Data Analysis

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knitr::opts chunk$set(message=FALSE, warning=FALSE, fig.height=3, fig.width=5, fig.align="center")
library(tidyverse)
library(broom)
library(plyr)
library(survival)
library(survminer)
aids <- read.csv( "http://pages.pomona.edu/~jsh04747/courses/math150/AIDSdata.csv")
dim(aids)
```

[1] 851 16

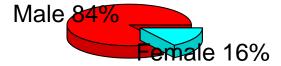
summary(aids)

```
##
          id
                                                               time_d
                            time
                                            censor
##
    Min.
           :
                1.0
                      Min.
                              : 1.0
                                               :0.00000
                                                           Min.
                                                                  : 1.0
    1st Qu.: 287.5
                      1st Qu.:179.5
                                       1st Qu.:0.00000
                                                           1st Qu.:199.5
    Median : 581.0
                      Median :257.0
                                       Median :0.00000
                                                           Median :266.0
##
##
    Mean
           : 579.5
                      Mean
                              :231.8
                                       Mean
                                               :0.08108
                                                           Mean
                                                                   :243.4
##
    3rd Qu.: 873.0
                      3rd Qu.:300.0
                                       3rd Qu.:0.00000
                                                           3rd Qu.:306.0
##
    Max.
            :1156.0
                              :362.0
                                               :1.00000
                                                                   :362.0
                      Max.
                                       Max.
                                                           Max.
##
       censor d
                                                              strat2
                             tx
                                             txgrp
                              :0.0000
##
            :0.0000
                                                                 :0.0000
    Min.
                                                :1.000
                      Min.
                                        Min.
                                                          Min.
##
    1st Qu.:0.0000
                      1st Qu.:0.0000
                                         1st Qu.:1.000
                                                          1st Qu.:0.0000
##
    Median :0.0000
                      Median :1.0000
                                        Median :2.000
                                                          Median :1.0000
##
    Mean
            :0.0235
                      Mean
                              :0.5041
                                         Mean
                                                :1.504
                                                          Mean
                                                                 :0.6157
##
    3rd Qu.:0.0000
                      3rd Qu.:1.0000
                                         3rd Qu.:2.000
                                                          3rd Qu.:1.0000
##
            :1.0000
                              :1.0000
                                                :2.000
                                                                 :1.0000
##
         sex
                         raceth
                                           ivdrug
                                                           hemophil
##
    Min.
           :1.000
                     Min.
                             :1.000
                                      Min.
                                              :1.000
                                                        Min.
                                                               :0.00000
```

```
1st Qu.:1.000
                     1st Qu.:1.000
                                     1st Qu.:1.000
                                                      1st Qu.:0.00000
##
    Median :1.000
                                                      Median :0.00000
##
                     Median :1.000
                                     Median :1.000
           :1.157
##
    Mean
                     Mean
                            :1.706
                                     Mean
                                            :1.317
                                                      Mean
                                                              :0.03408
    3rd Qu.:1.000
                     3rd Qu.:2.000
                                                      3rd Qu.:0.00000
##
                                     3rd Qu.:1.000
##
    Max.
           :2.000
                     Max.
                            :5.000
                                             :3.000
                                                              :1.00000
        karnof
                           cd4
                                           priorzdv
##
                                                               age
##
   Min.
           : 70.00
                      Min.
                             : 0.00
                                       Min.
                                              : 3.00
                                                         Min.
                                                                 :15.00
                      1st Qu.: 22.25
    1st Qu.: 90.00
##
                                        1st Qu.: 11.00
                                                          1st Qu.:33.00
##
    Median : 90.00
                      Median : 75.00
                                       Median : 21.00
                                                          Median :38.00
##
   Mean
           : 91.34
                      Mean
                             : 86.45
                                       Mean
                                               : 30.63
                                                          Mean
                                                                 :38.81
##
    3rd Qu.:100.00
                      3rd Qu.:135.75
                                        3rd Qu.: 44.00
                                                          3rd Qu.:44.00
           :100.00
                             :348.00
##
    Max.
                      Max.
                                        Max.
                                               :288.00
                                                          Max.
                                                                 :73.00
```

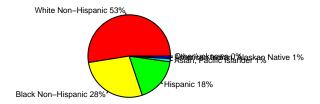
The data set contains a sample size equal to 851 participants and 16 different variables.

Gender Distribution



The Pie Chart represents the gender distribution in the sample, with 84% male and 16% female. This shows the potential for the data to not be able to correctly represent the difference of the data variance by gender, if there were to be one. Therefore, gender is something to look into in future data analysis.

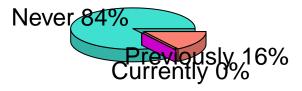
```
wnh<-sum(aids$raceth==1)
bnh<-sum(aids$raceth==2)
h<-sum(aids$raceth==3)
api<-sum(aids$raceth==4)
aian<-sum(aids$raceth==5)
oth<-sum(aids$raceth==6)
slices <- c(wnh,bnh,h,api,aian,oth)
lbls <- c("White Non-Hispanic", "Black Non-Hispanic", "Hispanic", "Asian, Pacific Islander", "American Ispect <- round(slices/sum(slices)*100)
lbls <- paste(lbls, pct)
lbls <- paste(lbls, "%",sep="")
pie(slices,lbls,col = rainbow(length(lbls)), cex=0.5 )</pre>
```



The distribution of race/ethnicity shows that the greatest number of participants consists of white non-hispanic identifying indiciduals, with black non-hispanic following and hispanic as the 3rd largest represented group.

