



An item response theory framework to evaluate automatic speech recognition systems against speech difficulty

Literature Review 2026.01.08
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Intro

- **Title**: An IRT framework to evaluate automatic speech recognition systems against speech difficulty
- **Journal(Year)** : Computer Speech and Language 95 (2026)
- **Background** : results of ASR systems are usually assessed by aggregating □ varieties are ignored
- **Key Words**
 - Application of existing IRT theories to ASR
 - Plots (to show correlations between: sentence difficulties, system performance, speaker quality)

ELSEVIER

Table of Contents

- 1. About ASR Evaluation
- 2. Suggested Solution
- 3. IRT (Item Response Theory) in AI evaluation
- 4. IRT evaluation in ASR
- 5. RCC (Recognizer Characteristic Curves)
- 6. ASR Fingerprint
- 7. Discussion

1. About ASR Evaluation

Importance

- particular application □ which technique?
- to know advantages & limitations of existing techniques

Relying Aspects

- Dataset
- Accessing the quality of transcriptions

Limitation of existing method

- usually assessed by aggregating the results
- the variety of difficulties are ignored

how can we
overcome this
limitation?



2. Suggested Solution



IRT (Item Response Theory)

theory that evaluates

- ability of ASR systems
- difficulty of test speeches

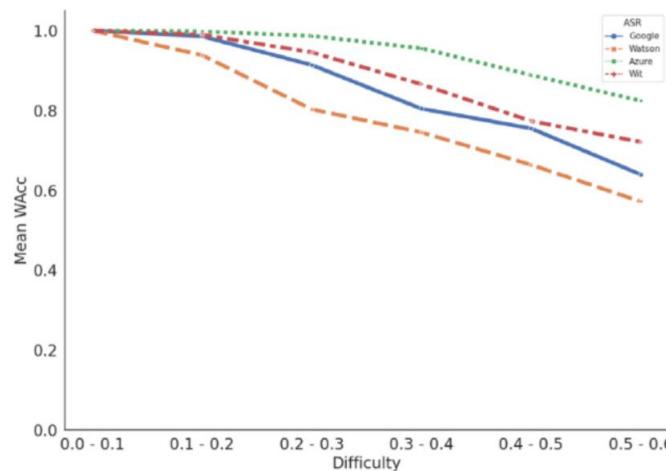
$$E[r_{jki} | \theta_i, \delta_{jk}] = \frac{\gamma_{jki}}{\gamma_{jki} + \omega_{jki}} = \frac{1}{1 + \left(\frac{\delta_{jk}}{1 - \delta_{jk}} \right) \left(\frac{\theta_i}{1 - \theta_i} \right)^{-1}}$$

$$E[\delta_{jk} | \varphi_k, w_j, a_j] = \frac{\alpha_{jk}}{\alpha_{jk} + \beta_{jk}} = \frac{1}{1 + \left(\frac{\varphi_k}{1 - \varphi_k} \right)^{a_j} \left(\frac{w_j}{1 - w_j} \right)^{-a_j}},$$

RCC (Recognizer Characteristic Curve)

plot

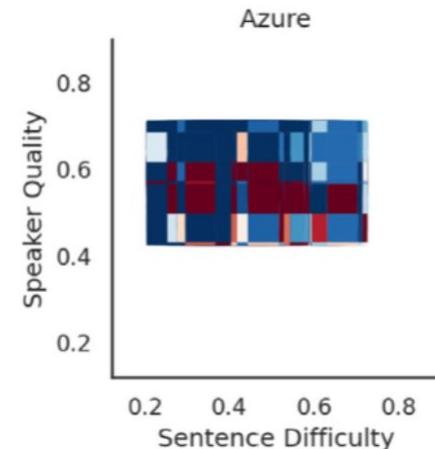
x axis: speech difficulty
y axis: ASR performance



ASR Fingerprint

plot

x axis: sentence difficulty
y axis: speaker quality
color: ASR performance



3. IRT (Item Response Theory) in AI Evaluation

3.1 Definition

- A paradigm developed in Psychometrics
- usually proposed to model the probability of binary responses
- **Respondent's Ability** : Estimates the ability of each AI system
(능력)
- **Item Difficulty** : Estimates the difficulty of each test task
 - Difficulty (난이도)
 - Discrimination (변별력)
 - Guessing (추측도)

– respondent's ability
– item's difficulties

3. IRT (Item Response Theory) in AI Evaluation

3.2 Formal Definition

“특정 테스트 항목 i 에 대한 응답자 j 의 응답은 확률 변수로 모델링되며, 이의 기댓값은 응답자 매개변수 벡터 Θ_j 와 항목 매개변수 벡터 Δ_i 모두에 의존한다. 매개변수 값은 원칙적으로 알려지지 않지만, 테스트에서 관찰된 응답 모음으로부터 추정될 수 있다.”



