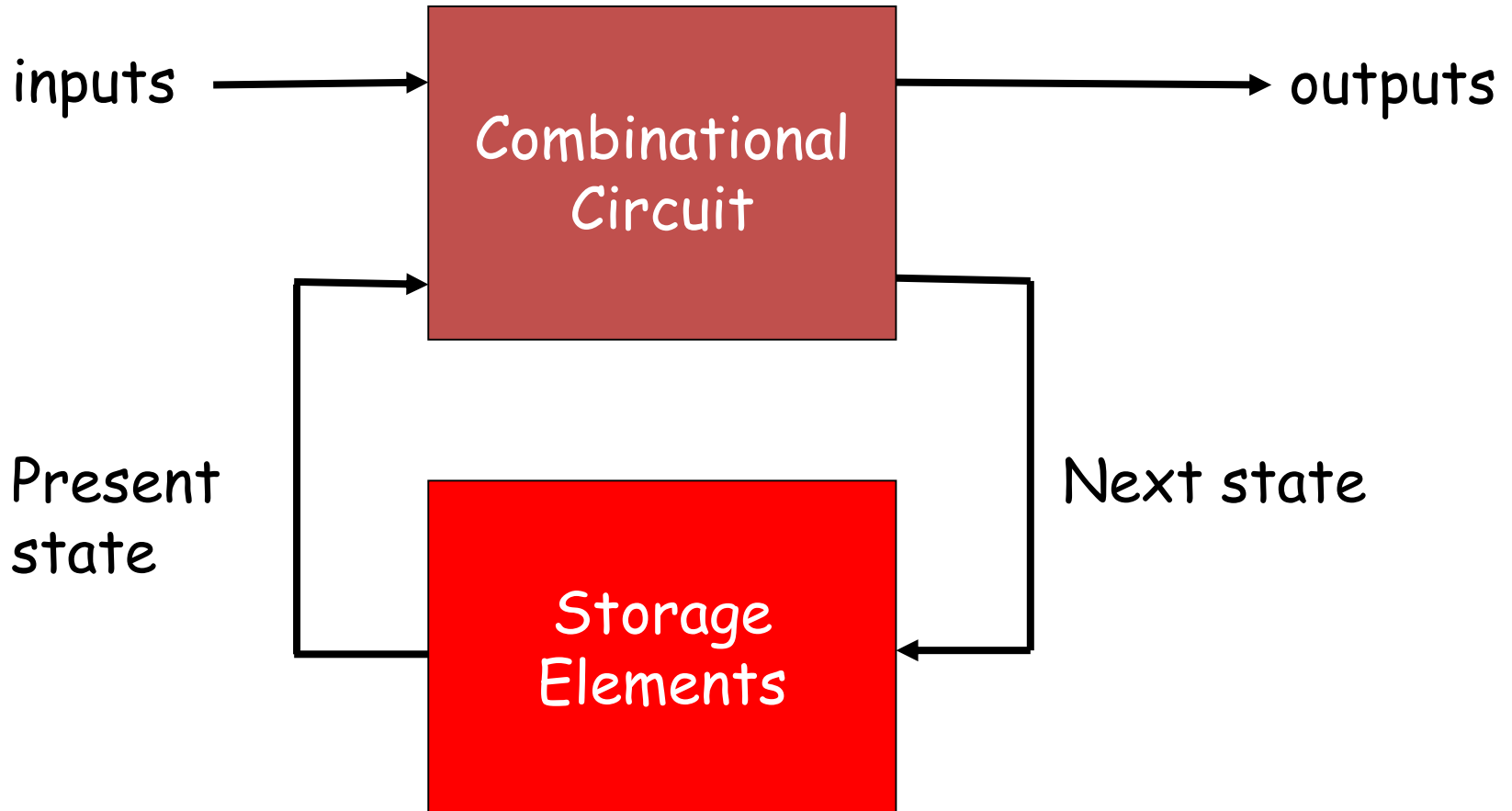


Sequential Circuit Model



Present state depends on the previous inputs

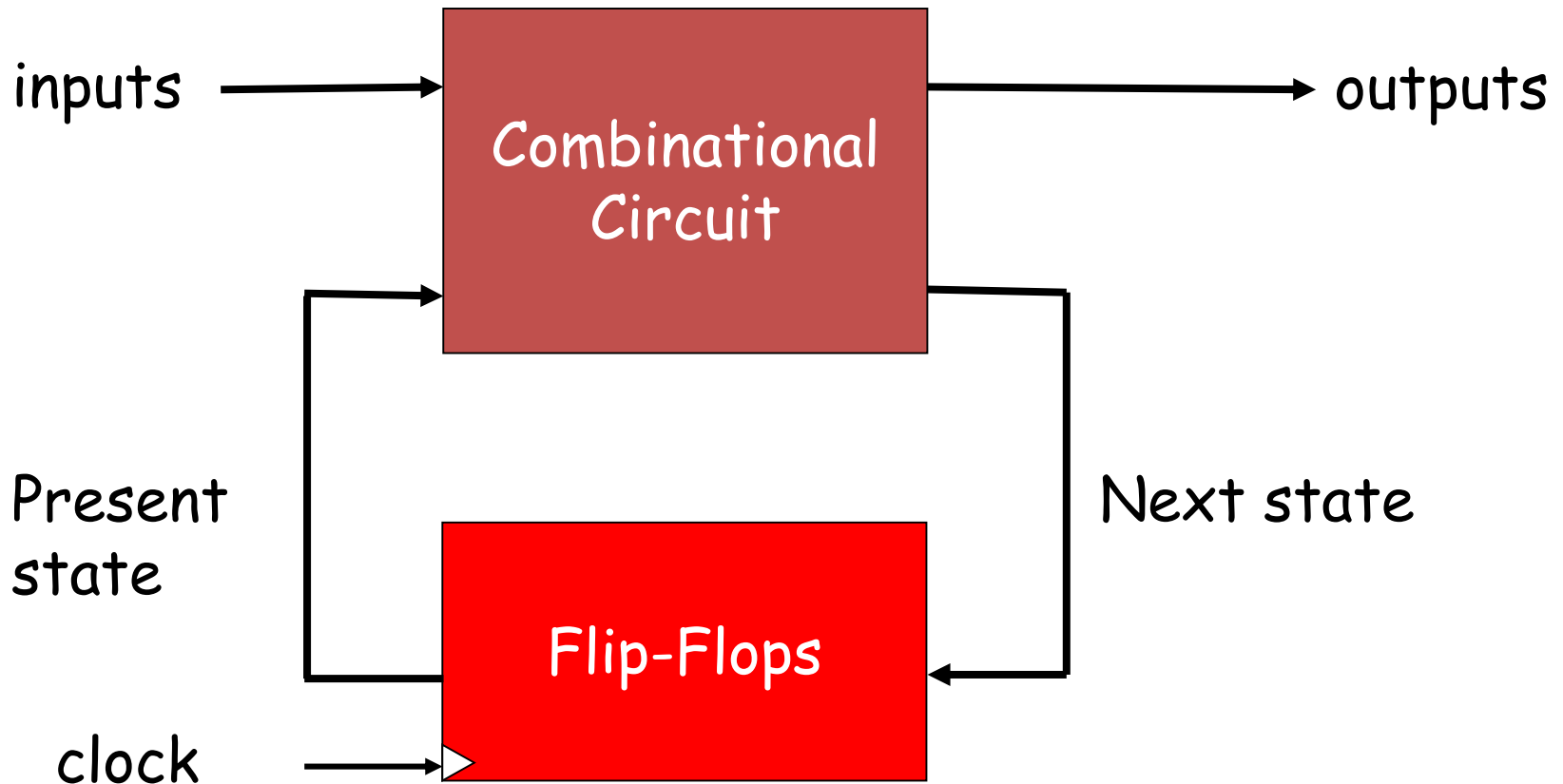
Synchronous Sequential Circuits

- Behavior defined from knowledge of its signals at **discrete** instances of time.
- **Discrete** instances of time need synchronization.
- Synchronization is done by a common clock signal.
- Clock signal is a periodic square signal.
- Storage elements observe inputs and can change state only in relation to a timing signal (**clock pulses** from a **clock**)



Synchronous Sequential Circuits

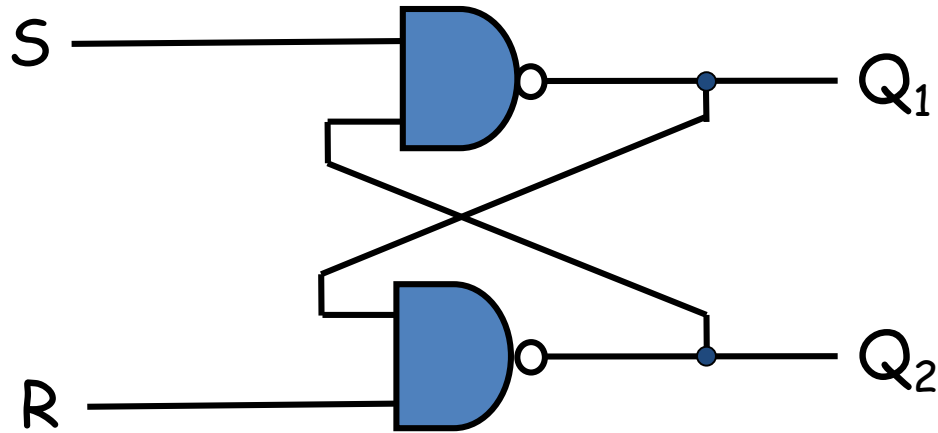
- The storage elements are flip-flops that can store one bit of information.