```
never<-sum(aids$ivdrug==1)
cur<-sum(aids$ivdrug==2)
prev<-sum(aids$ivdrug==3)
slices <- c(never,cur,prev)
lbls <- c("Never", "Currently", "Previously")
pct <- round(slices/sum(slices)*100)
lbls <- paste(lbls, pct)
lbls <- paste(lbls, "%",sep="")
pie3D(slices,labels=lbls,explode=0.1,col=c("turquoise","magenta","salmon"),cex.sub=0.5,
    main="IV Drug Use History ")</pre>
```

IV Drug Use History



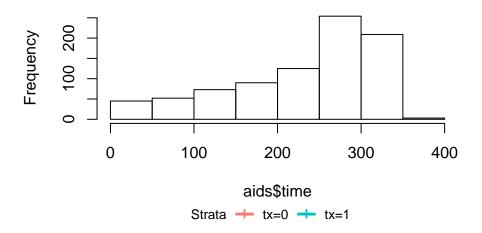
From this chart we see that most of the participants (84%) have never used IV drugs, whereas 16% of participants have some type of history of usage and none of the participants reported to be currently using the drugs.

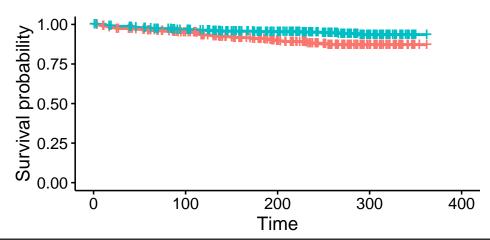
```
hist(aids$time)

###Data Plots

fit <- survfit(Surv(time,censor)~tx, data = aids)
ggsurvplot(fit,data = aids,conf.int = FALSE)</pre>
```

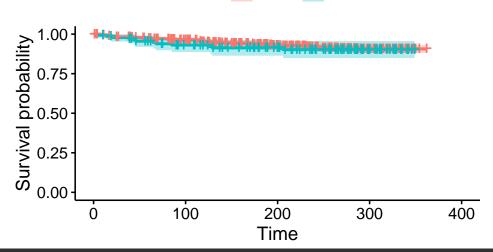
Histogram of aids\$time





aids_fit_time <- survfit(Surv(time, censor) ~ sex, data=aids)
ggsurvplot(aids_fit_time, data=aids, conf.int = TRUE)</pre>

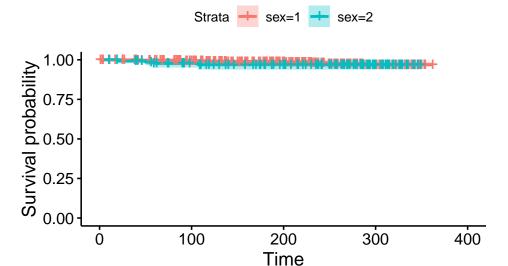
Strata



sex=1

sex=2

aids_fit_time.d <- survfit(Surv(time_d, censor_d) ~ sex, data=aids)
ggsurvplot(aids_fit_time.d, data=aids, conf.int = TRUE)</pre>



Survival Analysis

