



Hardware-Level Explanation of the Transpiled Bell Circuit (IBM Torino)

This document summarizes, in detailed but structured form, the meaning of the hardware-native circuit you observed after executing your Bell-state experiment on the IBM **ibm_torino** backend. This is the machine-language version of your simple logical circuit:

```
H(0)
CX(0, 1)
measure all
```

Because superconducting quantum processors do **not** support Hadamard or textbook CNOT gates natively, Qiskit must translate your logical circuit into the device's **basis gate set**, which is limited to:

- **RZ(θ)** : virtual Z rotation (no physical pulse)
- **SX** : square-root X rotation (native pulse)
- **X** : full π rotation around X
- **CX** : cross-resonance-based entangling gate

Everything else — including H, S, T, and even some Y rotations — must be synthesized from these.

Below is a clean, modular explanation of **each component** in your transpiled circuit.

1. Physical Qubit Mapping (q[60], q[61])

Your logical qubits were automatically mapped to **physical qubits 60 and 61**. This is chosen by Qiskit based on:

- device connectivity (must be neighbors for CX),
- gate fidelity,
- error rates,
- routing efficiency.

You don't choose these unless you *force* a mapping.

2. The Hadamard Decomposition (q[60])

A true Hadamard gate does not exist on IBM hardware. Instead, Qiskit synthesizes it as:

$$H \equiv RZ(\pi/2) \rightarrow SX \rightarrow RZ(\pi/2)$$

This is exactly what you see at the left of q[60]:

- **RZ($\pi/2$)** : virtual phase shift
- **SX** : physical microwave pulse
- **RZ($\pi/2$)** : another virtual phase shift

Together, these pulses implement the same unitary as the Hadamard.

3. Why q[61] Gets Extra Gates Before the CX

Even though you didn't apply any operation to qubit 1 before the CX, Qiskit inserts matching **RZ–SX–RZ** blocks on q[61]. These serve multiple hardware-level purposes:

A. Frame alignment

Superconducting qubits use virtual-Z frame tracking. The transpiler adds RZ gates to synchronize qubit phases prior to entanglement.

B. Compensation for parasitic interactions

The cross-resonance (CX) pulse unintentionally introduces stray interaction terms (IX, ZI, ZZ, XI). Pre-corrections reduce these.

C. Calibration optimization side effects

Machines maintain calibrated frames for individual qubits; these pre-gates bring q[61] into the same dynamical frame as q[60] before entangling.

So these gates appear not because your algorithm requires them, but because **the hardware does**.

4. The Entangling Gate (CX) Implementation

Your logical CNOT becomes a machine-level **cross-resonance pulse sequence**, represented visually as:

q[60] •————
q[61] └──X───

But physically, a CNOT is *not* a single clean pulse. It is:

- a microwave drive applied to q[60] at q[61]'s resonant frequency,
- producing an effective Hamiltonian $\sim ZX$,
- with multiple cancellation and echo pulses.

This is why there are **additional SX and RZ gates on q[61] after the CNOT**: these are part of cross-resonance echo sequences required to clean up undesired evolution.

5. Barrier Separators (the “||” vertical markers)

The vertical bars mark **compiler barriers**. They signal the transpiler:

- not to reorder gates across this point,
- to finalize all unitary evolution before measurement,
- to keep measurement operations isolated.

These do not affect the physics but structure the schedule.

6. Measurement Pulses (Gray Z boxes)

The gray boxes represent the final **Z-basis measurement pulses**, which:

- energize the qubit's readout resonator,
- demodulate the returning microwave signal,
- collapse the qubit into $|0\rangle$ or $|1\rangle$,
- feed the result into classical registers.

The dashed lines connect these measurements to the output classical bits.

7. Putting It All Together

Your simple logical Bell circuit:

H(0)
CX(0, 1)
measure

Becomes this hardware-expanded form:

q[60]: RZ \rightarrow SX \rightarrow RZ —————●————— Measure
 q[61]: RZ \rightarrow SX \rightarrow RZ —————X \rightarrow SX \rightarrow RZ ——— Measure

Where each additional pulse corrects, aligns, or compensates for physical realities of superconducting qubit operation.

8. Why All This Matters

This circuit reveals the entire **physical implementation layer** of your algorithm. It shows:

- how abstract gates become microwave pulses,
- how qubit connectivity forces routing choices,
- how hardware compensates for unwanted couplings,
- how real machines differ profoundly from textbook circuits.

Studying these decompositions is essential for:

- understanding quantum noise,
- interpreting experimental results,
- improving algorithm design for real hardware,
- working effectively with quantum transpilation.

This summary serves as a reference for your future quantum computing explorations.