Latch

- Basic storage element
- A latch is a storage element that can store its content forever.
- Latches are asynchronous circuits and do not need a clock signal to operate.
- Hence they can not be used in synchronous circuits directly.
- They are used to construct flip-flops.

SR-Latch



$$Q_1 = (S Q_2)' = S' + q_2'$$

$$Q_2 = (R Q_1)' = R' + q_1'$$

SR=00 \Rightarrow $\left. \begin{array}{l} 00-11-11-... \\ 01-11-11-... \\ 10-11-11-... \end{array} \right\} Q_1 Q_2 = 11$

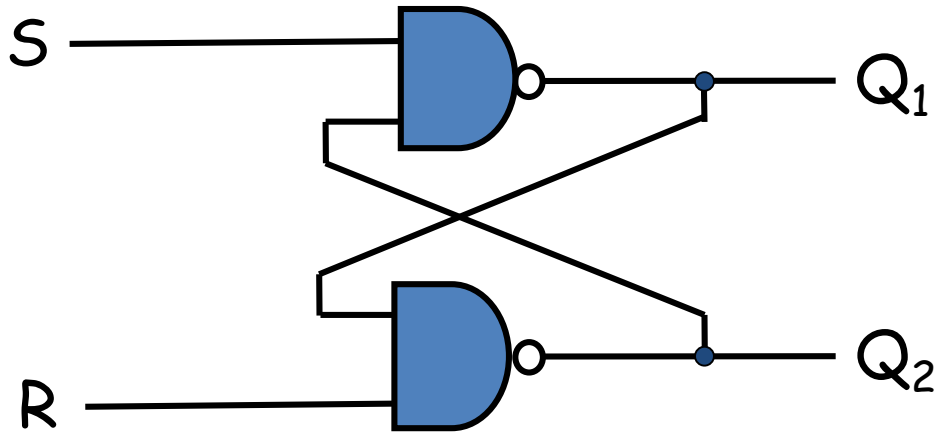
SR=01 \Rightarrow $\left. \begin{array}{l} 00-11-10-10-... \\ 01-11-10-10-... \end{array} \right\} Q_1 Q_2 = 10$

SR=10 \Rightarrow $\left. \begin{array}{l} 00-11-01-01-... \\ 10-11-01-01-... \end{array} \right\} Q_1 Q_2 = 01$

SR=11 \Rightarrow $\left. \begin{array}{l} 00-11-00-11-... \\ 01-01-... \\ 10-10-... \end{array} \right\} \begin{array}{l} Q_1 Q_2 = \text{osilates} \\ Q_1 Q_2 = q_1 q_2 \end{array}$

S	R	q ₁	q ₂	Q ₁	Q ₂
0	0	0	0	1	1
0	0	0	1	1	1
0	0	1	0	1	1
0	0	1	1	1	1
0	1	0	0	1	1
0	1	0	1	1	1
0	1	1	0	1	0
0	1	1	1	1	0
1	0	0	0	1	1
1	0	0	1	0	1
1	0	1	0	1	1
1	0	1	1	0	1
1	1	0	0	1	1
1	1	0	1	0	1
1	1	1	0	1	0
1	1	1	1	0	0

SR-Latch



S	R	Q ₁	Q ₂
0	0	x	x
0	1	1	0
1	0	0	1
1	1	q ₁	q ₂

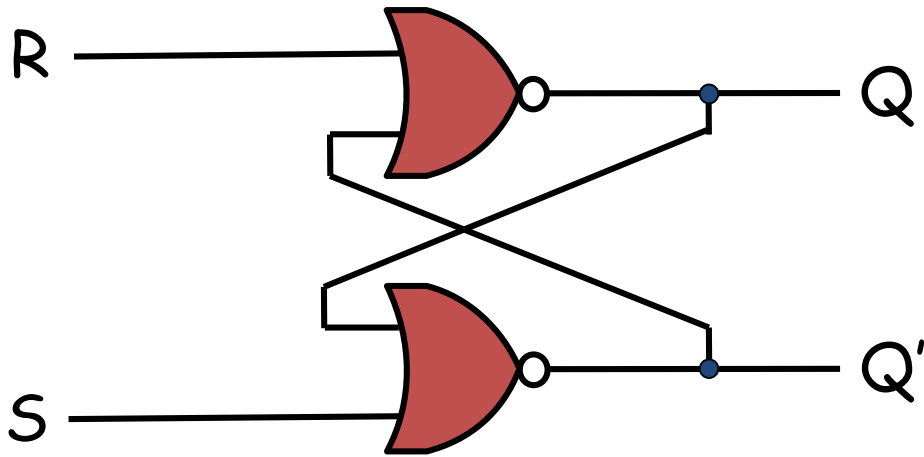
Undefined

$$Q_1 = Q_2'$$

$$Q_1 = Q$$

$$Q_2 = Q'$$

SR-Latch

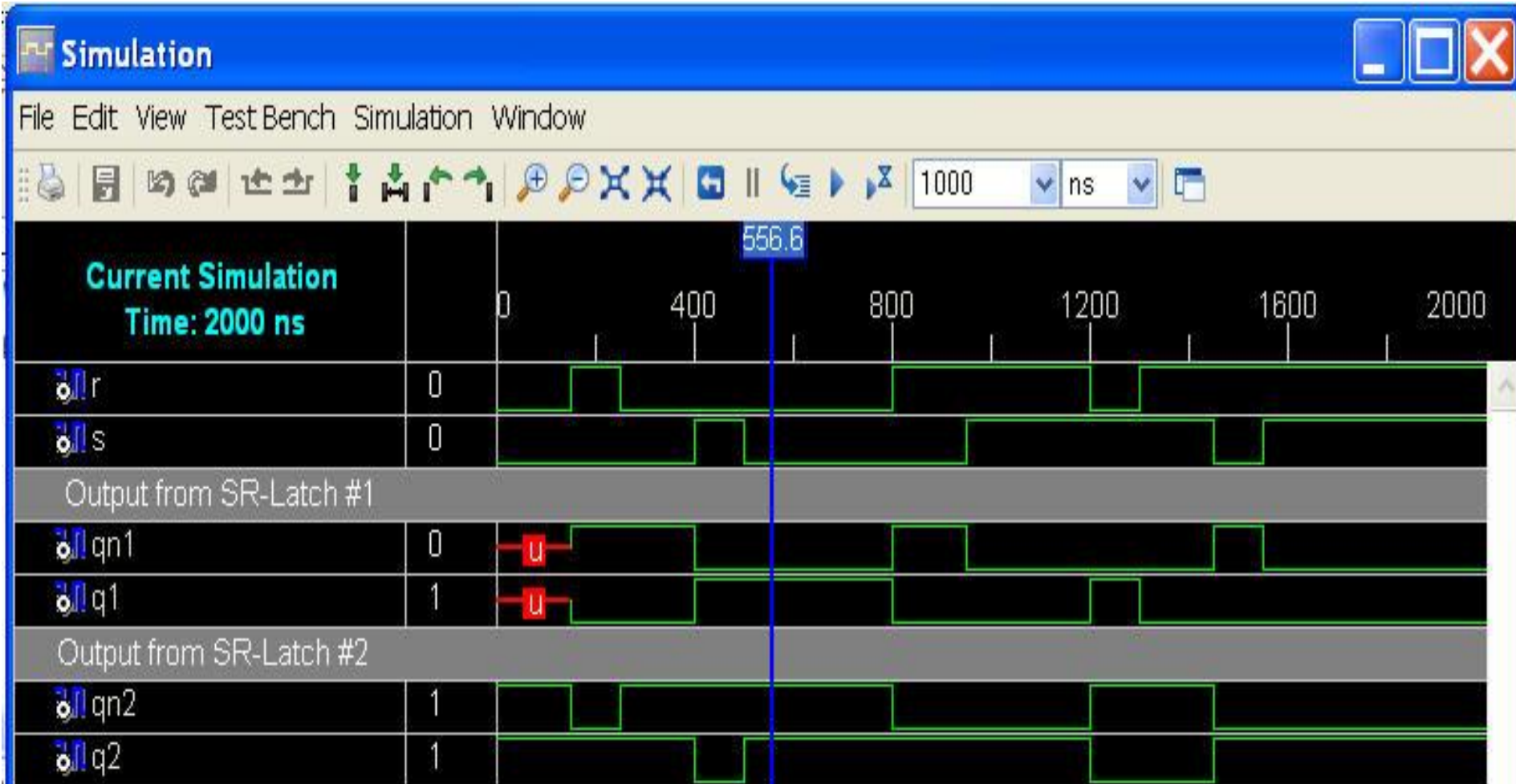


$$Q = (R + Q')' = R' q$$
$$Q' = (S + Q)' = S' q'$$

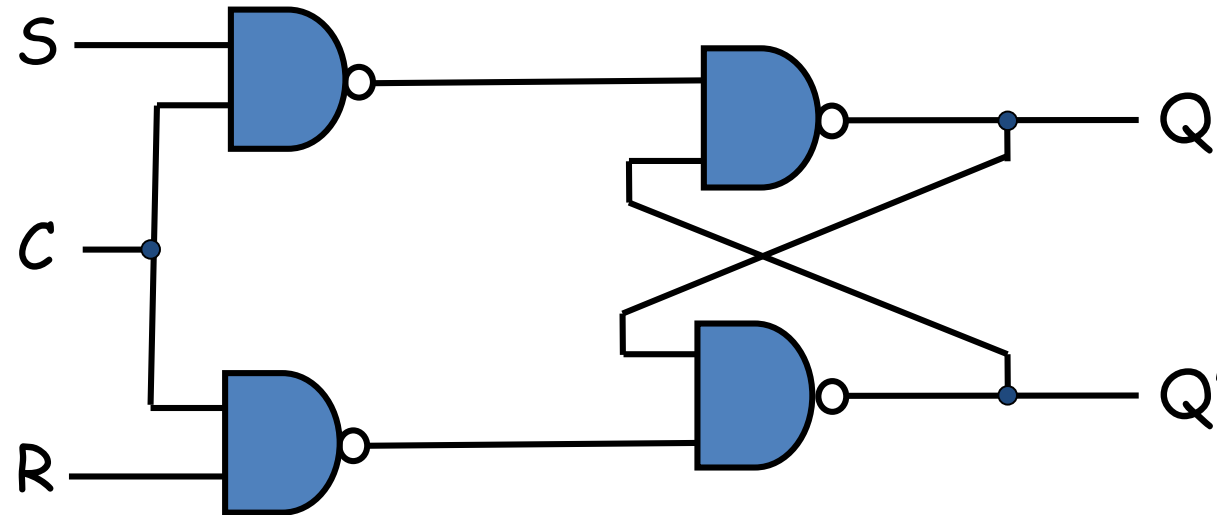
S	R	Q	Q'
0	0	q	q'
0	1	0	1
1	0	1	0
1	1	X	X