```
aids <- read.csv( "http://pages.pomona.edu/~jsh04747/courses/math150/AIDSdata.csv")
aids <- aids %>%
  mutate(age = ifelse(age <= 20, "under20",</pre>
                             ifelse(age <=30, "20-30",
                                    ifelse(age <= 40, "30-40",
                                           ifelse(age <=50, "40-50",
                                                ifelse(age <=60, "50-60",
                                                       mutate(age = factor(age,
                       levels = c("under20", "20-30", "30-40", "40-50", "50-60", "60-70", "over70")),
library(survival)
library (survminer)
library(ggplot2)
library(broom)
coxph(Surv(time,censor) ~ txgrp + sex + ivdrug + hemophil + karnof, data=aids) %>% tidy()
## # A tibble: 5 x 7
##
              estimate std.error statistic
                                                p.value conf.low conf.high
     term
##
     <chr>>
                 <dbl>
                          <dbl>
                                    <dbl>
                                                  <dbl>
                                                           <dbl>
                                                                     <dbl>
               -0.820
                          0.256
                                   -3.20 0.00138
                                                          -1.32
                                                                   -0.317
## 1 txgrp
## 2 sexmale
               0.325
                          0.319
                                    1.02 0.309
                                                          -0.301
                                                                    0.951
               -0.279
                                                          -0.637
                                                                    0.0786
## 3 ivdrug
                          0.183
                                    -1.53 0.126
## 4 hemophil
                0.340
                          0.593
                                    0.573 0.567
                                                          -0.823
                                                                    1.50
               -0.0854
## 5 karnof
                         0.0141
                                   -6.07 0.0000000131
                                                          -0.113
                                                                   -0.0578
full.ph <- coxph(Surv(time,censor) ~ txgrp + sex + ivdrug + hemophil + karnof, data=aids)
full.cox <-cox.zph(full.ph)</pre>
full.cox
##
                rho chisq
## txgrp
            -0.0840 0.4850 0.486
## sexmale -0.1728 2.1219 0.145
```

Global Schoenfeld Pest p: 0.6762 Schoenfeld Individ 13 2559100201721250 Time Schoenfeld Individ 26 13 2559100201721250 Time Schoenfeld Individ 26 13 2559100201721250 Time Schoenfeld Individ 27 13 2559100201721250 Time Schoenfeld Individ Time Schoenfeld Individ Time Schoenfeld Individ Time Time

coxph(Surv(time,censor) ~ txgrp + sex + ivdrug + karnof, data=aids) %>% tidy()

```
## # A tibble: 4 x 7
##
            estimate std.error statistic
                                               p.value conf.low conf.high
    term
##
    <chr>>
               <dbl>
                        <dbl>
                                  <dbl>
                                                 <dbl>
                                                         <dbl>
                                                                   <dbl>
             -0.824
## 1 txgrp
                        0.256
                                  -3.22 0.00129
                                                        -1.33
                                                                 -0.322
## 2 sexmale 0.317
                        0.319
                                  0.993 0.321
                                                        -0.309
                                                                  0.942
             -0.282
                        0.182
                                                        -0.640
                                                                  0.0752
## 3 ivdrug
                                  -1.55 0.122
             -0.0851
                        0.0140
## 4 karnof
                                  -6.06 0.0000000138
                                                         -0.113
                                                                 -0.0576
```

```
full.ph2 <- coxph(Surv(time,censor) ~ txgrp + sex + ivdrug + karnof, data=aids)
full.cox2 <-cox.zph(full.ph2)
full.cox2</pre>
```

