## Survival Analysis Project: HIV Clinical Trial

Juste Simanauskaite & Patricia Rivera

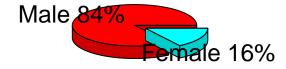
#### Contents

```
Survival Analysis
                                                                \mathbf{5}
Patricia's "Something New"
                                                               18
     18
    Juste's "Something New"
                                                               20
    1. What is goign on? What is the topic? 2. How it is relevant? How it relates to survival
         knitr::opts_chunk$set(message=FALSE, warning=FALSE, fig.height=3, fig.width=5,
               fig.align="center")
library(tidyverse)
library(broom)
library(plyr)
library(survival)
library(survminer)
library(coxed)
aids <- read.csv( "http://pages.pomona.edu/~jsh04747/courses/math150/AIDSdata.csv")
dim(aids)
## [1] 851 16
summary(aids)
##
      id
                 time
                            censor
                                        time_d
##
       :
          1.0
              Min.
                  : 1.0
                              :0.00000
                                     Min.
                                         : 1.0
##
  1st Qu.: 287.5
              1st Qu.:179.5
                                     1st Qu.:199.5
                         1st Qu.:0.00000
##
  Median: 581.0
              Median :257.0
                         Median :0.00000
                                     Median :266.0
##
  Mean
       : 579.5
              Mean
                  :231.8
                         Mean
                              :0.08108
                                     Mean
                                          :243.4
##
  3rd Qu.: 873.0
              3rd Qu.:300.0
                         3rd Qu.:0.00000
                                     3rd Qu.:306.0
##
       :1156.0
              Max.
                   :362.0
                              :1.00000
                                     Max.
                                          :362.0
##
    censor_d
                  t.x
                                       strat2
                            txgrp
##
  Min.
       :0.0000
              Min.
                   :0.0000
                         Min.
                              :1.000
                                         :0.0000
##
  1st Qu.:0.0000
              1st Qu.:0.0000
                         1st Qu.:1.000
                                    1st Qu.:0.0000
  Median :0.0000
              Median :1.0000
                         Median :2.000
                                    Median :1.0000
##
       :0.0235
                   :0.5041
                         Mean
                              :1.504
  Mean
              Mean
                                    Mean
                                         :0.6157
##
  3rd Qu.:0.0000
              3rd Qu.:1.0000
                         3rd Qu.:2.000
                                    3rd Qu.:1.0000
##
  Max.
       :1.0000
                   :1.0000
                              :2.000
                                         :1.0000
##
      sex
                raceth
                           ivdrug
                                     hemophil
##
       :1.000
                  :1.000
                             :1.000
                                        :0.00000
  \mathtt{Min}.
             Min.
  1st Qu.:1.000
             1st Qu.:1.000
                        1st Qu.:1.000
                                   1st Qu.:0.00000
  Median :1.000
             Median :1.000
                        Median :1.000
                                   Median :0.00000
```

```
##
   Mean
           :1.157
                    Mean
                            :1.706
                                     Mean
                                             :1.317
                                                      Mean
                                                              :0.03408
##
   3rd Qu.:1.000
                     3rd Qu.:2.000
                                      3rd Qu.:1.000
                                                      3rd Qu.:0.00000
##
           :2.000
                            :5.000
                                             :3.000
                                                              :1.00000
   Max.
                     Max.
                                     Max.
                                                      Max.
##
        karnof
                           cd4
                                           priorzdv
                                                               age
                                                                 :15.00
##
   Min.
           : 70.00
                     Min.
                             : 0.00
                                       Min.
                                               : 3.00
                                                         Min.
##
   1st Qu.: 90.00
                      1st Qu.: 22.25
                                        1st Qu.: 11.00
                                                         1st Qu.:33.00
   Median: 90.00
                     Median : 75.00
                                       Median : 21.00
                                                         Median :38.00
##
##
   Mean
           : 91.34
                            : 86.45
                                       Mean
                                               : 30.63
                                                                 :38.81
                      Mean
                                                         Mean
   3rd Qu.:100.00
                                        3rd Qu.: 44.00
##
                      3rd Qu.:135.75
                                                          3rd Qu.:44.00
   Max.
           :100.00
                     Max.
                             :348.00
                                       Max.
                                               :288.00
                                                         Max.
                                                                 :73.00
```

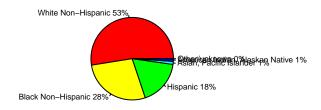
The data set contains a sample size equal to 851 participants and 16 different variables.

#### **Gender Distribution**



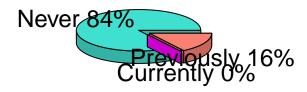
The Pie Chart represents the gender distribution in the sample, with 84% male and 16% female. This shows the potential for the data to not be able to correctly represent the difference of the data variance by gender, if there were to be one. Therefore, gender is something to look into in future data analysis.

```
pie(slices,lbls,col = rainbow(length(lbls)), cex=0.5 )
```



The distribution of race/ethnicity shows that the greatest number of participants consists of white non-hispanic identifying indiciduals, with black non-hispanic following and hispanic as the 3rd largest represented group.

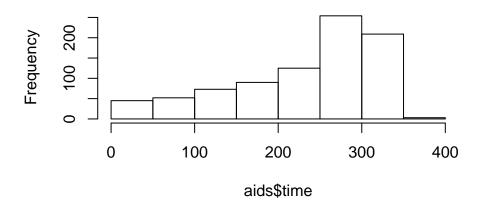
## **IV Drug Use History**

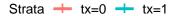


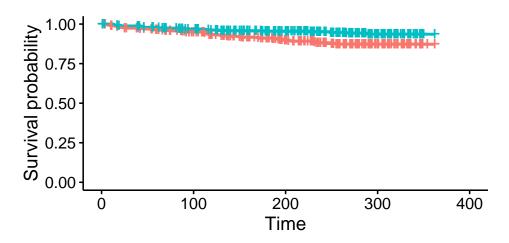
From this chart we see that most of the participants (84%) have never used IV drugs, whereas 16% of participants have some type of history of usage and none of the participants reported to be currently using the drugs.

```
hist(aids$time)
###Data Plots
fit <- survfit(Surv(time,censor)~tx, data = aids)
ggsurvplot(fit,data = aids,conf.int = FALSE)</pre>
```