Undefined

Simulation of SR-Latch



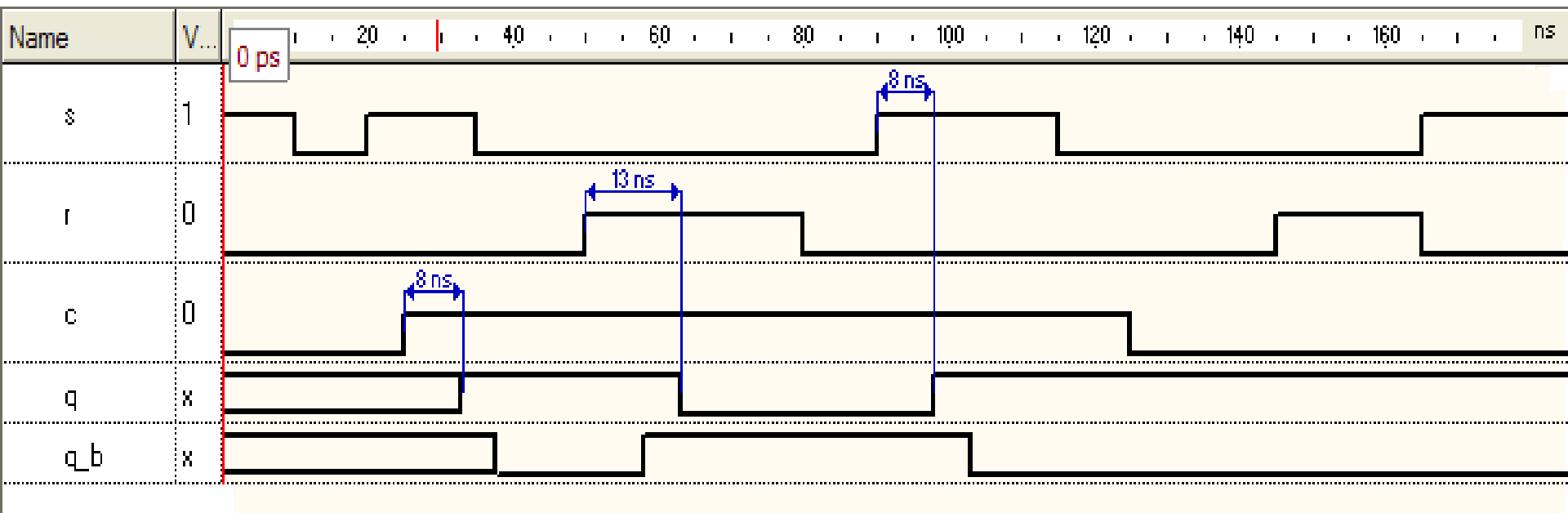
SR-Latch with Control Input



$$Q = ((S \ C)' Q')' = SC + Q$$
$$Q' = ((R \ C)' Q)' = RC + Q'$$

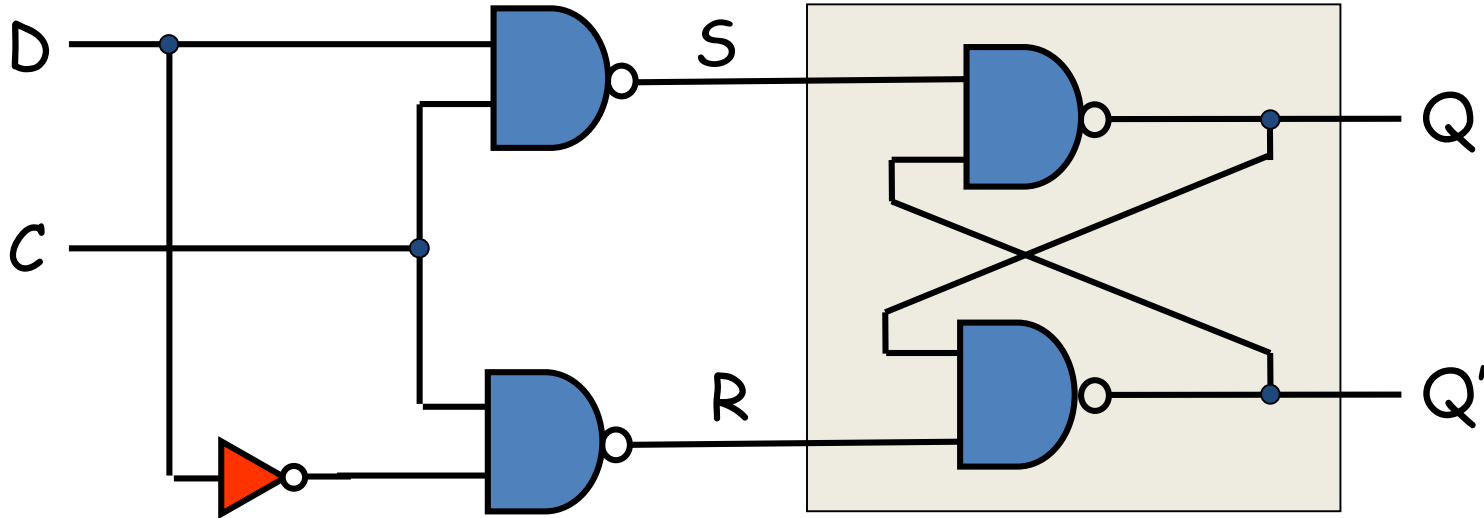
C	S	R	Q	Q'
0	X	X	No change	
1	0	0	No change	
1	0	1	Q = 0 Reset state	
1	1	0	Q = 1 Set state	
1	1	1	Undefined	

Simulation of SR-Latch with Control Input



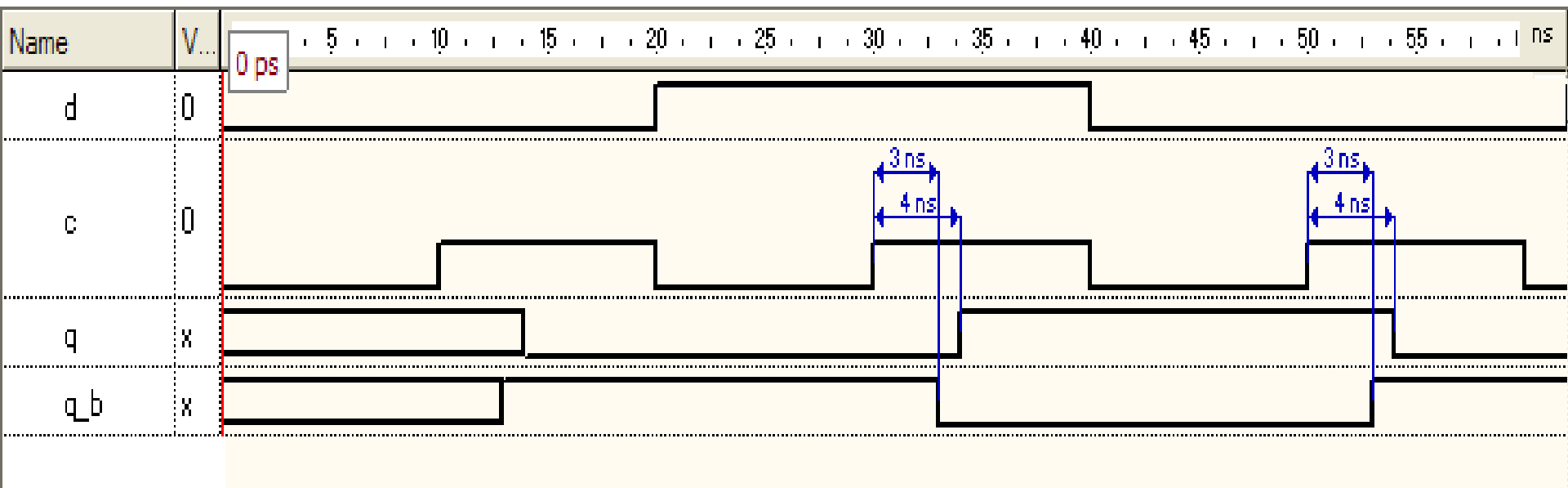
D-Latch

- Because the undefined situation can cause stability problems, SR latches are not used often.
- Solution: D-latch



This circuit guarantees that S and R inputs are always each other's complement.