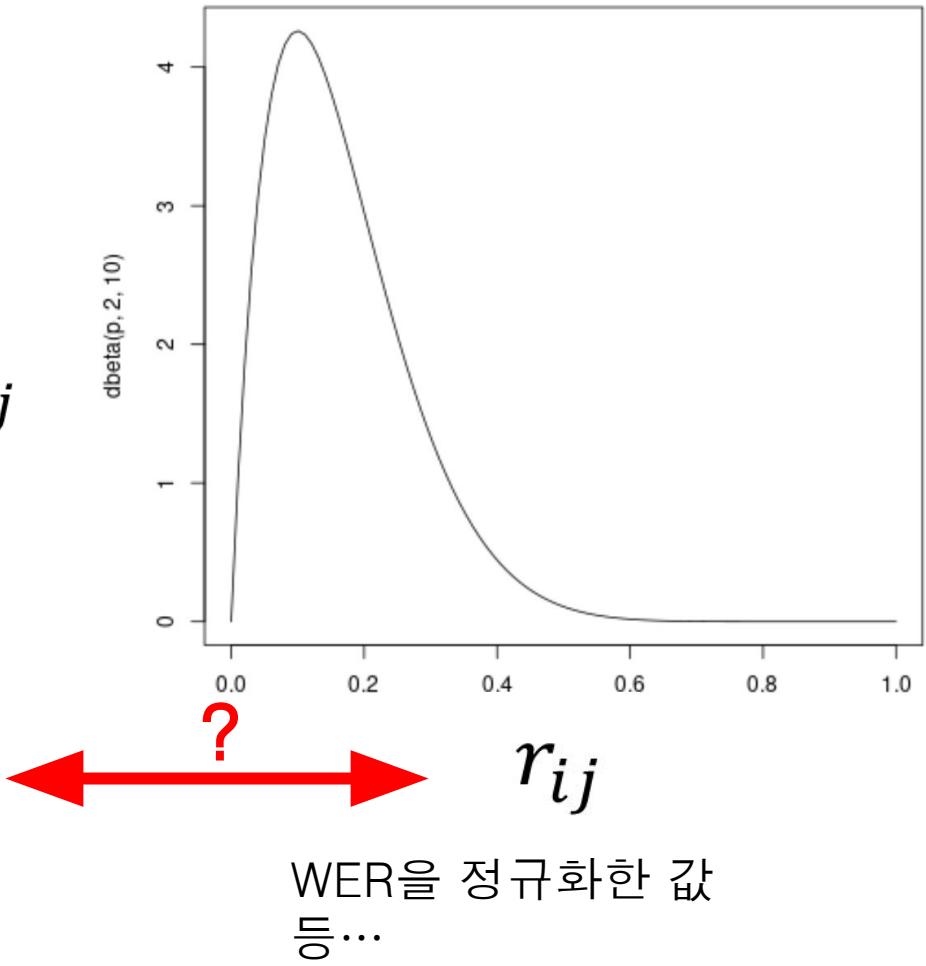
응시자(j)가 테스트(i)를 통과할지 말지는
1. 응시자의 능력 (θ_j)과
2. 항목의 난이도 (Δ_i)에
의존한다.
 θ, Δ 은 테스트 결과로 추정 가능하다

3. IRT (Item Response Theory) in AI Evaluation

3.3 IRT Model β^3

- Chen et al., 2019
- The model used in this paper
- for bounded, continuous responses r_{ij}
(음성 데이터)
- Responses' probability follows beta distribution