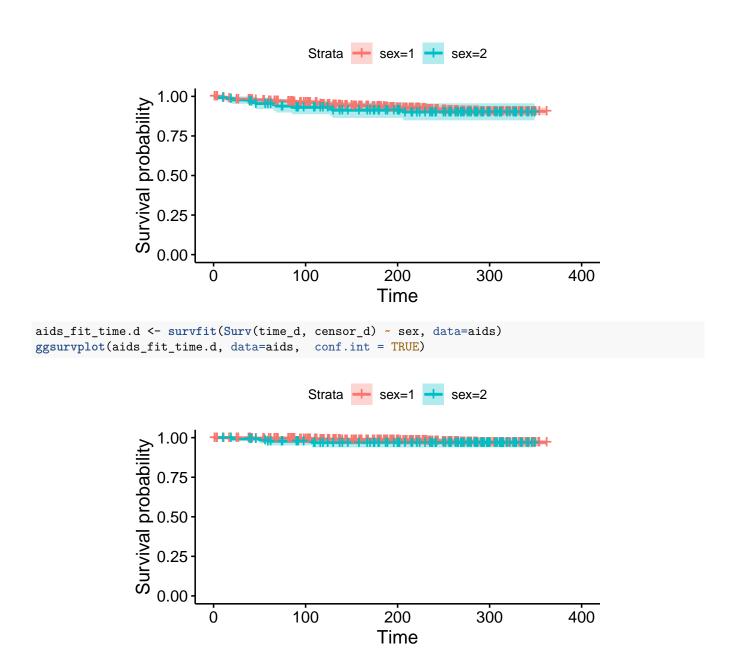
## Histogram of aids\$time







aids\_fit\_time <- survfit(Surv(time, censor) ~ sex, data=aids)
ggsurvplot(aids\_fit\_time, data=aids, conf.int = TRUE)</pre>



### Survival Analysis

```
sex = ifelse(sex == 2, "male", "female"))
Since there are many vuales of the explanatory variable "age" in the original data, we've decided to mutate the
variable into age categories from under 20 to over 70 in incriments of 10 years.
library(survival)
library (survminer)
library(ggplot2)
library(broom)
##### backwards selection ######
#full model
cph_full<- coxph(Surv(time,censor)~., data = aids)</pre>
cph_full$loglik
## [1] -452.6325 -380.7368
cph_full
## coxph(formula = Surv(time, censor) ~ ., data = aids)
##
##
                   coef
                         exp(coef)
                                     se(coef)
## id
              2.136e-05
                         1.000e+00
                                    3.956e-04
                                               0.054
                                                      0.95695
## time_d
              1.362e-03 1.001e+00
                                    2.139e-03 0.637
                                                      0.52432
## censor_d
              2.887e+00 1.795e+01
                                    3.990e-01 7.237 4.59e-13
## tx
             -3.917e-01
                         6.759e-01
                                    2.757e-01 -1.421 0.15540
## txgrp
                     NA
                                NA
                                    0.000e+00
                                                  NA
                                                            NA
              3.418e-01
                         1.408e+00
                                    4.397e-01
                                               0.777
                                                      0.43690
## strat2
## sexmale
              3.152e-01 1.371e+00
                                    3.518e-01 0.896
                                                      0.37024
## raceth
             -8.821e-02 9.156e-01
                                    1.543e-01 -0.572 0.56759
             -3.625e-01 6.959e-01
                                    1.942e-01 -1.867
## ivdrug
                                                      0.06197
## hemophil -1.247e-01 8.828e-01
                                    7.136e-01 -0.175
                                                      0.86132
## karnof
             -4.400e-02 9.569e-01 1.555e-02 -2.829 0.00467
## cd4
             -1.592e-02 9.842e-01 4.988e-03 -3.191 0.00142
## priorzdv -1.722e-04 9.998e-01 5.076e-03 -0.034
                                                      0.97293
## age20-30 -8.852e-01 4.126e-01 1.249e+00 -0.709
                                                      0.47862
## age30-40 -8.065e-01 4.464e-01 1.216e+00 -0.663 0.50706
## age40-50 -7.004e-01 4.964e-01 1.207e+00 -0.580
                                                     0.56174
                                   1.252e+00 -0.314
## age50-60 -3.926e-01
                         6.753e-01
                                                      0.75384
## age60-70 -1.054e+00
                         3.485e-01
                                   1.617e+00 -0.652 0.51443
## ageover70 -1.402e+01 8.172e-07 2.668e+03 -0.005 0.99581
##
## Likelihood ratio test=143.8 on 18 df, p=< 2.2e-16
## n= 851, number of events= 69
#reduced model 1
cph_r1 <- coxph(Surv(time,censor)~.-priorzdv, data = aids)</pre>
cph_r1$loglik
## [1] -452.6325 -380.7374
cph_r1
```