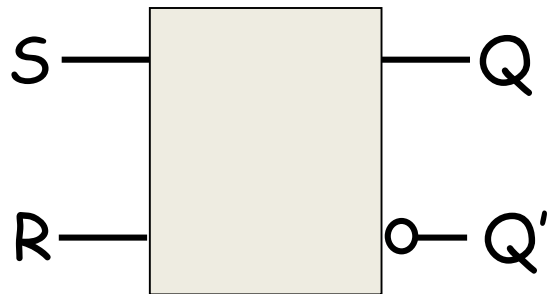
Simulation of D-Latch



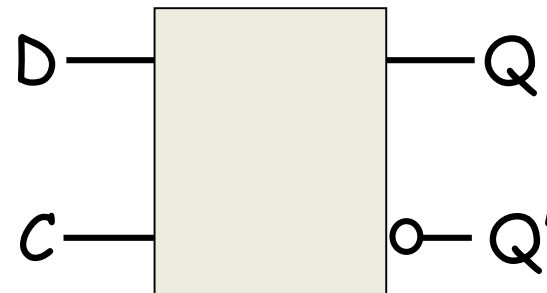
D-Latch

C	D	Next state of Q
0	X	No change
1	0	$Q = 0$; reset state
1	1	$Q = 1$; set state

- D input is sampled when $C=1$.



SR-latch



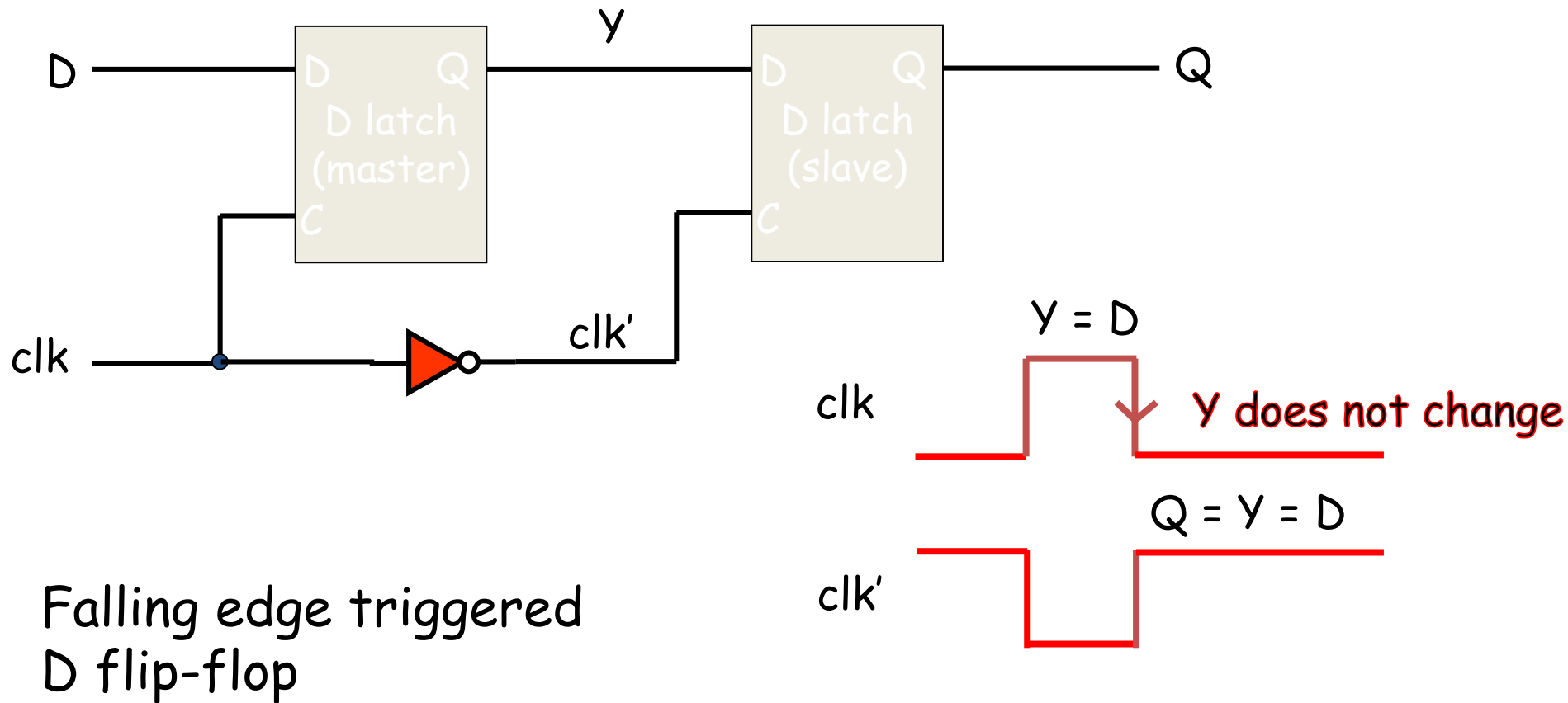
D-latch

D Latch as a Storage Element

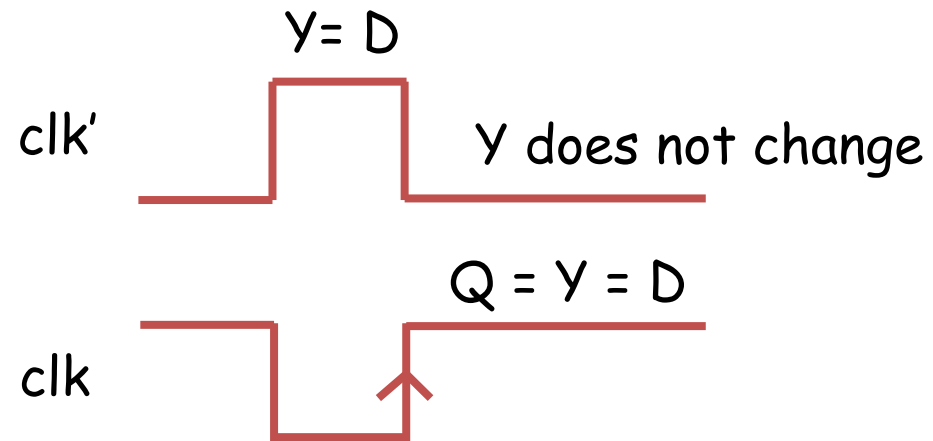
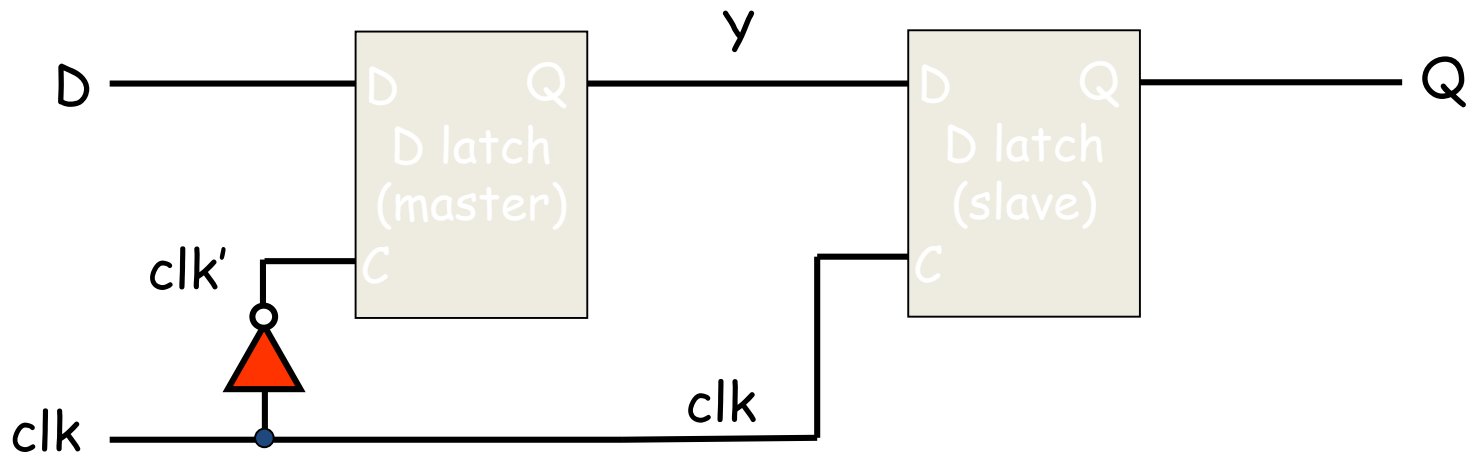
- When $C = 1$ D latch copies the input to the output.
- When $C = 0$ the information is kept unchanged.
- Latches are called **level triggered**.
 - While C is in logic-1 level, the changes at the input cause changes at the output.
- The states of the storage elements should change synchronously.
- We need a storage element which changes the state in a very short time spot.
- These storage elements are called **edge triggered** and specially flip-flops.