```
## txgrp -0.0861 0.5129 0.474

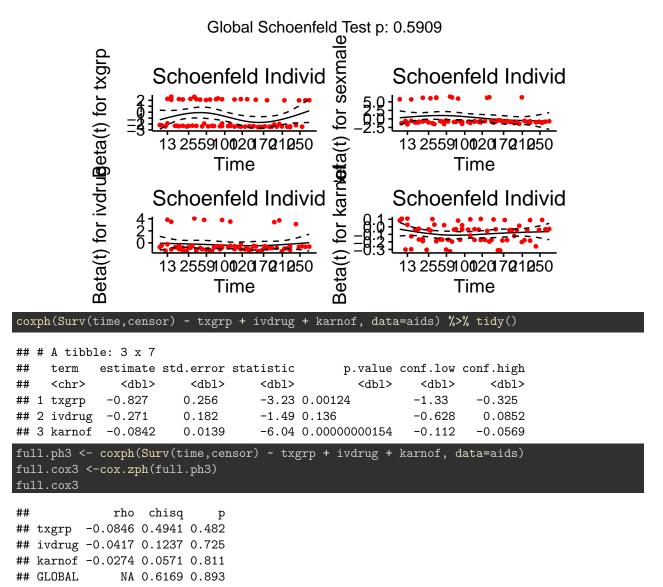
## sexmale -0.1749 2.1825 0.140

## ivdrug -0.0323 0.0755 0.784

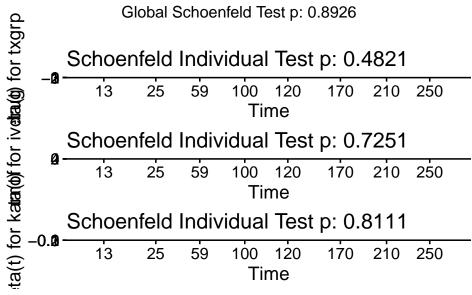
## karnof -0.0146 0.0167 0.897

## GLOBAL NA 2.8055 0.591
```

ggcoxzph(full.cox2)

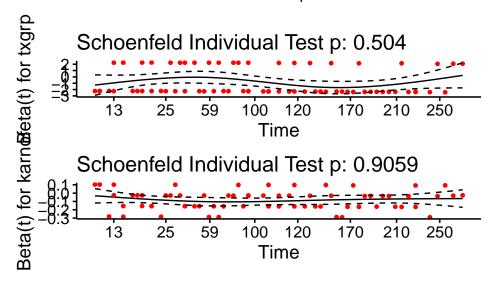


ggcoxzph(full.cox3)



coxph(Surv(time,censor) ~ txgrp + karnof, data=aids) %>% tidy() ## # A tibble: 2 x 7 ## term estimate std.error statistic p.value conf.low conf.high ## <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> -1.30 ## 1 txgrp -0.7970.255 -3.12 0.00181 -0.296 ## 2 karnof -0.0805 0.0137 -5.89 0.0000000396 -0.0537 -0.107 full.ph4 <- coxph(Surv(time,censor) ~ txgrp + karnof, data=aids)</pre> full.cox4 <-cox.zph(full.ph4)</pre> full.cox4 ## rho chisq ## txgrp -0.0804 0.447 0.504 ## karnof -0.0139 0.014 0.906 ## GLOBAL NA 0.461 0.794 ggcoxzph(full.cox4)

Global Schoenfeld Test p: 0.7941