## coxph(formula = Surv(time, censor) ~ . - priorzdv, data = aids)

##

```
##
                  coef exp(coef)
                                    se(coef)
                                                 z
## id
             2.138e-05 1.000e+00 3.956e-04 0.054 0.95690
             1.364e-03 1.001e+00
                                   2.137e-03 0.638 0.52338
## time_d
                                   3.977e-01 7.263 3.78e-13
## censor_d
             2.889e+00 1.797e+01
## tx
            -3.918e-01 6.758e-01
                                   2.756e-01 -1.422 0.15513
## txgrp
                    NA
                               NA
                                   0.000e+00
                                                NA
             3.417e-01 1.407e+00
                                  4.398e-01 0.777
## strat2
                                                    0.43720
## sexmale
             3.150e-01
                        1.370e+00
                                   3.517e-01 0.896
                                                    0.37046
## raceth
            -8.808e-02 9.157e-01
                                   1.543e-01 -0.571
                                                    0.56802
## ivdrug
            -3.630e-01 6.956e-01
                                  1.936e-01 -1.875
                                                   0.06080
## hemophil -1.251e-01 8.824e-01
                                  7.137e-01 -0.175
                                                    0.86086
## karnof
            -4.397e-02 9.570e-01
                                  1.551e-02 -2.835
                                                    0.00459
## cd4
            -1.592e-02 9.842e-01 4.987e-03 -3.193 0.00141
## age20-30 -8.791e-01 4.151e-01 1.237e+00 -0.711
                                                    0.47738
## age30-40 -8.014e-01 4.487e-01 1.207e+00 -0.664
                                                    0.50669
## age40-50 -6.951e-01 4.990e-01 1.198e+00 -0.580 0.56163
## age50-60 -3.881e-01 6.783e-01 1.246e+00 -0.312 0.75539
## age60-70 -1.048e+00 3.508e-01 1.606e+00 -0.652 0.51426
## ageover70 -1.403e+01 8.034e-07 2.695e+03 -0.005 0.99584
## Likelihood ratio test=143.8 on 17 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
stat1<- 2*(cph_full$loglik[2]-cph_r1$loglik[2])</pre>
1-pchisq(stat1,1)
## [1] 0.9728894
#reduced model 2
cph_r2 <- coxph(Surv(time,censor)~.-priorzdv -id, data = aids)</pre>
cph_r2$loglik
## [1] -452.6325 -380.7389
cph_r2
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id, data = aids)
##
##
                  coef
                        exp(coef)
                                    se(coef)
                                                 z
## time d
             1.382e-03 1.001e+00
                                  2.111e-03 0.654
                                                    0.51285
             2.894e+00 1.807e+01
                                  3.831e-01 7.555 4.18e-14
## censor_d
## tx
            -3.910e-01 6.764e-01
                                   2.752e-01 -1.421
                                                    0.15535
## txgrp
                               NA 0.000e+00
                                                NA
                    NΑ
## strat2
             3.434e-01 1.410e+00
                                  4.388e-01 0.783
                                                   0.43391
## sexmale
             3.145e-01 1.370e+00
                                  3.516e-01 0.895 0.37103
## raceth
            -8.832e-02 9.155e-01
                                   1.542e-01 -0.573
                                                    0.56676
## ivdrug
            -3.621e-01 6.962e-01 1.928e-01 -1.878 0.06041
## hemophil -1.282e-01 8.797e-01 7.115e-01 -0.180
## karnof
            -4.404e-02 9.569e-01 1.546e-02 -2.849 0.00439
## cd4
            -1.592e-02 9.842e-01
                                  4.987e-03 -3.193
                                                    0.00141
## age20-30 -8.819e-01 4.140e-01 1.236e+00 -0.713 0.47563
## age30-40 -8.049e-01 4.472e-01 1.205e+00 -0.668
                                                   0.50419
           -6.981e-01 4.975e-01 1.196e+00 -0.584
## age40-50
                                                    0.55950
## age50-60 -3.908e-01 6.765e-01
                                  1.245e+00 -0.314
                                                    0.75354
## age60-70 -1.053e+00 3.488e-01
                                  1.603e+00 -0.657 0.51119
## ageover70 -1.403e+01 8.053e-07 2.692e+03 -0.005 0.99584
##
```

```
## Likelihood ratio test=143.8 on 16 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
stat2 \leftarrow 2*(cph_r1$loglik[2]-cph_r2$loglik[2])
1-pchisq(stat2,1)
## [1] 0.9569002
#reduced model 3
cph_r3 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil, data = aids)</pre>
cph_r3$loglik
## [1] -452.6325 -380.7555
cph_r3
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil,
       data = aids)
##
                  coef exp(coef)
                                    se(coef)
##
                                                  \mathbf{z}
            1.359e-03 1.001e+00 2.108e-03 0.645 0.51912
## time_d
## censor_d 2.882e+00 1.785e+01 3.765e-01 7.654 1.94e-14
## tx
            -3.895e-01 6.774e-01 2.752e-01 -1.415 0.15692
                               NA 0.000e+00
## txgrp
                    NΑ
                                                 NΑ
                                                          NΑ
## strat2 3.381e-01 1.402e+00 4.387e-01 0.771 0.44085
## sexmale 3.186e-01 1.375e+00 3.509e-01 0.908 0.36394
## raceth
            -8.537e-02 9.182e-01 1.530e-01 -0.558 0.57691
## ivdrug -3.605e-01 6.973e-01 1.927e-01 -1.871 0.06135
## karnof -4.402e-02 9.569e-01 1.546e-02 -2.847 0.00441
## cd4
          -1.600e-02 9.841e-01 4.990e-03 -3.206 0.00134
## age20-30 -7.754e-01 4.605e-01 1.089e+00 -0.712 0.47650
## age30-40 -6.919e-01 5.006e-01 1.032e+00 -0.670 0.50275
## age40-50 -5.925e-01 5.529e-01 1.045e+00 -0.567 0.57085
## age50-60 -2.756e-01 7.591e-01 1.071e+00 -0.257 0.79702
## age60-70 -9.293e-01 3.948e-01 1.451e+00 -0.640 0.52190
## ageover70 -1.391e+01 9.074e-07 2.692e+03 -0.005 0.99588
##
## Likelihood ratio test=143.8 on 15 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
tat3 \leftarrow 2*(cph_r3$loglik[2]-cph_r2$loglik[2])
1-pchisq(stat3,1)
## [1] 1
#reduced model 4
cph_r4 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth, data = aids)
cph_r4$loglik
## [1] -452.6325 -380.9154
cph_r4
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
##
      raceth, data = aids)
##
                  coef exp(coef)
##
                                    se(coef)
                                                           р
```

```
## time d
            1.282e-03 1.001e+00 2.093e-03 0.612 0.54042
## censor d 2.861e+00 1.748e+01 3.737e-01 7.657 1.91e-14
## tx
            -3.907e-01 6.766e-01 2.752e-01 -1.419 0.15576
## txgrp
                    NA
                               NA 0.000e+00
                                                NA
## strat2 3.386e-01 1.403e+00 4.373e-01 0.774 0.43871
## sexmale 3.215e-01 1.379e+00 3.487e-01 0.922 0.35665
## ivdrug
            -3.823e-01 6.823e-01 1.886e-01 -2.027 0.04265
## karnof
            -4.462e-02 9.564e-01 1.549e-02 -2.880 0.00397
## cd4
            -1.588e-02 9.842e-01 4.961e-03 -3.202 0.00137
## age20-30 -7.510e-01 4.719e-01 1.087e+00 -0.691 0.48974
## age30-40 -6.587e-01 5.175e-01 1.030e+00 -0.639 0.52254
## age40-50 -5.503e-01 5.768e-01 1.042e+00 -0.528 0.59749
## age50-60 -2.362e-01 7.896e-01 1.069e+00 -0.221 0.82503
## age60-70 -8.498e-01 4.275e-01 1.444e+00 -0.589 0.55611
## ageover70 -1.389e+01 9.263e-07 2.698e+03 -0.005 0.99589
## Likelihood ratio test=143.4 on 14 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
tat4 \leftarrow 2*(cph_r3$loglik[2]-cph_r4$loglik[2])
1-pchisq(stat4,1)
## [1] 0.5718012
#reduced model 5
cph_r5 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth -time_d, data = aids)
cph_r5$loglik
## [1] -452.6325 -381.1059
cph_r5
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
##
      raceth - time_d, data = aids)
##
##
                  coef exp(coef)
                                   se(coef)
## censor_d 2.741e+00 1.550e+01 3.178e-01 8.625 < 2e-16
            -4.008e-01 6.698e-01 2.738e-01 -1.464 0.14321
## tx
## txgrp
                    NA
                               NA 0.000e+00
                                                NA
## strat2
            3.581e-01 1.431e+00 4.351e-01 0.823 0.41051
## sexmale 2.735e-01 1.315e+00 3.409e-01 0.802 0.42232
## ivdrug
            -3.773e-01 6.857e-01 1.881e-01 -2.006 0.04487
## karnof
            -4.545e-02 9.556e-01 1.539e-02 -2.953 0.00315
## cd4
            -1.602e-02 9.841e-01 4.953e-03 -3.234 0.00122
## age20-30 -6.860e-01 5.036e-01 1.082e+00 -0.634 0.52598
## age30-40 -5.895e-01 5.546e-01 1.024e+00 -0.576 0.56483
## age40-50 -4.787e-01 6.196e-01 1.036e+00 -0.462 0.64393
## age50-60 -1.506e-01 8.602e-01 1.059e+00 -0.142 0.88700
## age60-70 -8.000e-01 4.493e-01 1.443e+00 -0.554 0.57945
## ageover70 -1.383e+01 9.889e-07 2.663e+03 -0.005 0.99586
##
## Likelihood ratio test=143.1 on 13 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
stat5 \leftarrow 2*(cph_r5\$loglik[2]-cph_r4\$loglik[2])
1-pchisq(stat5,1)
```