Edge Triggered D Flip-Flop

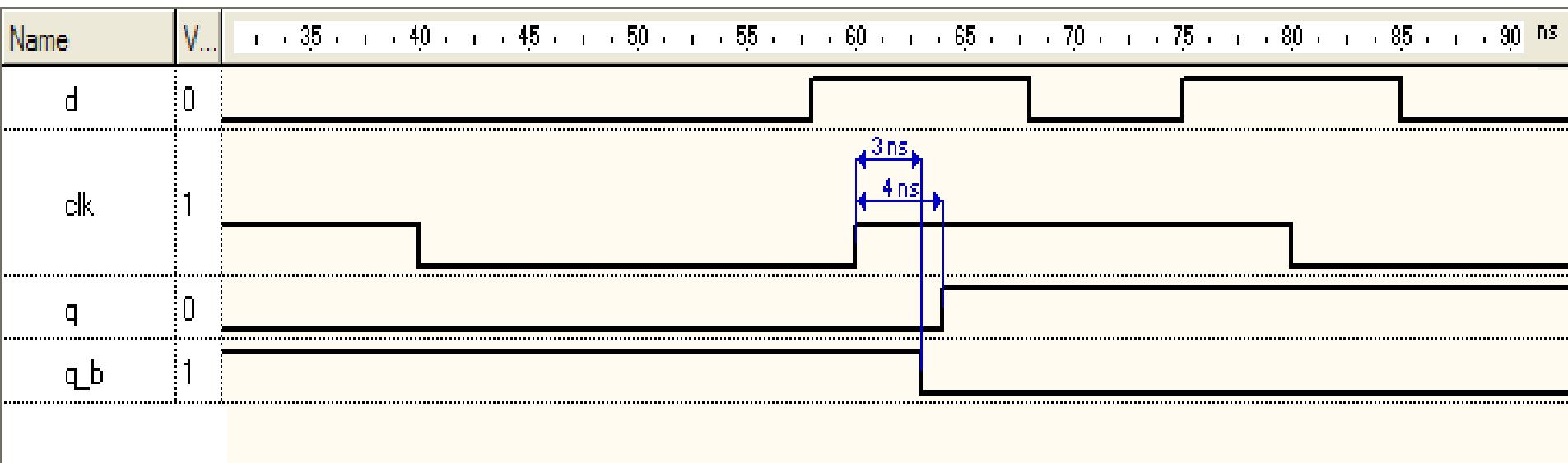
- Edge triggered D flip-flop can be constructed by using two D latches.



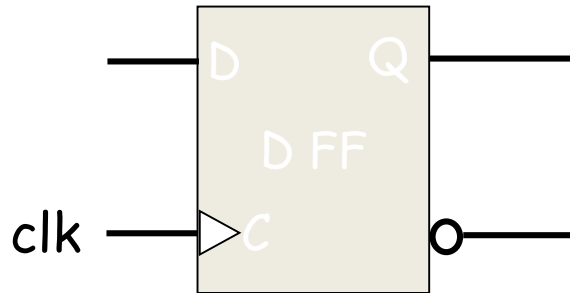
Rising Edge Triggered D Flip-Flop



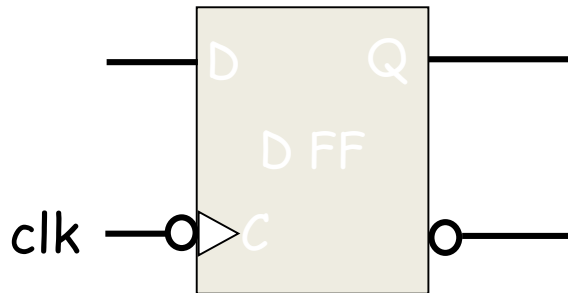
Simulation of Rising Edge Triggered D Flip-Flop



D Flip-Flop Symbols



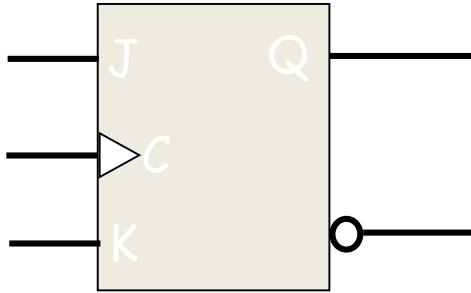
Rising edge triggered
D Flip-Flop



Falling edge triggered
D Flip-Flop

- Characteristic Equation
 - $Q(t+1) = D$
 - $Y=D$

JK Flip-Flop



J	K	Q(t+1)	Next State
0	0	Q(t)	No change
0	1	0	Reset
1	0	1	Set
1	1	Q'(t)	Complement

J	K	Y	Next State
0	0	y	No change
0	1	0	Reset
1	0	1	Set
1	1	y'	Complement

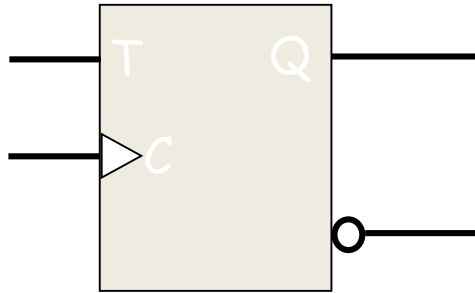
- Characteristic Equation

- $Q(t+1) = JQ'(t) + K'Q(t)$

- $Y = Jy' + K'y$

Characteristic Table

T (Toggle) Flip-Flop

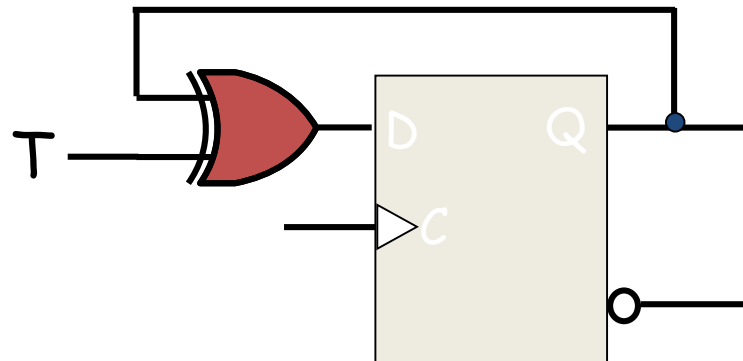
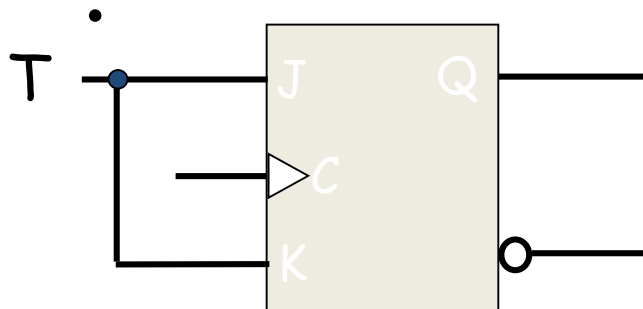


T	Q(t+1)	next state
0	Q(t)	no change
1	Q'(t)	Complement
T	y	next state
0	y	no change
1	y'	Complement

Characteristic Equation

Characteristic Table

- $Q(t+1) = T \oplus Q(t) = TQ'(t) + T'Q(t)$
- $Y = T \oplus y = Ty' + T'y$

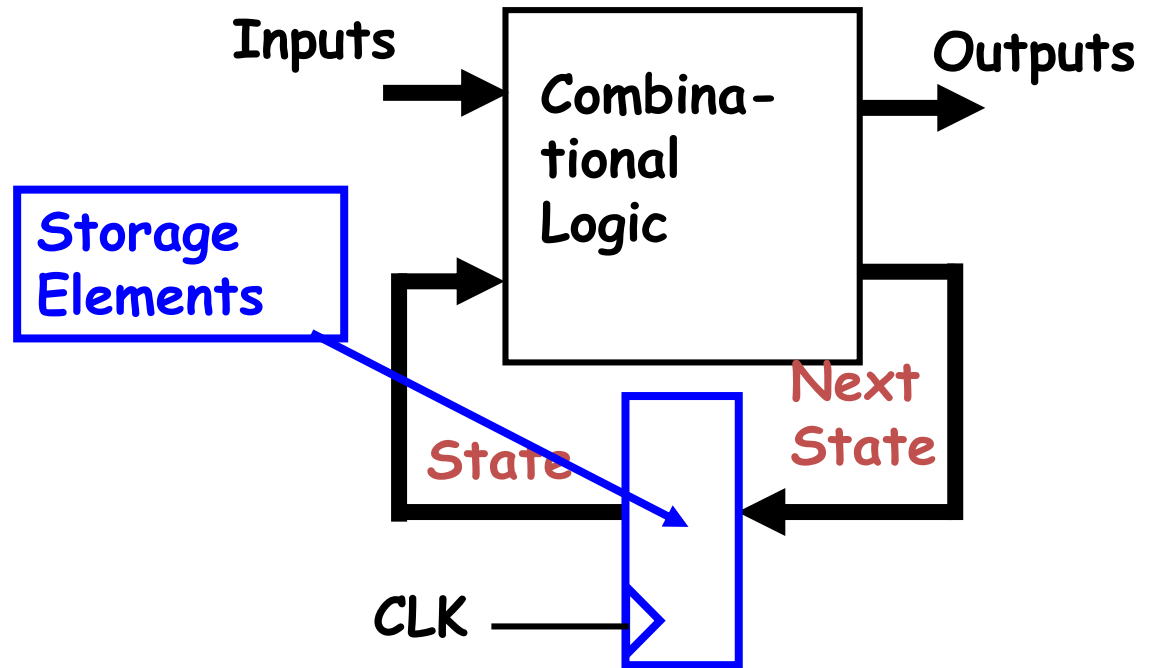


Analysis of Synchronous Sequential Circuits

- Aim:
 - Finding the behaviour of the synchronous sequential circuits
 - “Behaviour”
 - Inputs
 - Outputs
 - States of the flip-flops
 - Finding the Boolean functions of the outputs and the inputs of the flip-flops
 - Output and state equations
 - state table
 - state diagram