```
anova(full.ph ,full.ph2)
## Analysis of Deviance Table
## Cox model: response is Surv(time, censor)
## Model 1: ~ txgrp + sex + ivdrug + hemophil + karnof
## Model 2: ~ txgrp + sex + ivdrug + karnof
##
      loglik Chisq Df P(>|Chi|)
## 1 -429.87
## 2 -430.02 0.2969 1
                          0.5858
anova(full.ph2,full.ph3)
## Analysis of Deviance Table
## Cox model: response is Surv(time, censor)
## Model 1: ~ txgrp + sex + ivdrug + karnof
## Model 2: ~ txgrp + ivdrug + karnof
##
      loglik Chisq Df P(>|Chi|)
## 1 -430.02
## 2 -430.48 0.9208 1
                          0.3373
anova(full.ph3,full.ph4)
## Analysis of Deviance Table
## Cox model: response is Surv(time, censor)
## Model 1: ~ txgrp + ivdrug + karnof
## Model 2: ~ txgrp + karnof
##
      loglik Chisq Df P(>|Chi|)
## 1 -430.48
## 2 -431.74 2.5191 1
                          0.1125
coxph(Surv(time,censor) ~ sex, data=aids) %>% tidy()
## # A tibble: 1 x 7
##
             estimate std.error statistic p.value conf.low conf.high
     term
                                     <dbl>
                                             <dbl>
                                                      <dbl>
     <chr>>
                <dbl>
                          <dbl>
                                                                <dbl>
                                    0.625
                                             0.532
                                                     -0.424
                0.199
                          0.318
                                                                0.821
## 1 sexmale
coxph(Surv(time,censor) ~ age+ txgrp+ karnof, data=aids) %>% tidy()
## # A tibble: 8 x 7
##
     term
               estimate std.error statistic
                                                   p.value conf.low conf.high
##
     <chr>>
                 <dbl>
                            <dbl>
                                      <dbl>
                                                     <dbl>
                                                              <dbl>
                                                                        <dbl>
## 1 age20-30
               -0.438
                           1.07
                                   -0.409
                                            0.682
                                                             -2.53
                                                                       1.66
## 2 age30-40
               -0.442
                           1.02
                                   -0.434
                                           0.665
                                                             -2.44
                                                                       1.55
## 3 age40-50
                -0.361
                           1.03
                                   -0.352
                                            0.725
                                                             -2.37
                                                                       1.65
## 4 age50-60
                           1.04
                                                                       2.50
                0.460
                                    0.442
                                            0.659
                                                             -1.58
                -0.780
                                                             -3.55
## 5 age60-70
                           1.42
                                   -0.551
                                            0.582
                                                                       2.00
## 6 ageover70 -14.1
                        2688.
                                   -0.00525 0.996
                                                           -Inf
                                                                     Inf
                -0.844
                           0.257
                                   -3.28
                                            0.00103
                                                                      -0.340
## 7 txgrp
                                                             -1.35
                                                                      -0.0543
## 8 karnof
                -0.0814
                           0.0138 -5.89
                                             0.0000000385
                                                             -0.109
cox.zph(coxph(Surv(time,censor) ~ age + txgrp+karnof, data=aids))
##
                         chisq
                  rho
## age20-30
              0.09054 5.70e-01 0.450
```

age30-40

age40-50

0.19294 2.53e+00 0.112

0.14871 1.50e+00 0.220

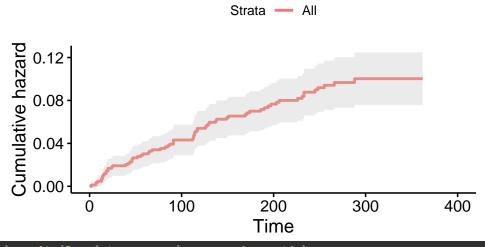
coxph(Surv(time,censor) ~ age *txgrp*karnof, data=aids) %>% tidy()

```
## # A tibble: 27 x 7
##
      term
                      estimate std.error statistic p.value conf.low conf.high
                                                                            <dbl>
##
      <chr>
                         <dbl>
                                    <dbl>
                                               <dbl>
                                                        <dbl>
                                                                 <dbl>
##
    1 age20-30
                        307.
                                 138277.
                                          0.00222
                                                        0.998
                                                                  -Inf
                                                                              Inf
##
    2 age30-40
                                 138277. 0.00231
                                                        0.998
                                                                  -Inf
                                                                              Inf
                        319.
##
    3 age40-50
                        327.
                                 138277.
                                          0.00237
                                                        0.998
                                                                  -Inf
                                                                              Inf
                                                                              Inf
##
    4 age50-60
                        343.
                                 138277.
                                          0.00248
                                                        0.998
                                                                  -Inf
    5 age60-70
                        287.
                                 176491.
                                          0.00163
                                                        0.999
                                                                  -Inf
                                                                              Inf
##
    6 ageover70
                         -1.66
                                  29414. -0.0000565
                                                        1.000
                                                                  -Inf
                                                                              Inf
                                  92392. 0.00163
                                                                  -Inf
                                                                              Inf
    7 txgrp
                        150.
                                                        0.999
##
                                                                  -Inf
    8 karnof
                          3.36
                                   1424. 0.00236
                                                        0.998
                                                                              Inf
    9 age20-30:txgrp -144.
                                  92392. -0.00156
                                                        0.999
                                                                  -Inf
                                                                              Inf
                                   92392. -0.00158
## 10 age30-40:txgrp -146.
                                                        0.999
                                                                  -Inf
                                                                              Inf
## # ... with 17 more rows
```

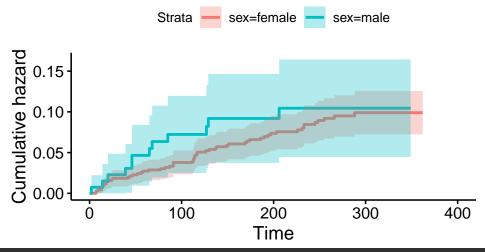
cox.zph(coxph(Surv(time,censor) ~ age *txgrp*karnof, data=aids))