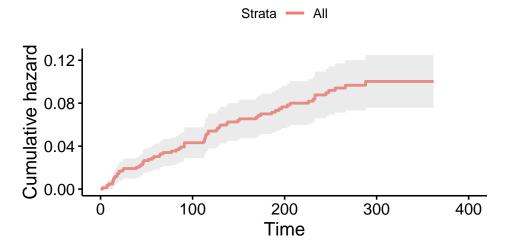
```
## [1] 1
#reduced model 6
cph_r6 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth -time_d -strat2, data = aids)
cph_r6$loglik
## [1] -452.6325 -381.4390
cph_r6
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
      raceth - time_d - strat2, data = aids)
##
##
                  coef exp(coef)
                                    se(coef)
                                                  z
## censor d
             2.727e+00 1.529e+01 3.159e-01 8.635 < 2e-16
## tx
            -4.203e-01 6.568e-01 2.726e-01 -1.542 0.12303
## txgrp
                    NA
                               NA 0.000e+00
                                                 NA
           2.625e-01 1.300e+00 3.415e-01 0.769 0.44201
## sexmale
## ivdrug
            -3.941e-01 6.743e-01 1.873e-01 -2.104 0.03542
## karnof
            -4.573e-02 9.553e-01 1.541e-02 -2.967 0.00301
## cd4
            -1.295e-02 9.871e-01 3.012e-03 -4.301 1.7e-05
## age20-30 -6.334e-01 5.308e-01 1.079e+00 -0.587 0.55725
## age30-40 -5.580e-01 5.723e-01 1.023e+00 -0.546 0.58539
## age40-50 -4.327e-01 6.487e-01 1.033e+00 -0.419 0.67536
## age50-60 -7.496e-02 9.278e-01 1.054e+00 -0.071 0.94333
## age60-70 -6.578e-01 5.180e-01 1.430e+00 -0.460 0.64555
## ageover70 -1.369e+01 1.138e-06 2.679e+03 -0.005 0.99592
## Likelihood ratio test=142.4 on 12 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
tat6 \leftarrow 2*(cph_r5$loglik[2]-cph_r6$loglik[2])
1-pchisq(stat6,1)
## [1] 0.4144233
#reduced model 7
cph_r7 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth -time_d -strat2 -sex,
               data = aids)
cph_r7$loglik
## [1] -452.6325 -381.7212
cph_r7
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
      raceth - time_d - strat2 - sex, data = aids)
##
##
##
                  coef exp(coef)
                                    se(coef)
## censor_d
             2.723e+00 1.523e+01 3.140e-01 8.672 < 2e-16
             -4.284e-01 6.516e-01 2.723e-01 -1.573 0.11567
## tx
## txgrp
                    NA
                               NA 0.000e+00
                                                 NA
                                                          NA
## ivdrug
            -4.023e-01 6.688e-01 1.875e-01 -2.146 0.03189
            -4.622e-02 9.548e-01 1.530e-02 -3.020 0.00253
## karnof
## cd4
             -1.301e-02 9.871e-01
                                   3.012e-03 -4.319 1.57e-05
## age20-30 -5.567e-01 5.731e-01 1.074e+00 -0.518 0.60438
## age30-40 -5.760e-01 5.621e-01 1.023e+00 -0.563 0.57333
## age40-50 -4.452e-01 6.407e-01 1.034e+00 -0.431 0.66667
```

```
## age50-60 -4.385e-02 9.571e-01 1.054e+00 -0.042 0.96680
## age60-70 -6.931e-01 5.000e-01 1.429e+00 -0.485 0.62774
## ageover70 -1.373e+01 1.093e-06 2.690e+03 -0.005 0.99593
## Likelihood ratio test=141.8 on 11 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
tat7 \leftarrow 2*(cph_r6\$loglik[2]-cph_r7\$loglik[2])
1-pchisq(stat7,1)
## [1] 0.45249
#reduced model 8
cph_r8 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth -time_d -strat2
                -sex -txgrp -age, data = aids)
cph_r8$loglik
## [1] -452.6325 -383.0225
cph_r8
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
##
       raceth - time_d - strat2 - sex - txgrp - age, data = aids)
##
##
                 coef exp(coef) se(coef)
## censor_d 2.801853 16.475139 0.303119 9.243 < 2e-16
           -0.406626  0.665893  0.267694  -1.519  0.12876
## ivdrug -0.401503 0.669313 0.187580 -2.140 0.03232
## karnof -0.045366 0.955648 0.015162 -2.992 0.00277
## cd4
           -0.012959 0.987125 0.003004 -4.314 1.61e-05
## Likelihood ratio test=139.2 on 5 df, p=< 2.2e-16
## n= 851, number of events= 69
#likelihood ratio test
tat8 \leftarrow 2*(cph_r7\$loglik[2]-cph_r8\$loglik[2])
1-pchisq(stat8,1)
## [1] 0.1066782
#reduced model 9
cph_r9 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth -time_d -strat2 -sex
                -txgrp -age -tx, data = aids)
cph_r9$loglik
## [1] -452.6325 -384.2077
cph_r9
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
       raceth - time_d - strat2 - sex - txgrp - age - tx, data = aids)
##
##
##
                 coef exp(coef) se(coef)
## censor_d 2.919993 18.541150 0.293976 9.933 < 2e-16
## ivdrug -0.379834 0.683975 0.186804 -2.033 0.04202
## karnof -0.045797 0.955235 0.015201 -3.013 0.00259
           -0.013233  0.986854  0.002997  -4.415  1.01e-05
## cd4
##
```