- respondent's ability
- item's difficulties

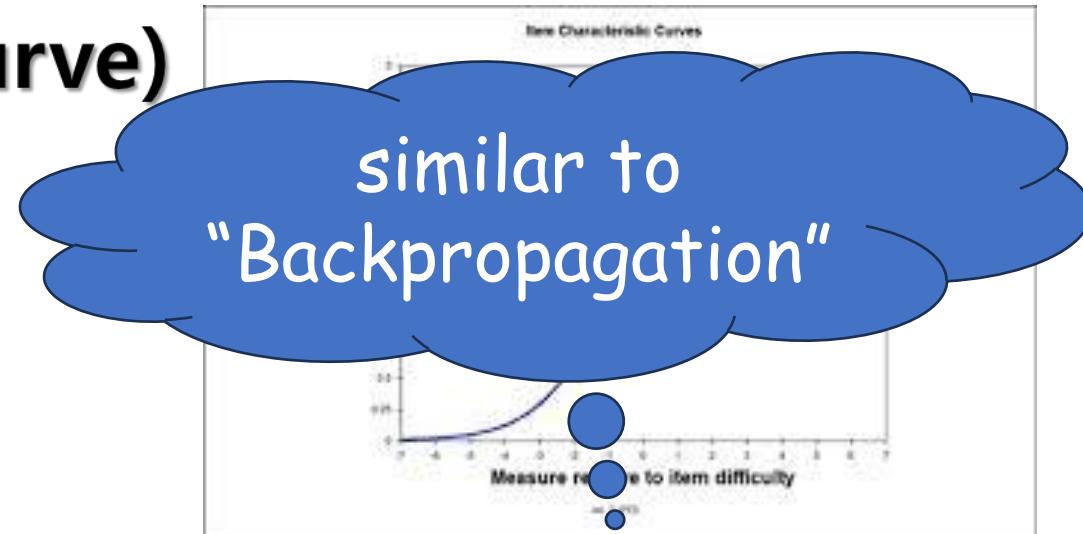


3. IRT (Item Response Theory) in AI Evaluation

3.4 ICC (Item Characteristic Curve)

- r_{ij} is calculated according to...

$$E[r_{ij} | \theta_j, \delta_i, a_i] = \frac{1}{1 + \left(\frac{\delta_i}{1-\delta_i} \right)^{a_i} \left(\frac{\theta_j}{1-\theta_j} \right)^{-a_i}}$$



- $r_{ij} \in [0, 1]$ is the response of respondent j to item i ;
- θ_j is the ability of the respondent j ;
- δ_i is the difficulty of the item i ;
- a_i is the discrimination of the item i .



3. IRT (Item Response Theory) in AI Evaluation

3.4 ICC (Item Characteristic Curve)

- *parameter θ, δ* inference:

초기

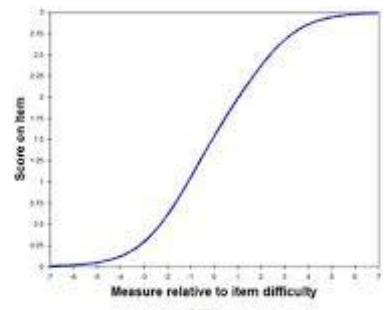
- ability parameter
- item's parameter

r_{ij}

via MLE,
...

업데이트

- ability parameter
- item's parameter



마침
내

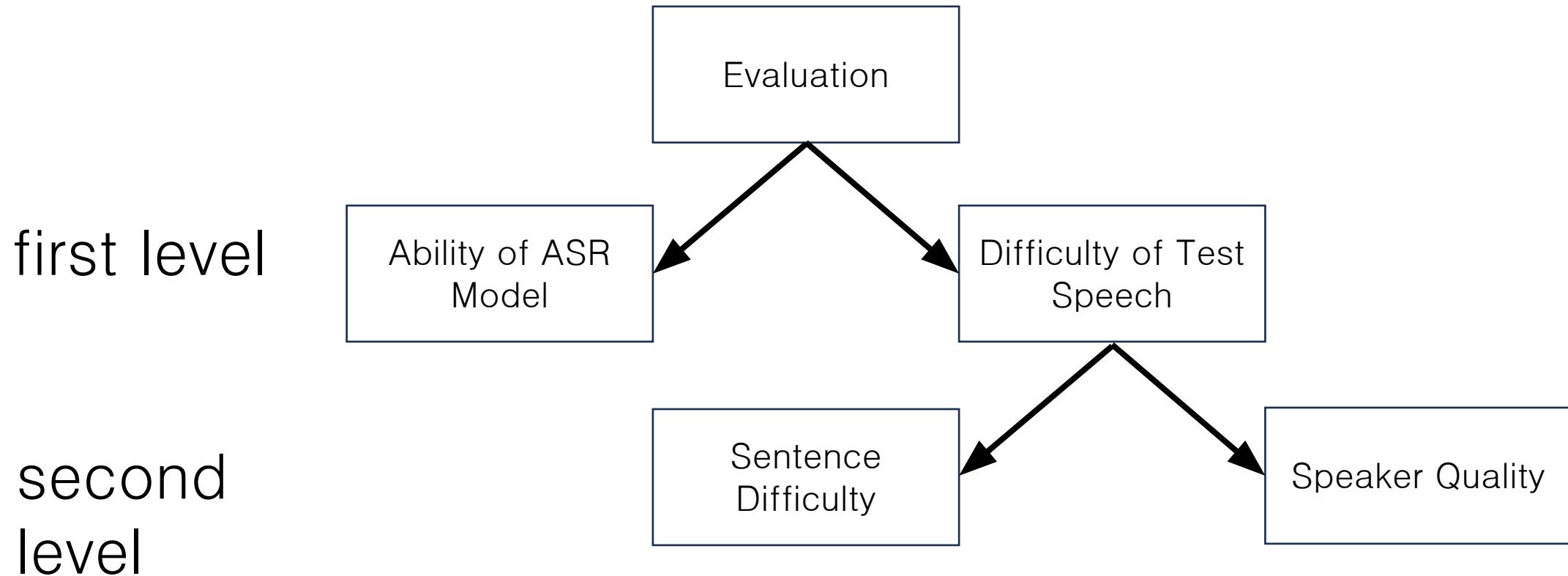
- respondent's ability
- item's difficulties

