

Name: Joseph Specht

Quiz 10 (Total: 30 points; 5 bonus points possible)

Due back on Wed. 19 April, 10 p.m.

- *Save your entire assignment as one PDF document and upload it in the appropriate assignment folder on Canvas.*
- *Assignments will only be graded if the honor code statement, below, is completed and signed.*

Honor Code Statement

ME 200, Quiz 10

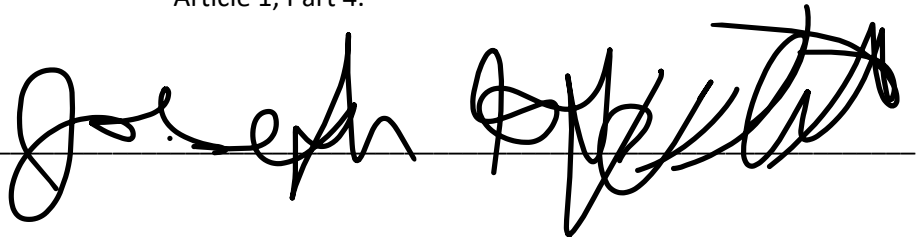
Being a student of high standards, I pledge to embody
the principles of *academic integrity*.

This ME 200 quiz is my own work. I did not seek (or get) outside help or collaboration with any of the questions and their solutions. I also did not offer my solutions to any other student.

I understand that this quiz is “open book” and “open notes” which means that I was permitted to use my prescribed textbook and lecture notes when addressing any of the questions. I have properly cited any other resources, with full cognizance of the regulations pertaining to plagiarism, copyright infringement, academic cheating, etc., as stipulated in the Student Code.

I acknowledge that academic violations will be dealt with according to the UIUC Student Code, Article 1, Part 4.

ME 200 Student's signature: _____

A handwritten signature in black ink, appearing to read 'Joseph Specht', written over a horizontal line.

Student's Name: Joseph Specht

Net-ID: jspecht3

Date: 4/17/23

2#10 - Joseph Specter

a)

1600K

Reversible
Heat Engine

$\rightarrow W_{out}$

400 K

$$\eta_{th} = 1 - \frac{T_c}{T_h} = 1 - \frac{400K}{1600K} = 1 - 0.25 = 0.75 = 75\%$$

$$\eta_{th} = 0.75 = 75\%$$

b)

773K

Reversible
Heat Engine

293K

$$\eta_{th} = 1 - \frac{T_c}{T_h} = \frac{W_{net}}{Q_H} \quad \therefore Q_H = \frac{W_{net}}{1 - \frac{T_c}{T_h}}$$

$$Q_H = 1610.42 \text{ J}$$

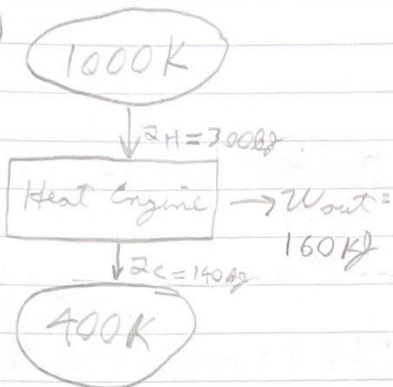
We also know $\eta_{th} = 1 - \frac{T_c}{T_h} = 1 - \frac{Q_C}{Q_H}$

$$\therefore \frac{T_c}{T_h} = \frac{Q_C}{Q_H} \Rightarrow Q_C = Q_H \left(\frac{T_c}{T_h} \right) = 1610.42 \text{ J} \left(\frac{293K}{773K} \right) = 610.4179$$

$$Q_C = 610.42 \text{ J}$$

2 #10 - Joseph Speck

2a)



1st law:

$$W_{net} = Q_H - Q_C = (300 - 140) \text{ J} = 160 \text{ J}$$

W_{net} is what it should be!

$$\text{also, } \eta_a = \frac{W_{net}}{Q_H} = \frac{160 \text{ J}}{300 \text{ J}} = .533 = 53.3\%$$

We then need to compare the efficiency to that of a theoretical engine w/ no irreversibilities.

$$\text{2nd law: } \eta_{th} = 1 - \frac{T_C}{T_H} = 1 - \frac{400 \text{ K}}{1000 \text{ K}} = 1 - .4 = .6 = 60\%$$

Since the practical efficiency < the theoretical efficiency, the system works & does not need irreversibilities to work!