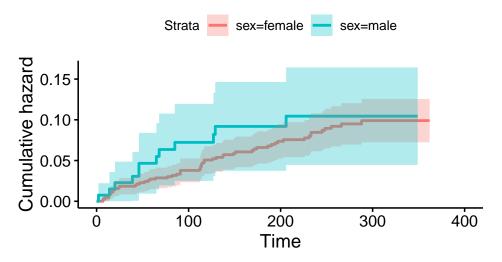
```
## Likelihood ratio test=136.8 on 4 df, p=< 2.2e-16
## n= 851, number of events= 69
###best model using backwards selection?
#likelihood ratio test
stat9 <- 2*(cph_r8$loglik[2]-cph_r9$loglik[2])
1-pchisq(stat9,1)
## [1] 0.1236681
#reduced model 10
cph_r10 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth -time_d -strat2 -sex
                 -txgrp -age -tx -censor_d, data = aids)
cph_r10$loglik
## [1] -452.6325 -417.9688
cph_r10
## Call:
## coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
       raceth - time_d - strat2 - sex - txgrp - age - tx - censor_d,
##
       data = aids)
##
##
               coef exp(coef) se(coef)
                                             z
                                                       p
## ivdrug -0.216832  0.805065  0.180491 -1.201
                                                    0.23
## karnof -0.061043 0.940783 0.014157 -4.312 1.62e-05
## cd4
         -0.015127  0.984987  0.003076  -4.917  8.77e-07
##
## Likelihood ratio test=69.33 on 3 df, p=5.947e-15
## n= 851, number of events= 69
#NOTE: should we take out censor_d anyways since its related to censor or keep it?
#likelihood ratio test
stat10 <- 2*(cph_r9$loglik[2]-cph_r10$loglik[2])
1-pchisq(stat10,1)
## [1] 2.220446e-16
coxph(Surv(time_d,censor_d) ~ sex , data=aids) %>% tidy()
## # A tibble: 1 x 7
             estimate std.error statistic p.value conf.low conf.high
    term
##
    <chr>
                <dbl>
                          <dbl>
                                    <dbl>
                                            <dbl>
                                                      <dbl>
                                                                <dbl>
                0.390
                          0.559
                                    0.697
                                            0.486
                                                     -0.706
                                                                 1.49
## 1 sexmale
coxph(Surv(time,censor) ~ sex, data=aids) %>% tidy()
## # A tibble: 1 x 7
##
   term
             estimate std.error statistic p.value conf.low conf.high
    <chr>>
                <dbl>
                                    <dbl>
                                            <dbl>
                          <dbl>
                                                      <dbl>
                                    0.625
                                            0.532
## 1 sexmale
                0.199
                          0.318
                                                    -0.424
                                                                0.821
coxph(Surv(time,censor) ~ age+ txgrp+ karnof, data=aids) %>% tidy()
## # A tibble: 8 x 7
               estimate std.error statistic
                                                  p.value conf.low conf.high
   term
##
                 <dbl>
                           <dbl>
                                                     <dbl>
                                                              <dbl>
                                                                        <dbl>
    <chr>>
                                      <dbl>
## 1 age20-30
               -0.438
                           1.07
                                   -0.409
                                            0.682
                                                             -2.53
                                                                       1.66
               -0.442
                           1.02
                                   -0.434
                                            0.665
                                                             -2.44
                                                                       1.55
## 2 age30-40
## 3 age40-50
               -0.361
                           1.03
                                   -0.352
                                            0.725
                                                             -2.37
                                                                       1.65
## 4 age50-60
                 0.460
                           1.04
                                    0.442
                                            0.659
                                                             -1.58
                                                                       2.50
```

```
## 5 age60-70
               -0.780
                           1.42
                                   -0.551
                                            0.582
                                                            -3.55
                                                                       2.00
                                   -0.00525 0.996
## 6 ageover70 -14.1
                        2688.
                                                          -Inf
                                                                    Tnf
## 7 txgrp
                -0.844
                           0.257
                                   -3.28
                                            0.00103
                                                             -1.35
                                                                      -0.340
                -0.0814
                           0.0138 -5.89
                                            0.0000000385
                                                            -0.109
                                                                      -0.0543
## 8 karnof
cox.zph(coxph(Surv(time,censor) ~ age + txgrp+karnof, data=aids))
##
                  rho
                         chisq
## age20-30
              0.09054 5.70e-01 0.450
## age30-40
              0.19294 2.53e+00 0.112
## age40-50
              0.14871 1.50e+00 0.220
## age50-60
              0.19861 2.69e+00 0.101
## age60-70
              0.16251 1.81e+00 0.179
## ageover70
             0.16355 2.57e-07 1.000
             -0.10779 8.34e-01 0.361
## txgrp
              0.00121 1.03e-04 0.992
## karnof
## GLOBAL
                   NA 7.98e+00 0.435
coxph(Surv(time,censor) ~ age *txgrp*karnof, data=aids) %>% tidy()
## # A tibble: 27 x 7
##
     term
                     estimate std.error statistic p.value conf.low conf.high
##
      <chr>
                                                     <dbl>
                      <dbl>
                                  <dbl>
                                             <dbl>
                                                              <dbl>
                                138081. 0.00222
##
   1 age20-30
                       307.
                                                     0.998
                                                               -Inf
                                                                           Inf
##
   2 age30-40
                       319.
                                138081. 0.00231
                                                    0.998
                                                               -Inf
                                                                           Inf
## 3 age40-50
                                138081. 0.00237
                                                   0.998
                       327.
                                                               -Inf
                                                                           Tnf
##
  4 age50-60
                       343.
                                138081. 0.00248
                                                     0.998
                                                               -Inf
                                                                          Inf
                                176360. 0.00163
##
  5 age60-70
                       287.
                                                     0.999
                                                               -Inf
                                                                           Inf
                       -1.66
                                 29411. -0.0000565 1.000
                                                               -Inf
##
   6 ageover70
                                                                           Inf
## 7 txgrp
                       150.
                                92258. 0.00163
                                                     0.999
                                                               -Inf
                                                                           Inf
##
                         3.36
                                 1422. 0.00236
                                                     0.998
                                                               -Inf
                                                                           Inf
   8 karnof
   9 age20-30:txgrp -144.
                                 92258. -0.00156
                                                     0.999
                                                                -Inf
                                                                           Inf
                                 92258. -0.00158
## 10 age30-40:txgrp -146.
                                                     0.999
                                                               -Inf
                                                                           Inf
## # ... with 17 more rows
cox.zph(coxph(Surv(time,censor) ~ age *txgrp*karnof, data=aids))
                                     chisq
## age20-30
                          -0.1005 4.30e-08 1.000
## age30-40
                          -0.1581 3.14e-08 1.000
## age40-50
                          -0.0961 1.24e-08 1.000
## age50-60
                          -0.2070 6.52e-08 1.000
                          -0.2060 3.03e-08 1.000
## age60-70
## ageover70
                          -0.2476 7.66e-11 1.000
                          -0.2030 2.66e-08 1.000
## txgrp
## karnof
                          -0.1972 5.23e-08 1.000
## age20-30:txgrp
                           0.0918 2.13e-08 1.000
## age30-40:txgrp
                           0.1139 1.07e-08 1.000
                           0.0820 5.56e-09 1.000
## age40-50:txgrp
                           0.1849 3.46e-08 1.000
## age50-60:txgrp
## age60-70:txgrp
                           0.2099 2.14e-08 1.000
## ageover70:txgrp
                           0.1974 3.99e-11 1.000
## age20-30:karnof
                           0.0981 4.52e-08 1.000
## age30-40:karnof
                           0.1522 3.43e-08 1.000
## age40-50:karnof
                           0.0934 1.39e-08 1.000
## age50-60:karnof
                           0.2052 7.76e-08 1.000
## age60-70:karnof
                           0.1977 2.99e-08 1.000
## ageover70:karnof
                               NA
                                       {\tt NaN}
                                             NaN
## txgrp:karnof
                           0.1994 2.79e-08 1.000
```