3. IRT (Item Response Theory) in AI Evaluation

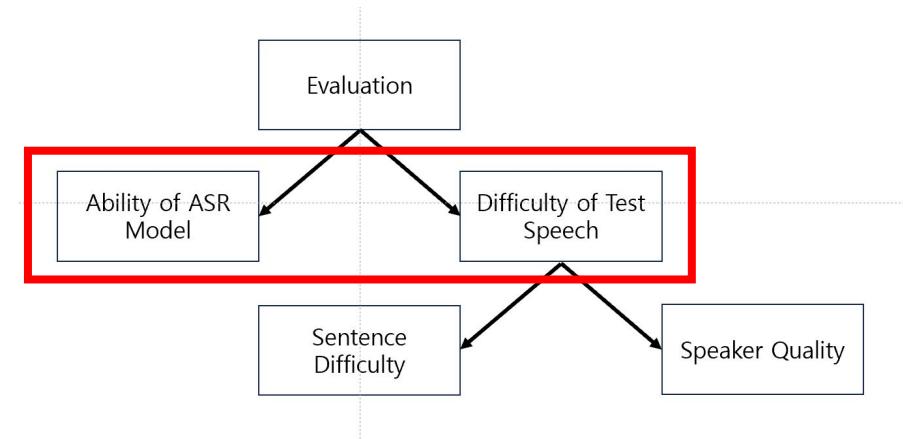
3.5 IRT in AI Domain

- Depending to AI Domain:
 - pool of respondents
 - pool of items
 - measuring method
- General Roadmap:
 - 1. choose pool of systems
 - 2. choose a benchmark of set of tasks
 - 3. evaluate the performance
 - 4. fit an appropriate IRT model (depends on domain of response)

4. IRT evaluation in ASR



4. IRT evaluation in ASR



4.1 First Level IRT

- Objective: Ability of ASR Model, Difficulty of Test Speech

$$r_{jki} \sim \text{Beta}(\gamma_{jki}, \omega_{jki}),$$

$$\gamma_{jki} = \left(\frac{\theta_i}{\delta_{jk}} \right),$$

$$\omega_{jki} = \left(\frac{1 - \theta_i}{1 - \delta_{jk}} \right),$$

$$\theta_i \sim \text{Beta}(1, 1), \delta_{ik} \sim \text{Beta}(1, 1).$$

$$E[r_{jki} | \theta_i, \delta_{jk}] = \frac{\gamma_{jki}}{\gamma_{jki} + \omega_{jki}} = \frac{1}{1 + \left(\frac{\delta_{jk}}{1 - \delta_{jk}} \right) \left(\frac{\theta_i}{1 - \theta_i} \right)^{-1}}.$$

r_{jki} Response

γ_{jki} Beta Parameter

ω_{jki} Beta Parameter

θ_i Ability of System

δ_{jk} Difficulty of Speech

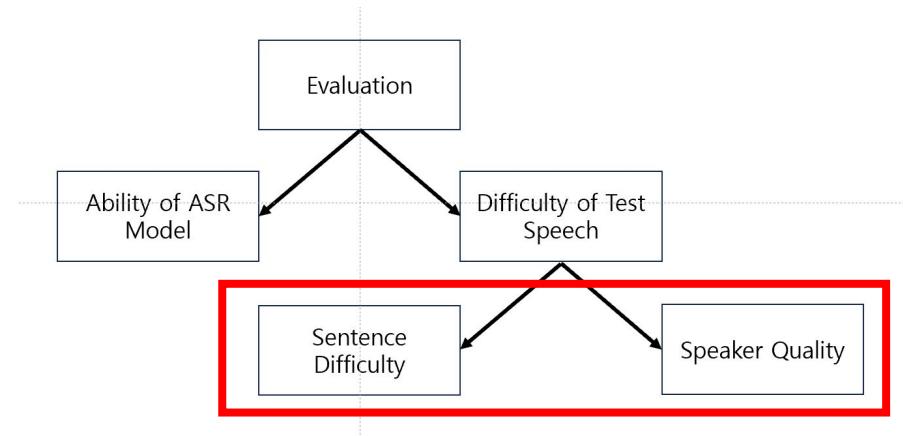
High (better) responses are expected
systems, easier speeches.