2#10 - Joseph Specter

20/

1000K

$\downarrow \dot{Q}_H = 300 \text{ W}$

Heat Engine

$\rightarrow W_{\text{net}} =$

120 W

$\downarrow \dot{Q}_C = 120 \text{ W}$

400K

1st Law:

$$W_{\text{net}} = \dot{Q}_H - \dot{Q}_C = (300 - 120) \text{ W} = 120 \text{ W}$$

Work matched!

$$\eta_{\text{th}} = 1 - \frac{\dot{Q}_C}{\dot{Q}_H} = 1 - \frac{120 \text{ W}}{300 \text{ W}} = 1 - 0.4 = 0.6 = 60\%$$

2nd Law:

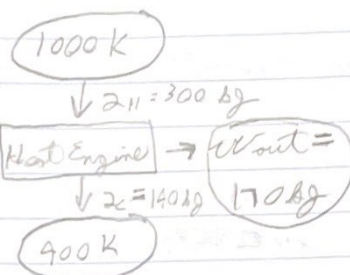
$$\eta_{\text{th}} = 1 - \frac{T_C}{T_H} = 1 - \frac{400 \text{ K}}{1000 \text{ K}} = 1 - 0.4 = 0.6 = 60\%$$

$$\eta_{\text{th}} = \eta_{\text{th}}$$

\therefore the process is theoretically possible, but the requirement is no irreversibilities can be present.

2 #10 - Joseph Specter

2c)



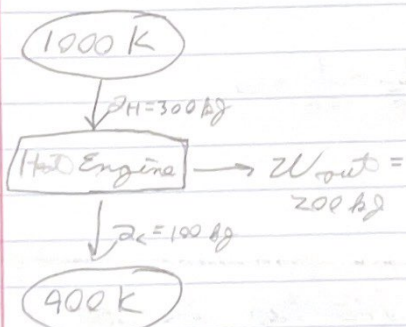
1st law:

$$W_{net} = Q_H - Q_C = 160 \text{ J}$$

$$W_{net} < W_{out} \quad \therefore \text{NOT POSSIBLE!}$$

Fails first law, so this process is impossible

2d)



1st law:

$$W_{net} = Q_H - Q_C = (300 - 100) \text{ J} = 200 \text{ J}$$

$$W_{net} = W_{out}, \text{ so checks out!}$$

$$\eta_{th} = \frac{W_{out}}{Q_H} = \frac{200 \text{ J}}{300 \text{ J}} = .667 = 66.7\%$$

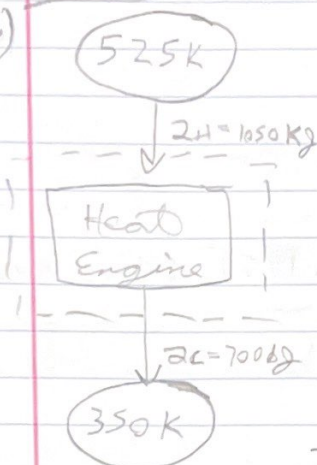
2nd law:

$$\eta'_{th} = 1 - \frac{T_C}{T_H} = 1 - \frac{400 \text{ K}}{1000 \text{ K}} = 1 - .4 = .6 = 60\%$$

$\eta_{th} > \eta'_{th} \therefore$ This process is impossible as the cycle efficiency is greater than the theoretical efficiency

2#10 - Joseph Specht

3)



using Clausius Equality

$$\oint \left(\frac{\delta Q}{T} \right) \leq 0$$

which can be written

$$\oint \left(\frac{\delta Q}{T} \right) = -\sigma_{\text{cycle}}$$

$$-\sigma_{\text{cycle}} = \frac{Q_H}{T_H} - \frac{Q_C}{T_C}$$

$$\Rightarrow -\sigma_{\text{cycle}} = \frac{1050 \text{ J}}{525 \text{ K}} - \frac{700 \text{ J}}{350 \text{ K}} = \frac{1}{2 \text{ K}} - \frac{1}{2 \text{ K}} = 0$$

$$\sigma_{\text{cycle}} = 0$$

There are no irreversibilities in the cycle meaning it is reversible & almost not possible.