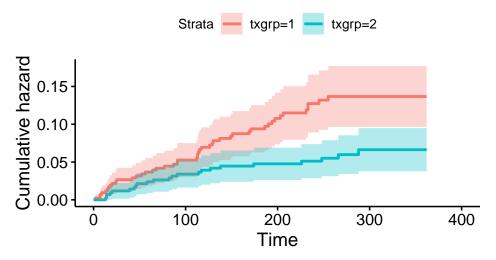
### **Estimated Hazard rates**



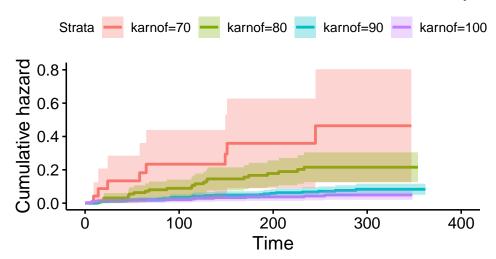
## Estimated Hazard rates based on sex



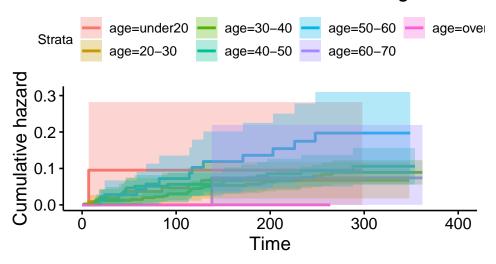
### Estimated Hazard rates based on treatment

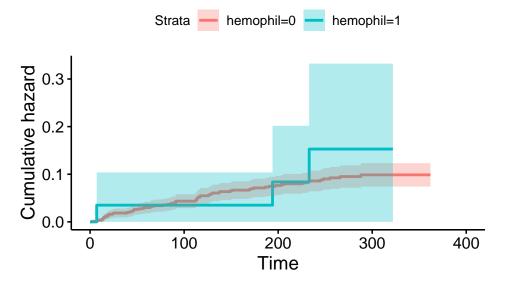


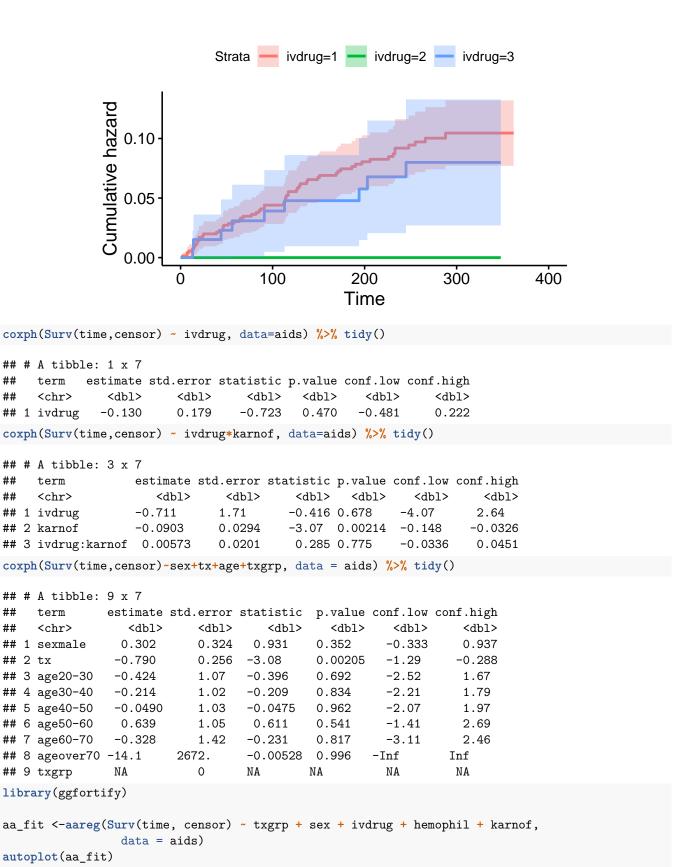
## Estimated Hazard rates based on klarnfsky



## Estimated Hazard rates based on age







##

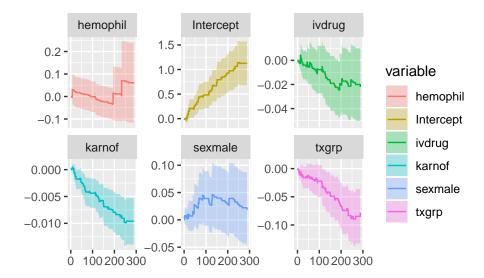
##

##

##

##

## 2 tx



The Aalen model assumes that the cumulative hazard H(t) for a subject can be expressed as a(t) + X B(t), where a(t) is a time-dependent intercept term, X is the vector of covariates for the subject possibly time-dependent, and B(t) is a time-dependent matrix of coefficients.

The plots show how the effects of the covariates change over time.

### Patricia's "Something New"

I will be doing a power analysis by simulating survival analysis curves

#### 1. What is the topic?

The topic is using sim.survdata in R to simulate survival data. Using that simulated data, we will make that the alternative and control for the coefficient beta by setting it equal to some value. Then using power analysis, we will see how many times we reject  $H_0$ .

#### 2. How it is relevant? How it relates to survival analysis/analysis at hand?

Power analysis relates to survival analysis because if power is large after comparing our data to the simulated survival data, this tells us that there is a high chance that we would reject the null in favor of the alternative (control versus treatment?)

#### 3. Resources to learn about the topic.

Below are some of the resources I have begun to use to learn about creating simulations of survival curves and performing power analysis:

a).  $https://cran.r-project.org/web/packages/coxed/vignettes/simulating\_survival\_data.html~b).~http://www.icssc.org/documents/advbiosgoa/tab\%2026.00\_survss.pdf$ 

#### 4. What will be challenging about learning something new?

Learning something new will be challenging because in this case, the concept of power analysis is something I just recently learned in Intro to Statistics. So learning to apply this concept in the context of survival analysis curves

will be a challenge for me to learn. Learning how to simulate survival curves will also be challenging because I will have to learn how to use and interpret new functions in R.