high-ability

Low (worse) responses are expected
systems, difficult speeches.

low-ability

4. IRT evaluation in ASR



4.2 Second Level IRT

- Objective: Sentence Difficulty, Speaker Quality

$$\begin{aligned}\delta_{jk} &\sim B(\alpha_{jk}, \beta_{jk}), \\ \alpha_{jk} &= \left(\frac{\varphi_k}{w_j} \right)^{a_j}, \\ \beta_{jk} &= \left(\frac{1 - \varphi_k}{1 - w_j} \right)^{a_j}, \\ \varphi_k &\sim B(1, 1), w_j \sim B(1, 1), a_j \sim \mathcal{N}(1, \sigma_0^2).\end{aligned}$$

δ_{jk}	Difficulty of Speech
α_{jk}	Beta Parameter
β_{jk}	Beta Parameter
φ_k	Speaker's Quality
w_j	Sentence Difficulty
a_j	Sentence Discrimination

$$E[\delta_{jk} | \varphi_k, w_j, a_j] = \frac{\alpha_{jk}}{\alpha_{jk} + \beta_{jk}} = \frac{1}{1 + \left(\frac{\varphi_k}{1 - \varphi_k} \right)^{a_j} \left(\frac{w_j}{1 - w_j} \right)^{-a_j}},$$

4. IRT evaluation in ASR

4.3 Benchmarks

- Speaker: audio speeches were produced by adopting 4 TTS tools.
- Noise level: three levels of white noise was injected
- Total 7,500 speeches: (25 speakers) x (100 sentences) * (3 noise levels)

$$WAcc = 1 - \frac{S + D + I}{N}$$

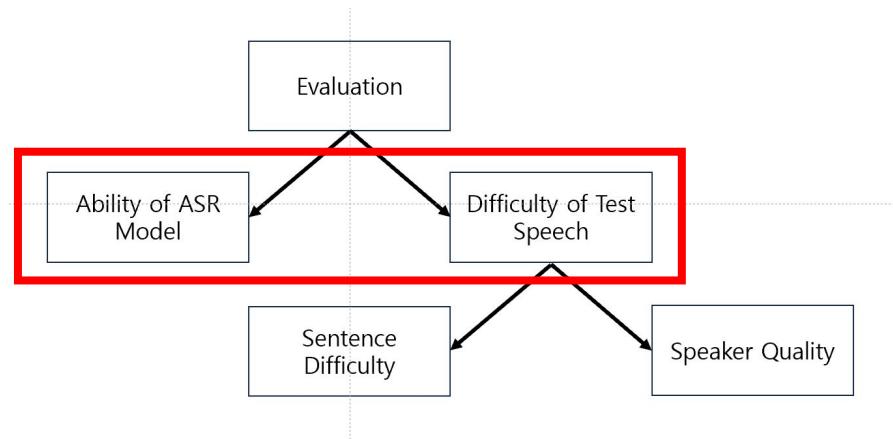
in which:

- S is the number of substitutions;
- D is the number of deletions;
- I is the number of insertions;
- N is the number of words in the original sentence.

4.4 IRT fitting

- Matrix for IRT model
- responses were defined as:

