



INTERPOLACIÓN CON PYTHON Y TRANSFORMA DE FOURIER



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Interpolación

- Se denomina en un conjunto de número se determine encontrar un polinomio de grado n .

```
In [1]: from scipy.interpolate import barycentric_interpolate
import numpy as np
import matplotlib.pyplot as plt
```

```
In [2]: def runge(x):
        """Función de Runge."""
        return 1 / (1 + x ** 2)
        N = 11 # Nodos de interpolación
        xp = np.linspace(-5,5,N)
        fp = runge(xp)
        x = np.linspace(-5, 5,200)
        y = barycentric_interpolate(xp, fp, x)
```

Obtener datos

Se obtienen los datos de la siguiente Imagen:

```
22
23 int main()
24     //Reader Image
25     vtkSmartPointer<vtkPNGReader> reader =
26     vtkSmartPointer<vtkPNGReader>::New();
27     reader->SetFileName("FFT.png");
28
29     //Filtro FFT
30     //implements a fast Fourier transform
31     vtkSmartPointer<vtkImageFFT> fftFilter =
32     vtkSmartPointer<vtkImageFFT>::New();
33     fftFilter->SetInputConnection(reader->GetOutputPort());
34     fftFilter->Update();
35
36     //Filter casts the input type to match the output
37     //type in the image processing pipeline.
38     vtkSmartPointer<vtkImageCast> fftCastFilter =
39     vtkSmartPointer<vtkImageCast>::New();
40     fftCastFilter->SetInputConnection(fftFilter->GetOutputPort());
41     fftCastFilter->SetOutputScalarTypeToUnsignedChar();
42     fftCastFilter->Update();
43
```

Mapear

```
//Filter casts the input type to match the output
//type in the image processing pipeline.
vtkSmartPointer<vtkImageCast> fftCastFilter =
    vtkSmartPointer<vtkImageCast>::New();
fftCastFilter->SetInputConnection(fftFilter->GetOutputPort());
fftCastFilter->SetOutputScalarTypeToUnsignedChar();
fftCastFilter->Update();

//Implements the reverse fast Fourier transform.
vtkSmartPointer<vtkImageRFFT> rfftFilter =
    vtkSmartPointer<vtkImageRFFT>::New();
rfftFilter->SetInputConnection(fftFilter->GetOutputPort());
rfftFilter->Update();

vtkSmartPointer<vtkImageExtractComponents> extractRealFilter =
    vtkSmartPointer<vtkImageExtractComponents>::New();
extractRealFilter->SetInputConnection(rfftFilter->GetOutputPort());
extractRealFilter->SetComponents(0);
extractRealFilter->Update();

vtkSmartPointer<vtkImageCast> rfftCastFilter =
    vtkSmartPointer<vtkImageCast>::New();
rfftCastFilter->SetInputConnection(extractRealFilter->GetOutputPort());
rfftCastFilter->SetOutputScalarTypeToUnsignedChar();
rfftCastFilter->Update();

// Create actors
vtkSmartPointer<vtkImageActor> originalActor =
    vtkSmartPointer<vtkImageActor>::New();
originalActor->GetMapper()->SetInputConnection(reader->GetOutputPort());

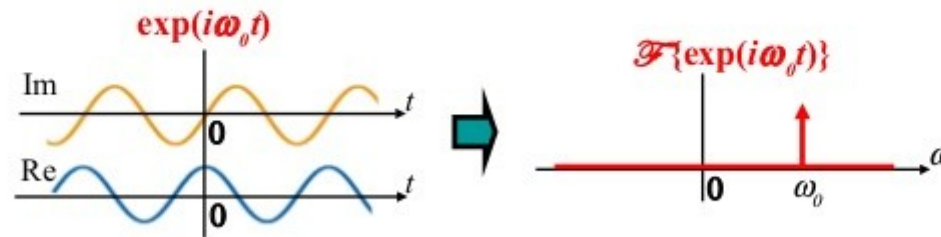
vtkSmartPointer<vtkImageActor> fftActor =
    vtkSmartPointer<vtkImageActor>::New();
fftActor->GetMapper()->SetInputConnection(fftCastFilter->GetOutputPort());
```

Cálculos de la Transforma de Fourier

La transformada de Fourier de la onda plana $\exp(i\omega_0 t)$

$$F\{e^{i\omega_0 t}\} = \int_{-\infty}^{\infty} e^{i\omega_0 t} e^{-i\omega t} dt =$$

$$\int_{-\infty}^{\infty} e^{-i(\omega - \omega_0)t} dt = 2\pi \delta(\omega - \omega_0)$$



La TF de $\exp(i\omega_0 t)$ es una frecuencia pura.

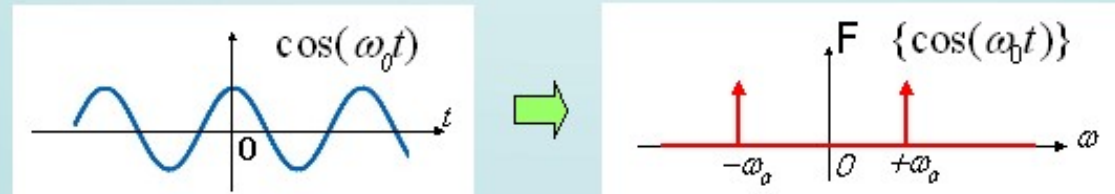
Cálculos de la Transforma de Fourier

Transformada de Fourier de la función coseno

$$\begin{aligned} f(t) &= \cos(\omega_0 t) & \hat{f}(\omega) &= \int_{-\infty}^{\infty} \cos(\omega_0 t) e^{-i\omega t} dt \\ &= \int_{-\infty}^{\infty} \left(\frac{e^{i\omega_0 t} + e^{-i\omega_0 t}}{2} \right) e^{-i\omega t} dt = \frac{1}{2} \int_{-\infty}^{\infty} (e^{-i(\omega - \omega_0)t} + e^{-i(\omega + \omega_0)t}) dt = \end{aligned}$$

$$\hat{f}(\omega) = \frac{2\pi}{2} [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)]$$

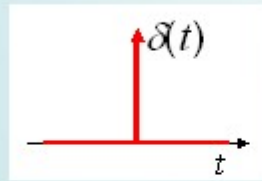
$$\hat{f}(\omega) = \pi [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)]$$



Cálculos de la Transforma de Fourier

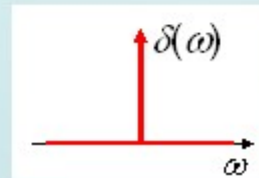
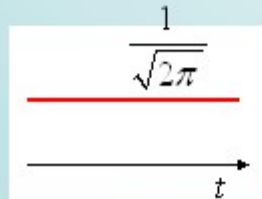
Transformada de Fourier de la $\delta(t)$:

$$f(t) = \delta(t) \rightarrow \hat{f}(\omega) = \int_{-\infty}^{\infty} \delta(t) e^{-i\omega t} dt = 1$$



Observa que la transformada de Fourier de $f(t) = 1$ es:

$$\hat{f}(\omega) = \int_{-\infty}^{\infty} 1 e^{-i\omega t} dt = 2\pi \delta(\omega)$$



Recordemos →

Transformada de Fourier