Analysis of Synchronous Sequential Circuits

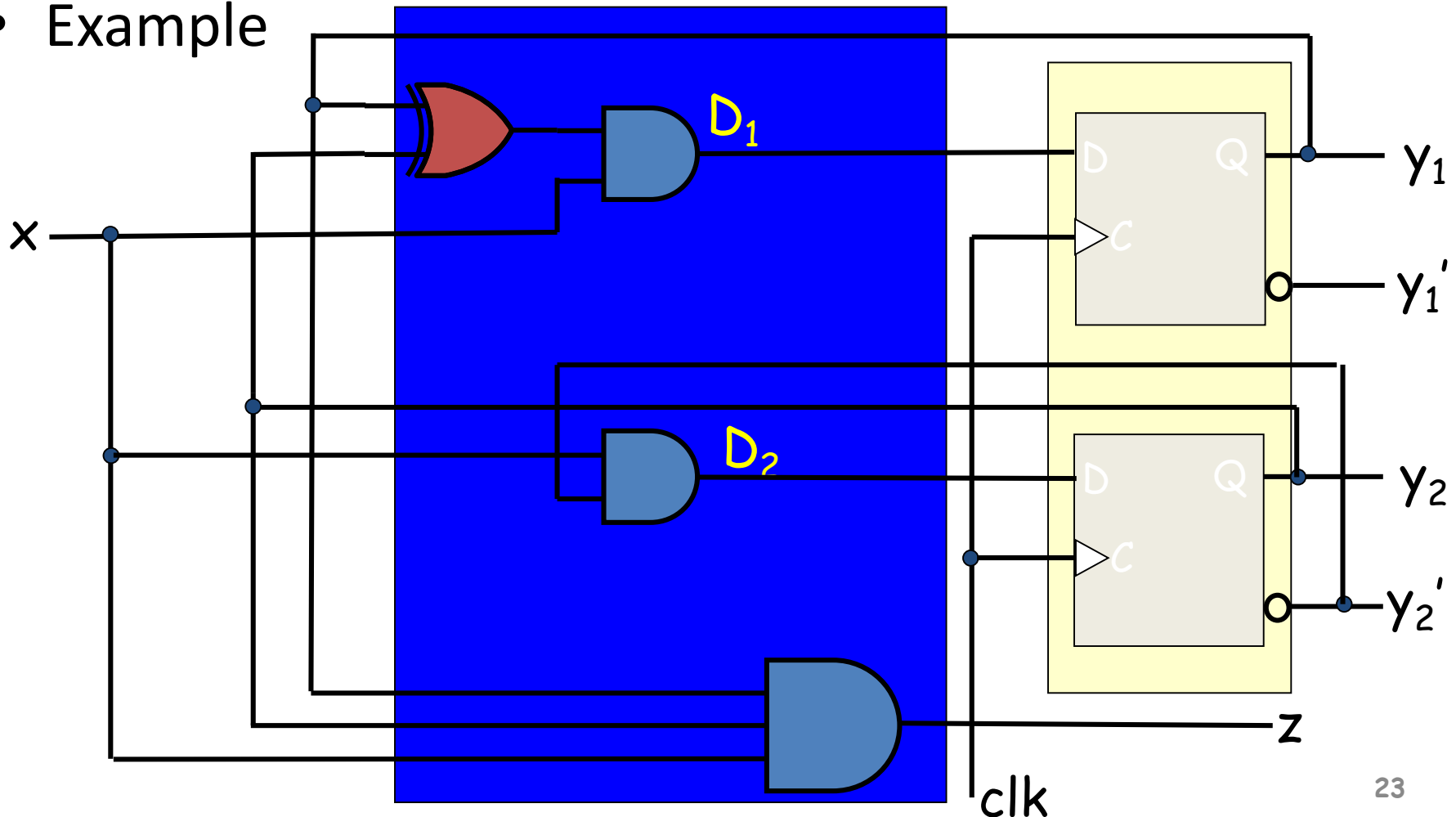
- **Current State** at time **t** is stored in an array of flip-flops.
- **Next State** at time **t+1** is a Boolean function of Current State and Inputs.
- **Outputs** at time **t** are a Boolean function of Current State and sometimes Inputs.



State and Output Equations

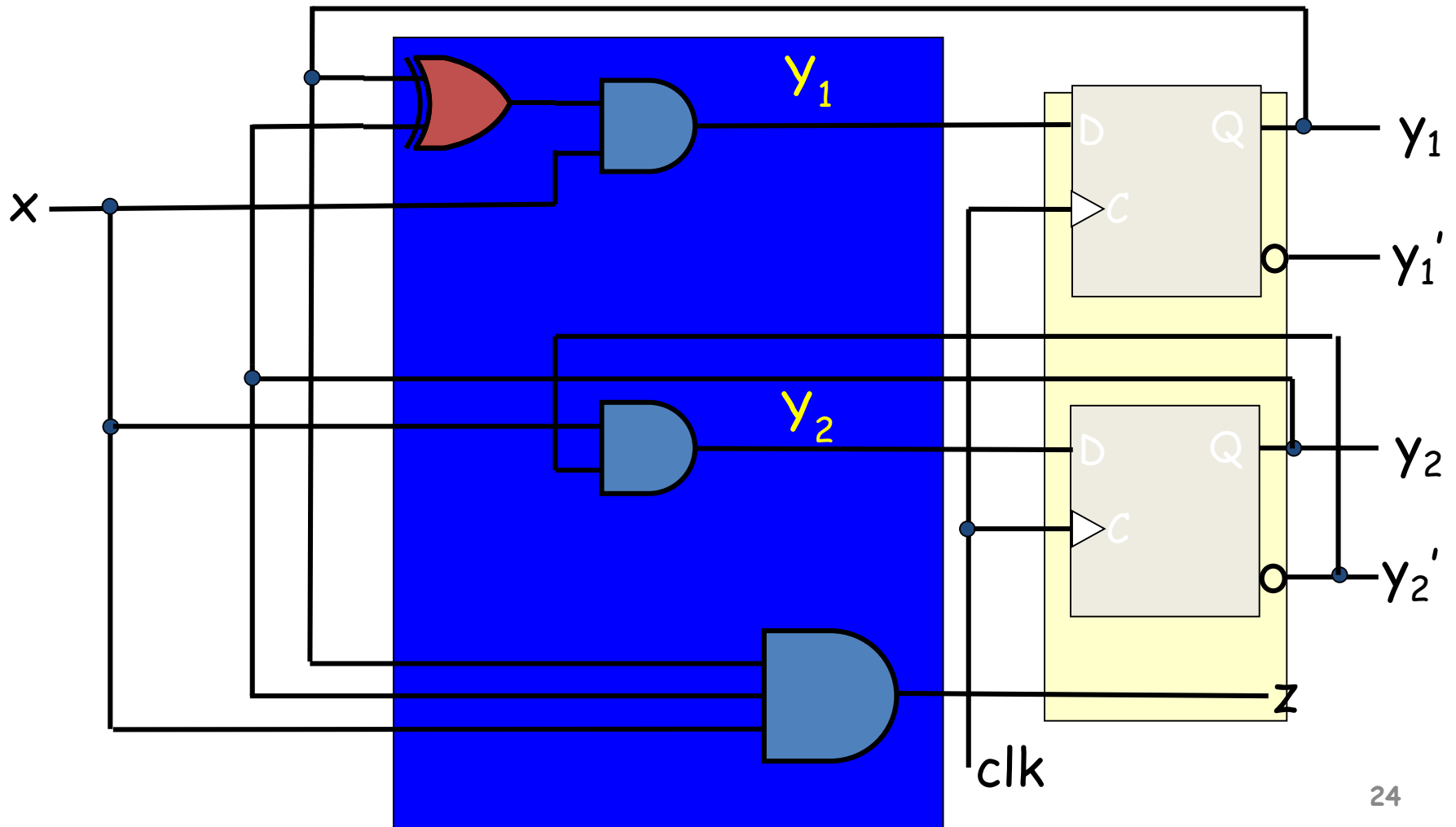
- They are also called transition equations.
 - They show the next state as a function of the present state and the inputs.