5. RCC



- Objective: Speech Difficulty \square ASR system's performance

$$R(\pi) = \int_{\delta} p(\delta) R(\pi|\delta) d\delta$$

$$R(\pi, D) = \sum_{\delta} \hat{p}(\delta) \hat{R}(\pi, D|\delta)$$

$R(\pi)$ ASR system's performance

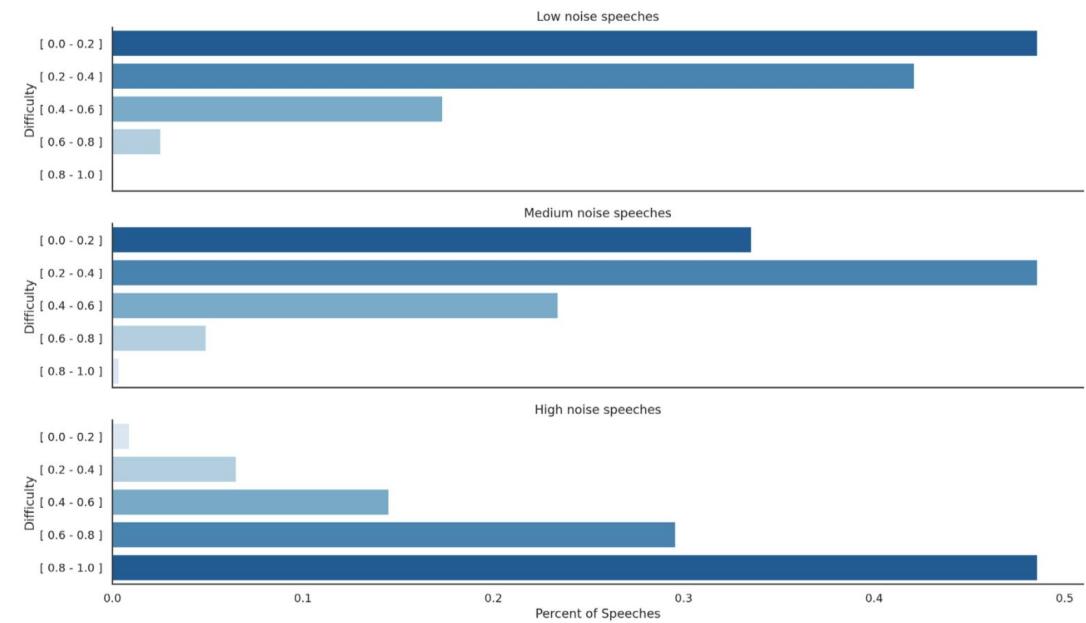
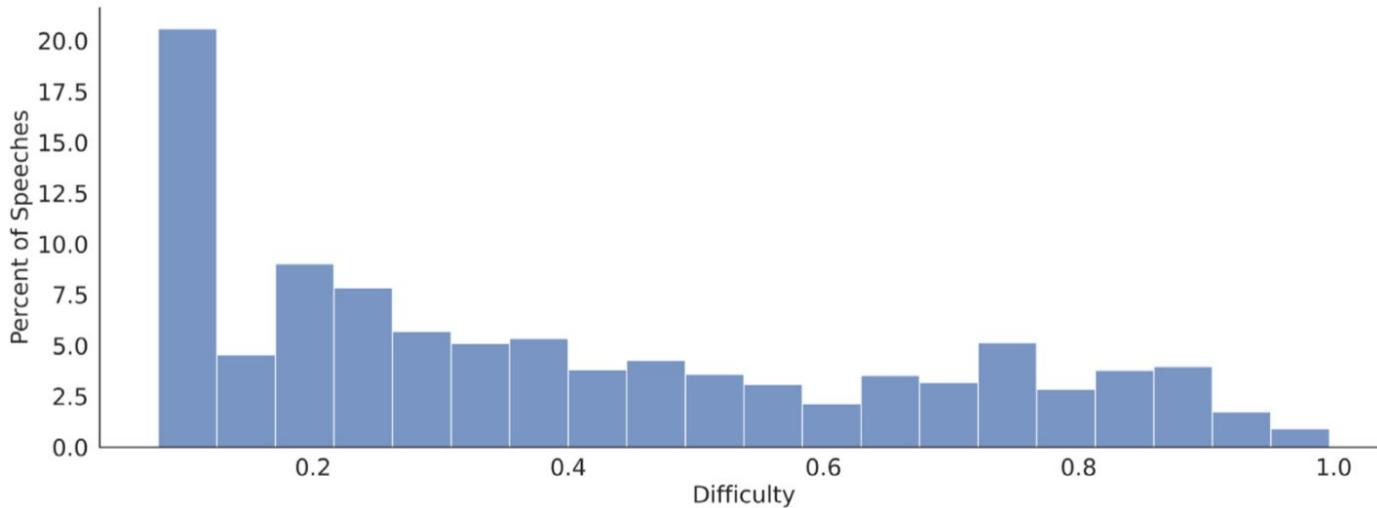
$p(\delta)$ Difficulty Distribution

$R(\pi, D)$ System's performance conditioned by benchmark data D's difficulty

$\hat{p}(\delta)$ Frequency of Speeches in D

$\hat{R}(\pi, D|\delta)$ system's performance averaged over the speeches with the same level of difficulty.

