

# Neural Population Geometry

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# Outline

Introduction

Preliminaries

Neural Population Geometry

Simulation

Conclusion

# Problem Description & Motivation

- ▶ Advances in recording techniques: thousands to millions of neurons simultaneously
- ▶ Challenges in studying large neural populations:
  - ▶ Neurons respond to multiple variables
  - ▶ Traditional tuning-based analyses have limitations
- ▶ Shift from single-neuron tuning to geometric approaches
- ▶ Neural computations arise from structured, high-dimensional activity patterns

# Neural Manifolds

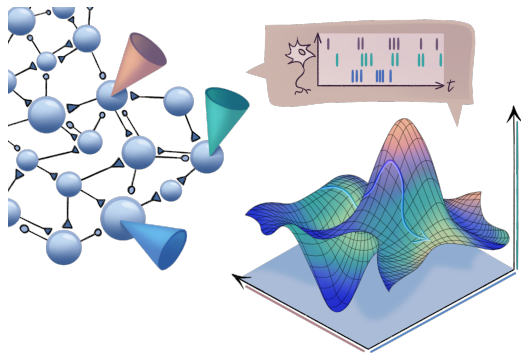
- ▶ Neural manifolds: low-dimensional geometric structures embedded in high-dimensional neural state space
- ▶ Key properties: dimensionality, curvature, and separability
- ▶ Provide insights into computational principles governing neural networks
- ▶ Framework has provided mechanistic insights into:
  - ▶ Perception
  - ▶ Decision-making
  - ▶ Motor control
  - ▶ Cognition

# Bridging Biological and Artificial Neural Networks

- ▶ Neural population geometry bridges biological and artificial neural networks
- ▶ Shared representational structures support efficient computation
- ▶ Geometric properties shape information encoding and processing
- ▶ Geometric perspective reveals how neural populations achieve:
  - ▶ Robustness
  - ▶ Efficiency
  - ▶ Scalability

# Neural State Space & Population Activity

- ▶ Neural state space: each axis represents a single neuron
- ▶ Repeated stimulus presentations create point clouds
- ▶ Neuronal variability induces fluctuations
- ▶ Manifolds emerge from stimulus responses



# Key Concepts in Neural Population Geometry

- ▶ Population-level representations vs. single-neuron tuning
- ▶ Geometric transformations of neural manifolds
- ▶ Dimensionality and information encoding
- ▶ Manifold separability and computational capabilities
- ▶ Curvature and computational constraints

# Artificial Neural Networks

- ▶ Demonstration of geometric structures in neural representations
- ▶ Simulation experiment: encoding circular variables
- ▶ Illustrates how topological structures naturally emerge

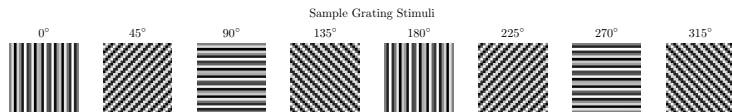


Figure: Sample grating stimuli at different orientations



# Circular Manifold Experiment

- ▶ CNN trained to predict orientation of visual grating stimuli
- ▶ Analogous to orientation selectivity in visual cortex
- ▶ Sinusoidal gratings at orientations from  $0^\circ$  to  $360^\circ$
- ▶ Architecture: convolutional layers + fully connected layers
- ▶ 32-dimensional latent space analyzed for geometric properties
- ▶ Trained to predict sine and cosine components (handles circular topology)

# Results: Circular Manifold

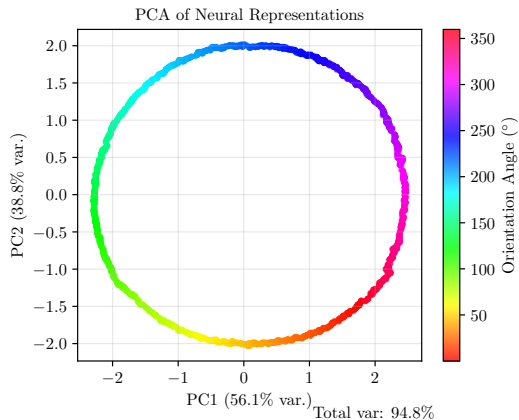


Figure: PCA of the latent space

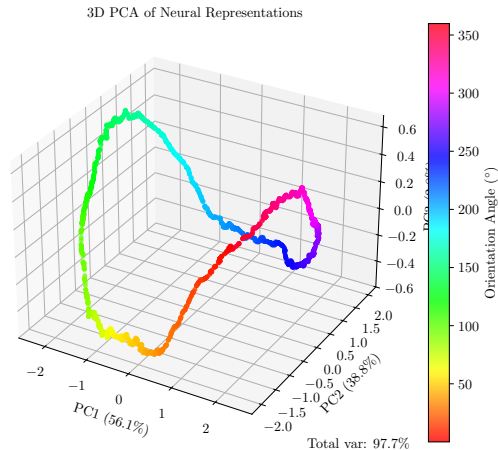


Figure: 3D visualization of the manifold

- Circular manifold emerged in latent space
- Similar orientations positioned close together

# Key Principles Demonstrated

- ▶ **Manifold structure:** Low-dimensional manifold (circle) embedded in high-dimensional space
- ▶ **Topological correspondence:** Manifold topology matches task space topology
- ▶ **Continuous representation:** Similar stimuli mapped to nearby points
- ▶ **Dimensionality reduction:** High-dimensional input compressed to essential variables

## Insight

Circular topology emerged naturally without explicit constraints—the network discovered this efficient representation on its own






# Biological Neural Networks

- ▶ Application of geometric principles to biological neural data
- ▶ Comparison with artificial neural network findings
- ▶ Insights into biological neural computation

# Conclusion

- ▶ Neural population geometry provides powerful framework for analyzing neural activity
- ▶ Geometric principles describe population-level representations
- ▶ Approach yields mechanistic insights across multiple domains
- ▶ Bridges biological and artificial neural networks
- ▶ Geometric perspective deepens understanding of neural computation

# References

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