#### Power Analysis code and simulation

```
simdata <- sim.survdata(N=1000, T=100, num.data.frames=1, beta = c(0.01,0.07,0.3))
head(simdata$data,10)
##
              X1
                          X2
                                     ХЗ
                                          y failed
## 1
       34
                                              TRUE
## 2
      0.01384654 -1.89955331 -1.1296499
                                          2
                                             FALSE
## 3
      0.48610593 -0.06788361 -0.7928867
                                              TRUE
                                         98
## 4
      0.51671053  0.30832579  0.5916228
                                         33
                                              TRUE
## 5 -0.49061845 -0.07541795 -0.8431818 100
                                              TRUE
## 6
      0.34518709 -0.61589930 -0.1059686
                                              TRUE
                                         96
## 7
     -1.24719594 -0.43437948 -0.1640219
                                         95
                                              TRUE
## 8 -1.96050359 0.41345164 0.3364959
                                              TRUE
                                         96
## 9 -1.54638010 0.21906593 -2.5576578
                                         56
                                              TRUE
## 10 0.49173672 0.81528552 -0.5025144
                                              TRUE
simdata$betas
##
        [,1]
## [1,] 0.01
## [2,] 0.07
## [3,] 0.30
head(simdata$baseline,10)
##
      time failure.PDF failure.CDF survivor
                                                 hazard
## 1
         ## 2
        2 0.024567830 0.05240683 0.9475932 0.025271360
## 3
        3 0.021501111 0.07390794 0.9260921 0.022690234
## 4
        4 0.018638839
                       0.09254678 0.9074532 0.020126335
## 5
        5 0.015981016 0.10852779 0.8914722 0.017610842
## 6
         6 0.013527640
                       0.12205543 0.8779446 0.015174495
## 7
        7 0.011278713
                       0.13333415  0.8666659  0.012846725
## 8
        8 0.009234233
                       0.14256838 0.8574316 0.010654894
## 9
         9 0.007394201
                       0.14996258 0.8500374 0.008623663
## 10
       10 0.005758618 0.15572120 0.8442788 0.006774546
\#ggsurvplot(survfit(Surv(y,failed) \sim X1 + X2 + X3, data = simdata\$data))
model <- coxph(Surv(y, failed) ~ X1 + X2 + X3, data = simdata$data)</pre>
library(dplyr)
library(broom)
model %>% tidy()
## # A tibble: 3 x 7
##
    term
          estimate std.error statistic
                                         p.value conf.low conf.high
##
     <chr>>
              <dbl>
                       <dbl>
                                 <dbl>
                                           <dbl>
                                                    <dbl>
                                                              <dbl>
## 1 X1
             0.0712
                      0.0330
                                  2.16 0.0311
                                                  0.00648
                                                              0.136
## 2 X2
             0.0478
                      0.0337
                                  1.42 0.156
                                                 -0.0182
                                                              0.114
## 3 X3
             0.126
                      0.0321
                                  3.91 0.0000908 0.0628
                                                              0.189
n.reps <- 100
simoutput <- c()
for(i in 1:n.reps){
```

```
simdata <- sim.survdata(N=1000, T=100, num.data.frames=1, xvars=4,beta = c(0,0.01,0.07,0.3))
  model <- coxph(Surv(y, failed) ~ X1 + X2 + X3 + X4, data = simdata$data)</pre>
  simoutput <- rbind(simoutput, cbind(rep = rep(i, 4), model %>% tidy()))
}
#simoutput
#sum(which(simoutput$p.value < 0.05))
sum(simoutput$p.value <0.05)</pre>
## [1] 134
#simoutput%>%filter(term=="X1")%>%summarize(sum(p.value<0.05))</pre>
simoutput%%dplyr::filter(term=="X1")%%dplyr::summarize(sum(p.value<0.05))
##
     sum(p.value < 0.05)
## 1
simoutput%%dplyr::filter(term=="X2")%%dplyr::summarize(sum(p.value<0.05))
     sum(p.value < 0.05)
##
## 1
simoutput%%dplyr::filter(term=="X3")%%dplyr::summarize(sum(p.value<0.05))
##
     sum(p.value < 0.05)
## 1
simoutput%>%dplyr::filter(term=="X4")%>%dplyr::summarize(sum(p.value<0.05))</pre>
     sum(p.value < 0.05)
## 1
                       93
```

### Juste's "Something New"

I will be analyzing the Shoenfeld residuals for the Cox PH model.

# 1. What is goign on? What is the topic? 2. How it is relevant? How it relates to survival analysis/analysis at hand?

Cox proportional hazards (PH) model is considered a great way to identify combined effects of several covariates on the relative risk (hazard). This model assumes that the hazards of the different strata formed by the levels of the covariates are proportional. This proportional hazards assumption is particularly important and can be tested via three different clases of tests. The first class is focused on the piecewise estimation of models for subsets of data defined by stratification of time. The second one considers the interactions between covariates and some function of time. Final, third one is based on examinations of regression residuals. The Schoenfeld Residuals are a part of the third class of proportional hazard assumption testing and I will be exploring it in order to be able to eradicate a method for testing for the PH assumption in the current and future data set analyses. This topic is particularly important in relation to survival analysis since it provides an idea of whether the model is appropriate for the data set at hand and whether some covariates should be considered as variants of time in order to supply the best model for prediction of proportional hazards.

#### 3. Resources to learn about the topic.

I have been researching articles and scientific journals that provide insights into the Schoenfeld residuals and their use in the Cox PH model. Sources include:

- 1. https://onlinelibrary.wiley.com/doi/full/10.1111/ajps.12176
- 2. https://rstudio-pubs-static.s3.amazonaws.com/39354 34153ff19e624116bd2fbdec7d2534aa.html

#### 4. What will be challenging about learning something new?

Taking a completely new model of analyzing survival data is particularly difficult since the mathematical derivations and notations are also very varied from what we have seen in class. Although, I do remember some of the ideas behind parametric functions, their applications to statistical models are much more challenging than I have expected. Therefore, it will require me a lot of time and extensive research to be able to understand and learn how to apply this model to our data and other instances of survival analysis.

#### Explanation of the Theory Behind Schoenfeld Residuals

Let  $z_{ij}(t)$  be the  $j^{th}$  covariate of the  $i^{th}$  unit, where i = 1, 2, ..., n and j = 1, 2..., p

This notation indicates that  $z_{ij}$  is allowed to vary as a function of the time scale.

- 1) As we know from lecture, the Cox PH model assumes that h(t) of the  $i^{th}$  individual satisfies:
- $h_i(t) = h_0(t)e^{z_i(t)\beta}$  where:
- $h_0$  -> baseline hazard
- $z_i(t) \rightarrow 1 \times p$  vector of covariates for unit i each of which can be time fixed or time-varying.
- 2) However, another possibility has been presented by Therneau and Granbsh in 2000, where they proposed an idea that there ciuyld be an alternative to the current Cox model, where the coefficient of the estimate could also be varying as a function of time.

The new hazard function would look like this:  $h_i(t) = h_0(t)e^{z_i(t)\beta(t)}$ 

Therefore, in order to examine thee two models in a case when  $\beta = \beta(t)$  requires a residual analysis that could indicate whether a model should consider a covariate as a variable with time.