5. RCC



$R(\pi)$ ASR system's performance

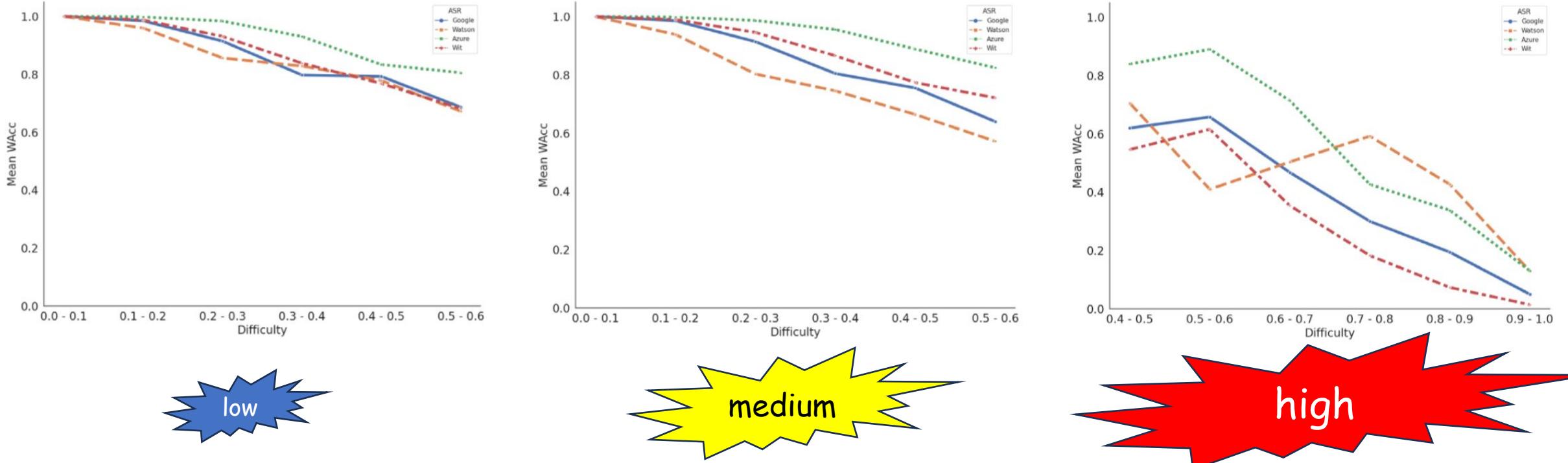
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5. RCC



$R(\pi)$ ASR system's performance

$p(\delta)$ Difficulty Distribution

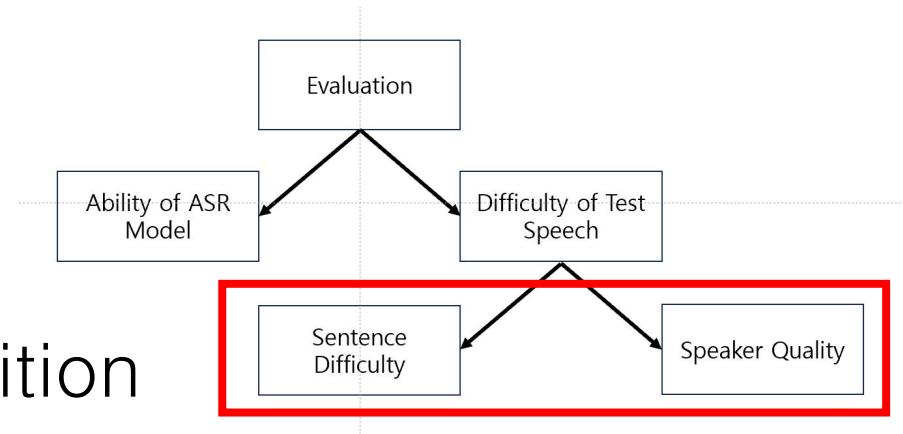
$R(\pi, D)$ System's performance conditioned by benchmark data D's difficulty

$\hat{p}(\delta)$ Frequency of Speeches in D

$\hat{R}(\pi, D|\delta)$ system's performance averaged over the speeches with the same level of difficulty.

6. ASR Fingerprint

- Objective: Speech Difficulty Decomposition



$$R(\pi|\delta) = \int_{\omega,\phi} p(\omega, \phi|\delta) R(\pi|\omega, \phi) d(\omega, \phi)$$



Decompositio
n

$$R(\pi) = \int_{\delta} \int_{\omega,\phi} p(\delta) p(\omega, \phi|\delta) R(\pi|\omega, \phi) d(\omega, \phi) d\delta$$



Empirically estimated
as...

$$R(\pi, D) = \sum_{\delta} \sum_{\omega,\phi} \hat{p}(\delta) \hat{p}(\omega, \phi|\delta) \hat{R}(\pi, D|\omega, \phi)$$

