

WS #7 Joseph Specht

$$\underline{1a)} \quad z = \frac{1}{1+j\omega} \cdot \frac{1-j\omega}{1-j\omega} = \frac{1-j\omega}{1+\omega^2} = \frac{1}{1+\omega^2} - \frac{j\omega}{1+\omega^2}$$

$$R = \sqrt{\left(\frac{1}{1+\omega^2}\right)^2 + \left(\frac{\omega}{1+\omega^2}\right)^2} = \frac{1}{\sqrt{1+\omega^2}} = R$$

$$\Theta = \boxed{\arctan\left(\frac{-\omega}{1}\right)} = \boxed{\arctan(-\omega)}$$

$$\underline{b)} \quad z = \frac{-1}{1+j\omega} \cdot \frac{1-j\omega}{1-j\omega} = \frac{-1}{1+\omega^2} + \frac{j\omega}{1+\omega^2} \quad R = \sqrt{\frac{1}{(1+\omega^2)^2} + \frac{\omega^2}{(1+\omega^2)^2}} = \frac{1}{\sqrt{1+\omega^2}} = R$$

$$\Theta = \arctan\left(\frac{\omega}{-1}\right) = \boxed{\arctan(-\omega) + \pi} = \Theta$$

$$\underline{c)} \quad z = \frac{1}{1-j\omega} \cdot \frac{1+j\omega}{1+j\omega} = \frac{1+j\omega}{1+\omega^2} \quad R = \sqrt{\frac{1^2}{(1+\omega^2)^2} + \frac{\omega^2}{(1+\omega^2)^2}} = \frac{1}{\sqrt{1+\omega^2}} = R$$

$$\Theta = \arctan\left(\frac{\omega}{1}\right) = \boxed{\arctan(\omega)} = \Theta$$

$$\underline{2)} \quad v = 5 \sin(5t) + 5\sqrt{2} \sin(5t+45^\circ) = 5 \cos(5t-90^\circ) + 5\sqrt{2} \cos(5t-45^\circ)$$

$$\begin{aligned} \bar{F} &= 5 \angle -90^\circ + 5\sqrt{2} \angle -45^\circ = 5(\cos(-90^\circ) + j\sin(-90^\circ)) + 5\sqrt{2}(\cos(-45^\circ) + j\sin(-45^\circ)) \\ &= 5(0-j) + 5\sqrt{2}\left(\frac{-\sqrt{2}}{2} + \frac{\sqrt{2}}{2}j\right) = -5j + 5 + 5j = 5 = 5 \angle 0^\circ \end{aligned}$$

$$\bar{V}(t) = 5 \cos(5t) = \boxed{5 \sin(5t+90^\circ) = V(t)}$$