Due to the fact that that some observations might be censored and in particular, regarding the Cox PH model, the baseline hazard is not estimated, in oprder to analyse the residuals a particular score process. The risk score for unit i at time t is thought to be  $r_i(t) = e^{z_i(t)\beta}$ , where  $Y_i(t)$  is the indicator function and  $Y_i(t) = 1$  indicates a point in which i is under risk and thus observation and it is equal to 0 in other occasions.

The Schoenfeld residuals are given by the equations:

1. 
$$s_k = Z_{(k)} - \frac{\sum_i Y_i(t_k) r_i(t_k) Z_i(t_k)}{\sum_i Y_i(t_k) r_i(t_k)}$$
  
2.  $s_k = Z_{(k)} - \bar{z}(\hat{\beta}, t_k)$ 

In this case, the Z(k) is the covariate vector of the particular unit that is experiencing the evnt at time k;  $\hat{\beta}$  is the estimate of  $\beta$  and  $\bar{z}(\hat{\beta}, t_k)$  is the wighted mean of covariate values.

Furthermore, the weighted variance can be represented by the derived equation at the  $k^{th}$  time as

$$V(\beta, t_k) = \sum_{i} Y_i(t_k) r_i(t_k) Z_i(t_k) - \bar{z}(\hat{\beta}, t_k)' Z_i(t_k) - \frac{\bar{z}(\hat{\beta}, t_k)}{\sum_{i} Y_i(t_k) r_i(t_k)}$$

From this, we can scale the Schoenfeld residuals by  $V(\beta, t_k)$  of X at  $t_k$  via the equation:

$$s_k^* = V^{-1}(\hat{\beta}, t_k) s_k$$

The scaled Schoenfeld residuals can also be defined as follows:

$$s_k^* = m \sum_{k=1}^d V(\hat{\beta}, t_k) s_k$$

here, m is the total number of deaths in the data set.

Following the calculations, the residuals are plotted against time in order to test the prportional hazards assumption. If the assumption is correct, the residuals should be fiting around the line centered at zero (y=0). The further away this predicted line is form the horizontal of (y=0) the more likely one is to call the PH assumption to question and determine whether it is met through the model.

To go a little deeper into the analysis of the resiaul calculation, one can look at the calculations of the test statistic for this residual mdoel.

By producing a least squares slope of regression and assuming a relationship between  $s_{kj}^*$  and  $t_{kj}$  or some function  $g(t_k)$  allows to derive a test statistic for the proportional hazards assumption in regards to the  $j^{th}$  covariate, which is given by:

$$T_j = \frac{\left[\sum_{k=1}^d (g(t_k) - \hat{g}) s_{kj}^8\right]^2}{dI^{jj} \sum_{k=1}^d (g(t_k) - \hat{g})^2}$$

## karnof -0.0630 0.2834 0.595

0.1524 1.4618 0.227

## cd4

Here, the distribution is asymptotical as  $X^2(1)$  stating the null hypothesis that the relationship between the covariate, in this case j and the event time follows the assumption of PH.

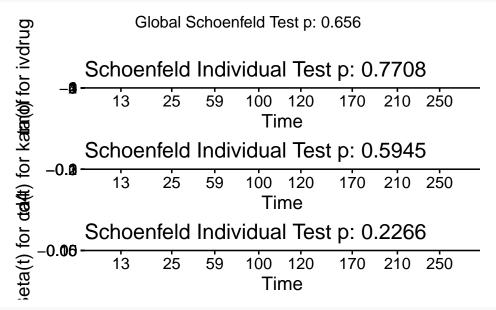
Interpretation of Schoenfeld Residuals from plots in R and the p-values presented.

The y-axis of the Schoenfeld residuals graph can be interpreted as the log of the hazard ratio for the explanatory variable—the coefficient in Cox's model if it were allow to vary over time. If the graph is flat, then the PH assumption is adequate. Furthermore, the Schoenfeld residuals are independent of time. A plot that shows a non-random pattern against time is evidence of violation of the PH assumption. The PH assumption is supported when there's a non-significan relationship between residuals and time. ### HIV Data Cox PH model analysis using Schoenfeld Residuals

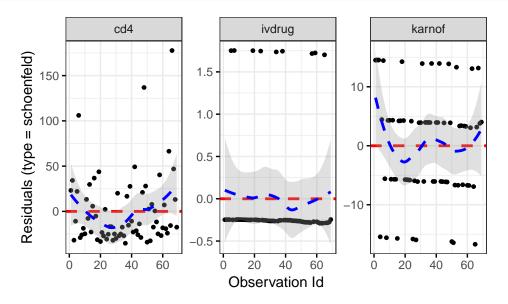
Schoenfeld Residuals applied to our best Cox PH model for AIDS data where, we have an additive model of explanatory variables: baseline cd4 count, iv drug use history, and karnofsky performance scale score:

```
cph r10 <- coxph(Surv(time,censor)~.-priorzdv -id -hemophil -raceth -time d -strat2
                 -sex -txgrp -age -tx -censor_d, data = aids)
cph_r10
## Call:
  coxph(formula = Surv(time, censor) ~ . - priorzdv - id - hemophil -
##
##
       raceth - time_d - strat2 - sex - txgrp - age - tx - censor_d,
##
       data = aids)
##
##
               coef exp(coef)
                               se(coef)
                                                       p
## ivdrug -0.216832 0.805065
                               0.180491 -1.201
                                                    0.23
## karnof -0.061043
                     0.940783
                               0.014157 -4.312 1.62e-05
## cd4
          -0.015127
                     0.984987
                               0.003076 -4.917 8.77e-07
##
## Likelihood ratio test=69.33 on 3 df, p=5.947e-15
## n= 851, number of events= 69
zph_r10 <- cox.zph(cph_r10)</pre>
zph_r10
##
              rho chisq
## ivdrug -0.0348 0.0849 0.771
```

ggcoxzph(zph\_r10)



ggcoxdiagnostics(cph\_r10, type="schoenfeld")



Using the best determined Cox PH model for our data, we can look at the Schoenfeld residuals to determine if the PH assumption is met. Via the function "ggcoxzph()", which produces, for each covariate, graphs of the scaled Schoenfeld residuals against the transformed time. Here, the solid line is a smoothing spline fit to the plot, with the dashed lines representing a +/- 2-standard-error. from these graphs, we don't see any patterns or significance of the residual fit regarding the graphs of the covariates with time. Therefore, the assumption of proportional hazrads seems to be supported for the covariates: baseline cd4 count, iv drug use history, and karnofsky performance scale score.

Using the ggcoxdiagnostics() function we can provide another graphic representation of the residual distribution in regards to the covariates with time. Here, we also see that there's no particular pattern of the residuals around the line of fit, threfore again, we can state that the PH assumption has been met.