- Example



State and Output Equations

- $D_1 = (y_1 \oplus y_2) x = Y_1$
- $D_2 = x y_2' = Y_2$
- $z = y_1 y_2 x$



Example: State (Transition) Table

$y_1 = ?$

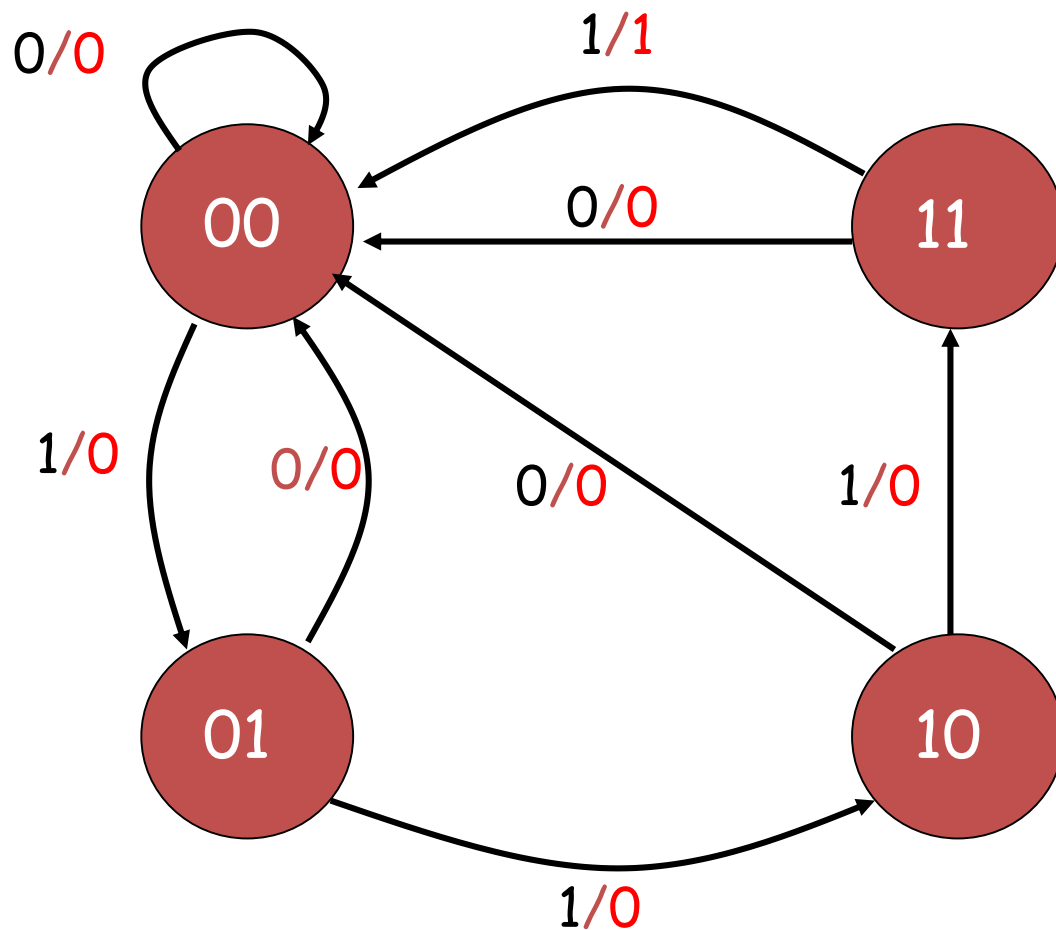
$y_2 = ?$

$z = ?$

Present State		Input	Next State		Output
y_1	y_2	x	y_1	y_2	z
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	0
0	1	1	1	0	0
1	0	0	0	0	0
1	0	1	1	1	0
1	1	0	0	0	0
1	1	1	0	0	1

There are 2^{m+n} rows in the state table of a synchronous sequential circuit with m FFs and n inputs.

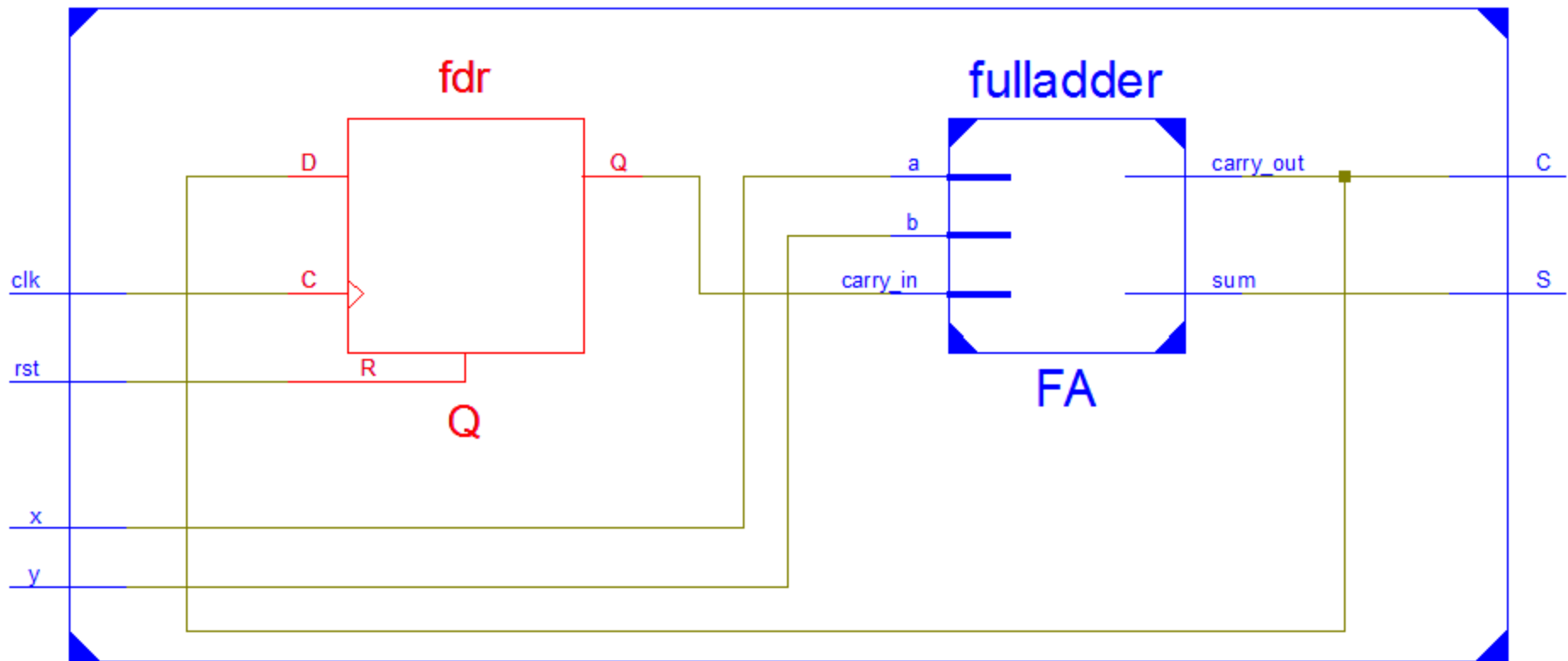
Example: State (Transition) Diagram



Current State		Input		Next State		Output
y_1	y_2	x		Y_1	Y_2	z
0	0	0	0	0	0	0
0	0	1	0	0	1	0
0	1	0	0	0	0	0
0	1	1	1	1	0	0
1	0	0	0	0	0	0
1	0	1	1	1	1	0
1	1	0	0	0	0	0
1	1	1	1	0	0	1

The state diagram and table give the same information

serial_adder:1

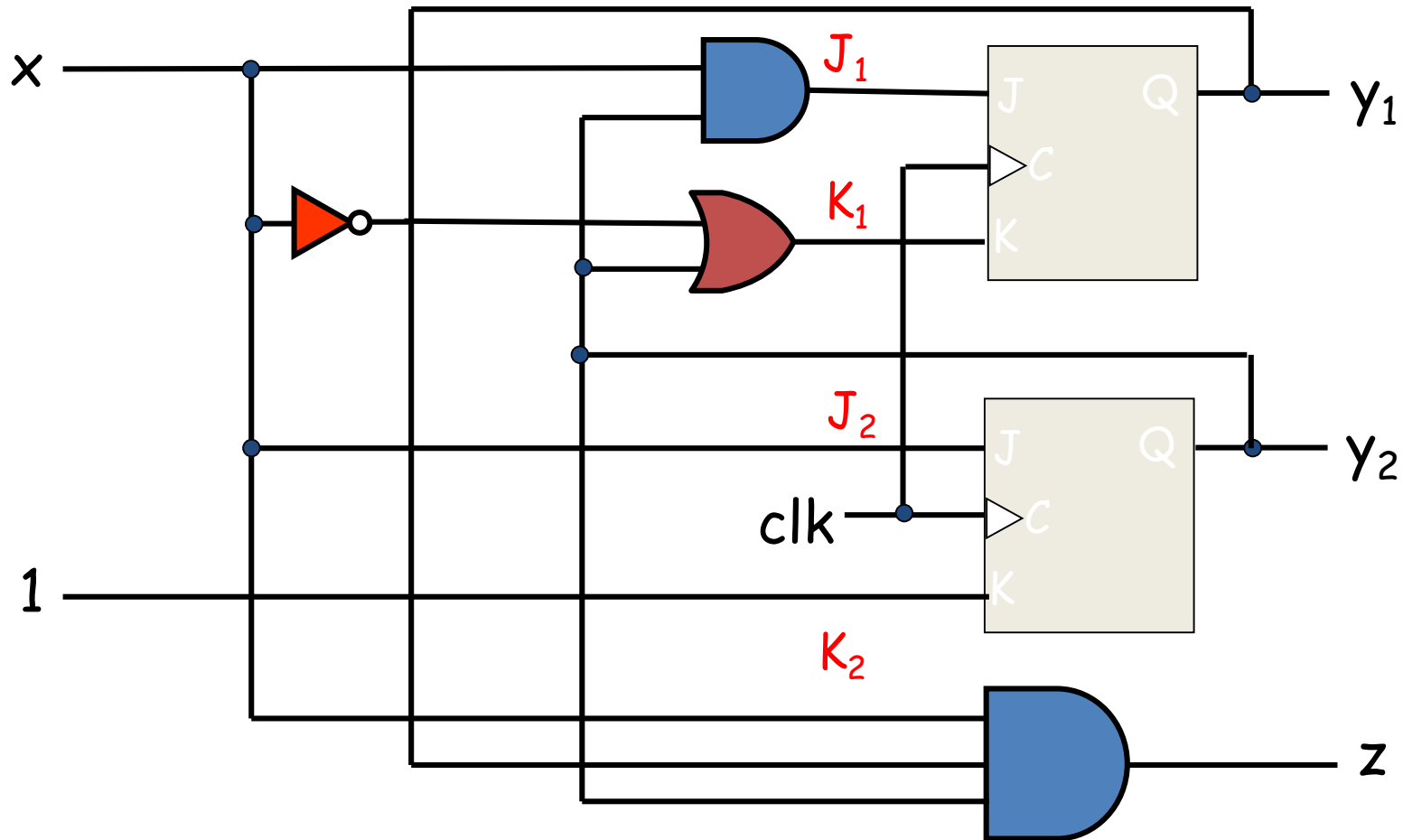


serial_adder

Analysis of a Synchronous Sequential Circuit with JK Flip-Flops

- For a D flip-flop, the state equation is the same as the flip-flop input equation
 - $Q(t+1) = D$
- For JK flip-flops, situation is different
 - Goal is to find state equations
 - Method
 1. determine flip-flop input equations
 2. List the binary values of each input equation
 3. Use the corresponding flip-flop characteristic table to determine the next state values in the state table