$R(\pi|\delta)$ Partial
Performance measure

δ_{jk} Difficulty of Speech

φ_k Speaker's Quality

ω_j Sentence Difficulty

6. ASR Fingerprint

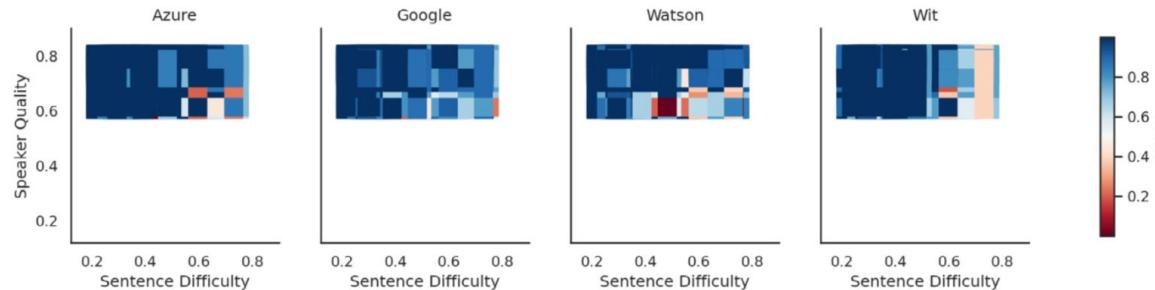
- for all noise level

δ_{jk} Difficulty of Speech
 φ_k Speaker's Quality
 ω_j Sentence Difficulty

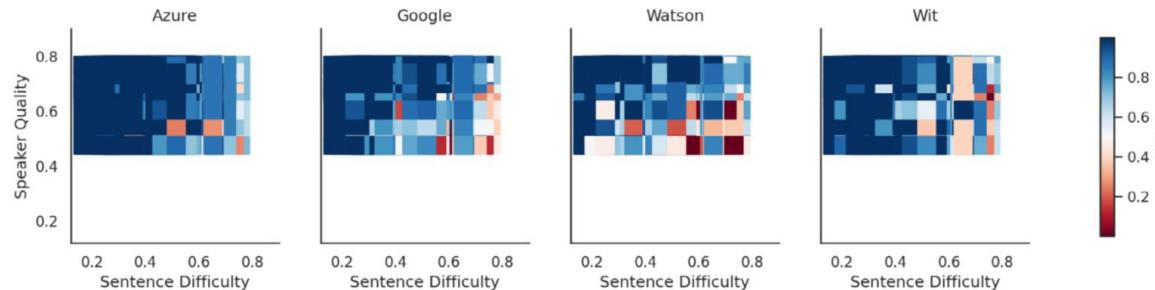


$$R(\pi, D) = \sum_{\delta} \sum_{\omega, \phi} \hat{p}(\delta) \hat{p}(\omega, \phi | \delta) \hat{R}(\pi, D | \omega, \phi)$$

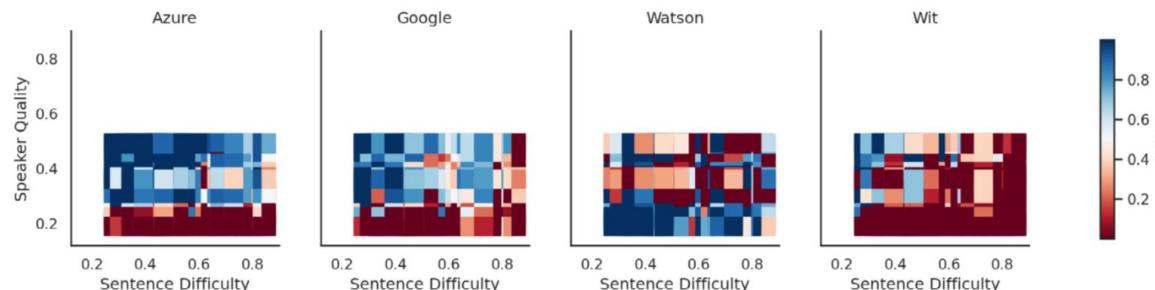
6. ASR Fingerprint



(a) Low noise level.



(b) Medium noise level.



(c) High noise level.

7. Discussion

- **Noise Injection**

- Contribution: RCCs revealed impact of each noise injection on each ASR system's performances (medium is best)
- Future work: richer noise types can be adopted

- **Human vs Synthetic test items**

- Contribution: synthetic test items can produce diverse test items (scalability and cover many types)
- Limitation: cannot express complex nuances of humans voices
- Future work: Synthetic speech and human–record speech can be compared in terms of difficulty

- **Speech variability and data representativeness**

- Contribution: many factors which makes speech diverse can be evaluated
- Future work: larger and representative test benchmarks



Thank you!

Q&A