```
rho
                                      chisq
## age20-30
                           -0.1008 4.31e-08 1.000
## age30-40
                           -0.1583 3.15e-08 1.000
                          -0.0965 1.25e-08 1.000
## age40-50
## age50-60
                          -0.2071 6.53e-08 1.000
## age60-70
                          -0.2062 3.04e-08 1.000
## ageover70
                          -0.2493 7.81e-11 1.000
                          -0.2032 2.68e-08 1.000
## txgrp
## karnof
                           -0.1974 5.24e-08 1.000
## age20-30:txgrp
                           0.0921 2.14e-08 1.000
## age30-40:txgrp
                           0.1142 1.08e-08 1.000
                           0.0826 5.64e-09 1.000
## age40-50:txgrp
## age50-60:txgrp
                           0.1851 3.47e-08 1.000
## age60-70:txgrp
                           0.2102 2.15e-08 1.000
## ageover70:txgrp
                           0.1967 3.96e-11 1.000
## age20-30:karnof
                           0.0984 4.53e-08 1.000
                           0.1524 3.44e-08 1.000
## age30-40:karnof
## age40-50:karnof
                           0.0938 1.40e-08 1.000
## age50-60:karnof
                           0.2053 7.78e-08 1.000
## age60-70:karnof
                           0.1978 3.00e-08 1.000
## ageover70:karnof
                                              NaN
                                NΑ
                                        NaN
                           0.1996 2.81e-08 1.000
## txgrp:karnof
                          -0.0910 2.15e-08 1.000
## age20-30:txgrp:karnof
## age30-40:txgrp:karnof
                          -0.1020 9.71e-09 1.000
                          -0.0823 6.23e-09 1.000
## age40-50:txgrp:karnof
## age50-60:txgrp:karnof
                          -0.1796 3.72e-08 1.000
                          -0.1981 1.98e-08 1.000
## age60-70:txgrp:karnof
## ageover70:txgrp:karnof
                               NA
                                        NaN
                                              NaN
## GLOBAL
                                NA 1.84e+01 0.891
```

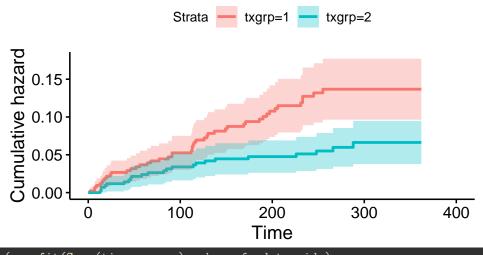
Estimated Hazard rates



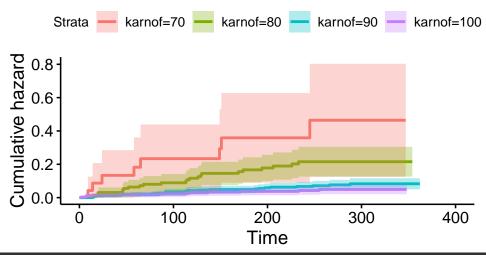
Estimated Hazard rates based on sex

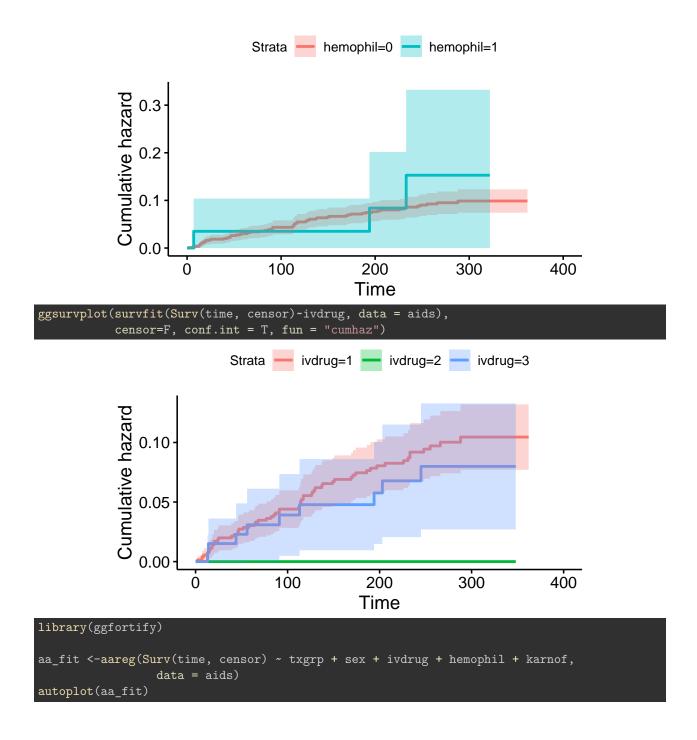


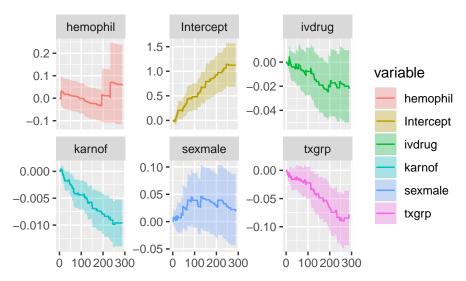
Estimated Hazard rates based on treatment



Estimated Hazard rates based on klarnfsky







The Aalen model assumes that the cumulative hazard H(t) for a subject can be expressed as a(t) + X B(t), where a(t) is a time-dependent intercept term, X is the vector of covariates for the subject possibly time-dependent, and B(t) is a time-dependent matrix of coefficients.

The plots show how the effects of the covariates change over time.

Patricia's "Something New"

I will be doing a power analysis by simulating survival analysis curves

1. What is the topic?

The topic is using sim.survdata in R to simulate survival data. Using that simulated data, we will make that the alternative and control for the coefficient beta by setting it equal to some value. Then using power analysis, we will see how many times we reject H_0 .

2. How it is relevant? How it relates to survival analysis/analysis at hand?

Power analysis relates to survival analysis because if power is large after comparing our data to the simulated survival data, this tells us that there is a high chance that we would reject the null in favor of the alternative (control versus treatment?)

3. Resources to learn about the topic.

