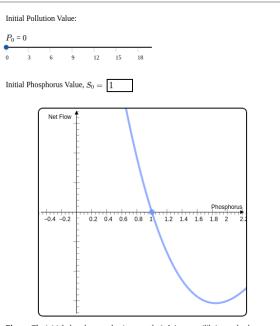
Standalone Embed

2 Sensitivity

Work in your group to fill out the following table to compute the sensitivities to pollution at various equilibrium values.

Use the first graph to set your initial pollution value, and find the associated initial phosphorus equilibrium value by either moving the point on the horizontal axis, or setting the value manually so that the net flow rate is 0. Similarly, use the second graph to set your next pollution value, and find the associated next phosphorus equilibrium value.

The first row is completed for you to use as a guide.

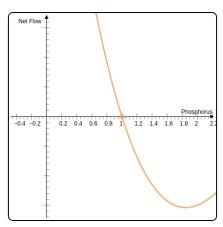


 $\label{eq:Figure:The initial phosphorus value is currently 1. It is an equilibrium value because the net flow rate is 0.$

Next Pollution Value:



Next Phosphorus Value, $S_1=oxed{1}$



 ${\bf Figure}:$ The next phosphorus value is currently 1. It is an equilibrium value because the net flow rate is 0.

0 1 0.25 1.006 1.006 1.006-1 0.25 0.0 6	P_0	S_0	P_1	S_1	Sensitivity
12 Check Check Check	0	1	0.25	1.006	$\frac{1.006-1}{0.25-0} = 0.023$
- Check - Check	6				
	12			← Check Work	
15 Check Mort Work Work	15				← Check Work

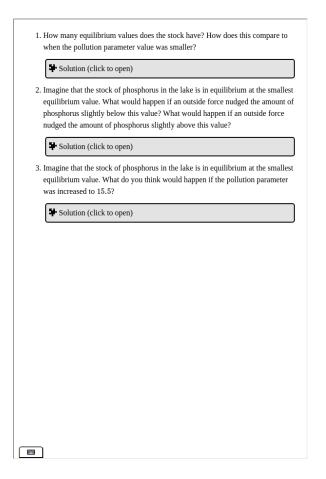


Standalone Embed

- 1. Once your table is completed correctly, discuss the following questions in your group.
 - (a) How do the sensitivities change as pollution values change?
 - (b) Are there pollution values that can change the *number* of equilibrium values in the system? How does this seem to be connected to sensitivities?

3 Tipping Points

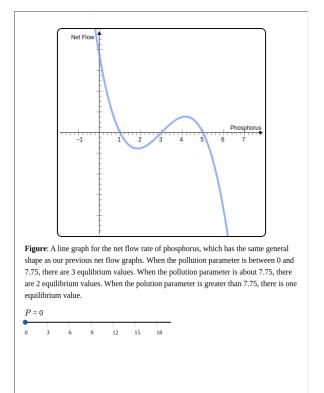
Place the pollution parameter slider in [cross-reference to target(s) "fig-net-flow-parameter" missing or not unique] to 15.25, and answer the following questions in your group.





Standalone Embed

4 Tipping Point Behaviors

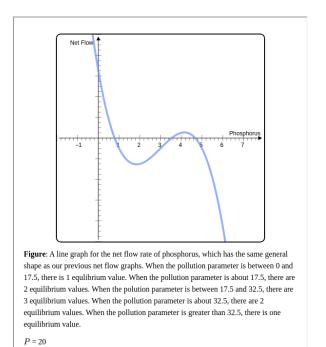




1. What are the tipping point values for the parameter P?

2. Imagine the phosphrus stock is in equilibrium when P = 0 at a phosphorus value of 1. If the parameter value exceeds the tipping point value closest to P = 0, how will the phosphorus value change?

3. If the parameter value exceeds the tipping point value closest to P = 0, is it possible for the phosphorus value to return to an equilibrium value of 1?





4. What are the tipping point values for the parameter P?

5. Imagine the phosphrus stock is in equilibrium when P=20 at a phosphorus value of 0.8. If the parameter value exceeds the tipping point value which is larger than P=20, how will the phosphorus value change?

6. If the parameter value exceeds the tipping point value which is larger than P = 20, is it possible for the phosporus value to return to an equilibrium value of less than 1?