Below are some of the resources I have begun to use to learn about creating simulations of survival curves and performing power analysis:

a). https://cran.r-project.org/web/packages/coxed/vignettes/simulating_survival_data.html b). http://www.icssc.org/documents/advbiosgoa/tab%2026.00_survss.pdf

4. What will be challenging about learning something new?

Learning something new will be challenging because in this case, the concept of power analysis is something I just recently learned in Intro to Statistics. So learning to apply this concept in the context of survival

analysis curves will be a challenge for me to learn. Learning how to simulate survival curves will also be challenging because I will have to learn how to use and interpret new functions in R.

Juste's "Something New"

I will be analyzing the Shoenfeld residuals for the Cox PH model.

1. What is goign on? What is the topic? 2. How it is relevant? How it relates to survival analysis/analysis at hand?

Cox proportional hazards (PH) model is considered a great way to identify combined effects of several covariates on the relative risk (hazard). This model assumes that the hazards of the different strata formed by the levels of the covariates are proportional. This proportional hazards assumption is particularly important and can be tested via three different clases of tests. The first class is focused on the piecewise estimation of models for subsets of data defined by stratification of time. The second one considers the interactions between covariates and some function of time. Final, third one is based on examinations of regression residuals. The Schoenfeld Residuals are a part of the third class of proportional hazard assumption testing and I will be exploring it in order to be able to eradicate a method for testing for the PH assumption in the current and future data set analyses. This topic is particularly important in relation to survival analysis since it provides an idea of whether the model is appropriate for the data set at hand and whether some covariates should be considered as variants of time in order to supply the best model for prediction of proportional hazards.

3. Resources to learn about the topic.

I have been researching articles and scientific journals that provide insights into tthe Schoenfeld residuals and their use in the Cox PH model. Sources include:

- 1. https://onlinelibrary.wiley.com/doi/full/10.1111/ajps.12176
- $2. \ https://rstudio-pubs-static.s3.amazonaws.com/39354 \ \ 34153ff19e624116bd2fbdec7d2534aa.html$

4. What will be challenging about learning something new?

Taking a completely new model of analyzing survival data is particularly difficult since the mathematical derivations and notations are also very varied from what we have seen in class. Although, I do remember some of the ideas behind parametric functions, their applications to statistical models are much more challenging than I have expected. Therefore, it will require me a lot of time and extensive research to be able to understand and learn how to apply this model to our data and other instances of survival analysis.

Explanation of the Theory Behind Schoenfeld Residuals

Let $z_{ij}(t)$ be the j^{th} covariate of the i^{th} unit, where i = 1, 2, ..., n and j = 1, 2..., p

This notation indicates that z_{ij} is allowed to vary as a function of the time scale.

- 1) As we know from lecture, the Cox PH model assumes that h(t) of the i^{th} individual satisfies:
- $h_i(t) = h_0(t)e^{z_i(t)\beta}$ where:
- h_0 -> baseline hazard
- $z_i(t) \rightarrow 1 \times p$ vector of covariates for unit i each of which can be time fixed or time-varying.

2) However, another possibility has been presented by Therneau and Granbsh in 2000, where they proposed an idea that there civyld be an alternative to the current Cox model, where the coefficient of the estimate could also be varying as a function of time.

The new hazard function would look like this: $h_i(t) = h_0(t)e^{z_i(t)\beta(t)}$

Therefore, in order to examine thee two models in a case when $\beta = \beta(t)$ requires a residual analysis that could indicate whether a model should consider a covariate as a variable with time.

Due to the fact that that some observations might be censored and in particular, regarding the Cox PH model, the baseline hazard is not estimated, in oprder to analyse the residuals a particular score process. The risk score for unit i at time t is thought to be $r_i(t) = e^{z_i(t)\beta}$, where $Y_i(t)$ is the indicator function and $Y_i(t) = 1$ indicates a point in which i is under risk and thus observation and it is equal to 0 in other occasions.

The Schoenfeld residuals are given by the equations:

1.
$$s_k = Z_{(k)} - \frac{\sum_i Y_i(t_k) r_i(t_k) Z_i(t_k)}{\sum_i Y_i(t_k) r_i(t_k)}$$

2. $s_k = Z_{(k)} - \bar{z}(\hat{\beta}, t_k)$

In this case, the Z(k) is the covariate vector of the particular unit that is experiencing the evnt at time k; $\hat{\beta}$ is the estimate of β and $\bar{z}(\hat{\beta}, t_k)$ is the wighted mean of covariate values.

Furthermore, the weighted variance can be represented by the derived equation at the k^{th} time as

$$V(\beta, t_k) = \sum_{i} Y_i(t_k) r_i(t_k) Z_i(t_k) - \bar{z}(\hat{\beta}, t_k)' Z_i(t_k) - \frac{\bar{z}(\hat{\beta}, t_k)}{\sum_{i} Y_i(t_k) r_i(t_k)}$$

From this, we can scale the Schoenfeld residuals by $V(\beta, t_k)$ of X at t_k via the equation:

$$s_k^* = V^{-1}(\hat{\beta}, t_k) s_k$$

The scaled Schoenfeld residuals can also be defined as follows:

$$s_k^* = m \sum_{k=1}^d V(\hat{\beta}, t_k) s_k$$

here, m is the total number of deaths in the data set.

Following the calculations, the residuals are plotted against time in order to test the prportional hazards assumption. If the assumption is correct, the residuals should be fiting around the line centered at zero (y=0). The further away this predicted line is form the horizontal of (y=0) the more likely one is to call the PH assumption to question and determine whether it is met through the model.

To go a little deeper into the analysis of the resiaul calculation, one can look at the calculations of the test statistic for this residual mdoel.

By producing a least squares slope of regression and assuming a relationship between s_{kj}^* and t_{kj} or some function $g(t_k)$ allows to derive a test statistic for the proportional hazards assumption in regards to the j^{th} covariate, which is given by:

$$T_j = \frac{\left[\sum_{k=1}^{d} (g(t_k) - \hat{g}) s_{kj}^8\right]^2}{dI^{jj} \sum_{k=1}^{d} (g(t_k) - \hat{g})^2}$$

Here, the distribution is asymptotical as $X^{2}(1)$ stating the null hypothesis that the relationship between the covariate, in this case j and the evnt time follows the assumption of PH.

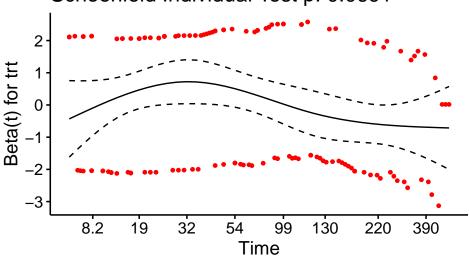
Schoenfeld:

```
veteran.ph <- coxph(Surv(time,status) ~ trt, data=veteran)
cox.veteran <- cox.zph(veteran.ph)
cox.veteran</pre>
```

rho chisq p ## trt -0.16 3.3 0.0691

ggcoxzph(cox.veteran)

Schoenfeld Individual Test p: 0.0691



ggcoxdiagnostics(veteran.ph, type="schoenfeld")