Example: Analysis with JK FFs



- Flip-flop input equations
 - $J_1 = xy_2$ and $K_1 = x' + y_2$
 - $J_2 = x$ and $K_2 = 1$

Example: Analysis with JK FFs

$$\begin{array}{ll} - J_1 = xy_2 & \text{and} \quad K_1 = x' + y_2 \\ - J_2 = x & \text{and} \quad K_2 = 1 \end{array}$$

present State		input	next state		FF inputs			
y_1	y_2	x	y_1	y_2	J_1	K_1	J_2	K_2
0	0	0	0	0	0	1	0	1
0	0	1	0	1	0	0	1	1
0	1	0	0	0	0	1	0	1
0	1	1	1	0	1	1	1	1
1	0	0	0	0	0	1	0	1
1	0	1	1	1	0	0	1	1
1	1	0	0	0	0	1	0	1
1	1	1	0	0	1	1	1	1

Example: Analysis with JK FFs

- Characteristic equations

- $Y_1 = J_1 y_1' + K_1' y_1$

- $Y_2 = J_2 y_2' + K_2' y_2$

- Flip-flop Input equations

- $J_1 = xy_2$ ve $K_1 = x' + y_2$

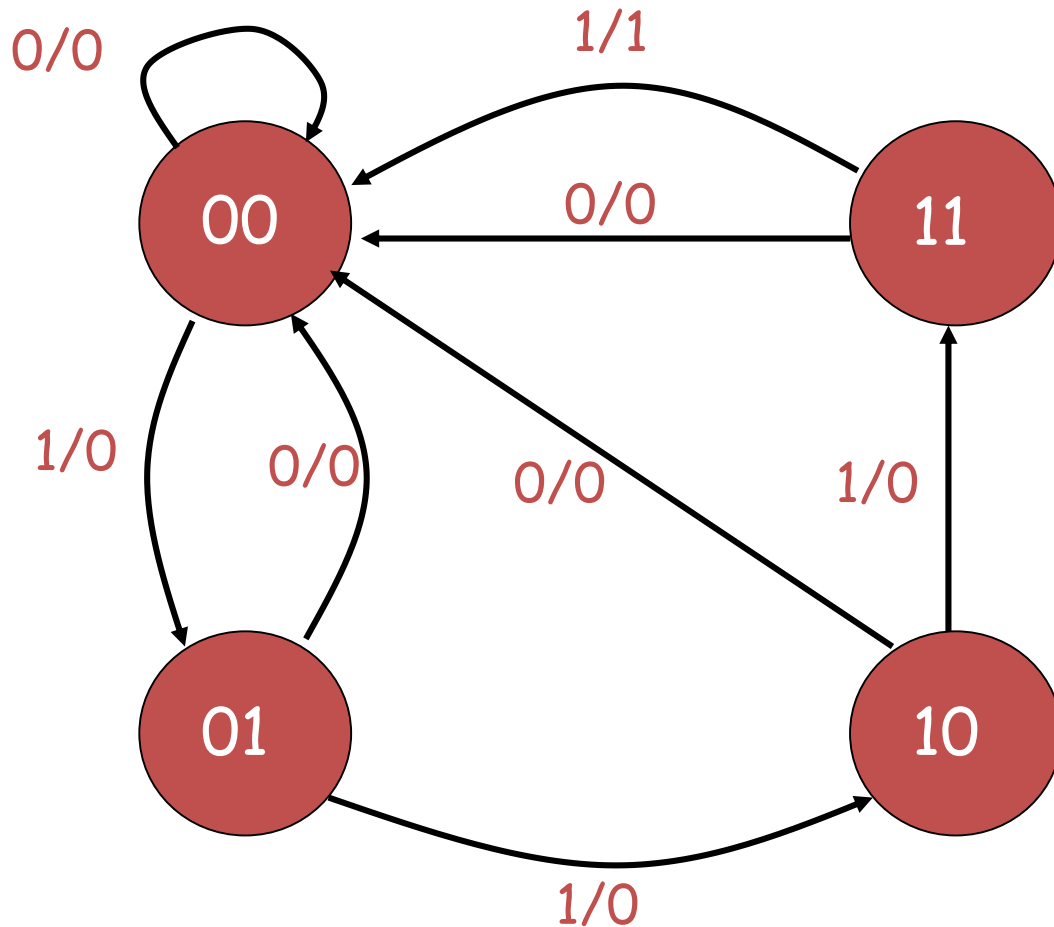
- $J_2 = x$ ve $K_2 = 1$

- State equations

- $Y_1 = xy_2 y_1' + (x' + y_2)' y_1 = xy_2 y_1' + xy_2' y_1 = x(y_2 \oplus y_1)$

- $Y_2 = xy_2' + 1' y_2 = xy_2'$

State Diagram



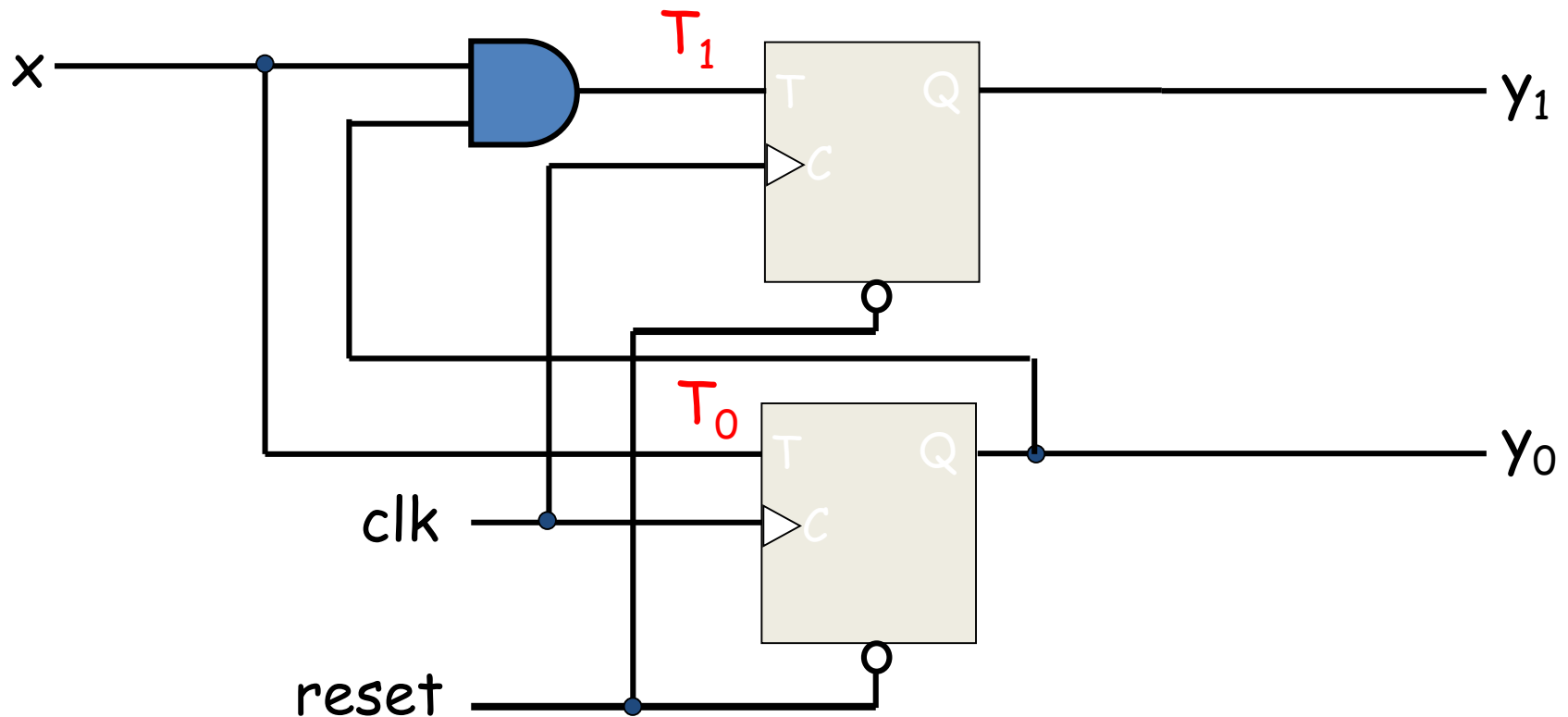
Present state		Input	Next State		Output
y_1	y_2	x	Y_1	Y_2	z
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	0
0	1	1	1	0	0
1	0	0	0	0	0
1	0	1	1	1	0
1	1	0	0	0	0
1	1	1	0	0	1

What is the circuit doing?

Analysis with T Flip-Flops

- Method is the same
- Example

$$T_1 = xy_0$$
$$T_0 = x$$



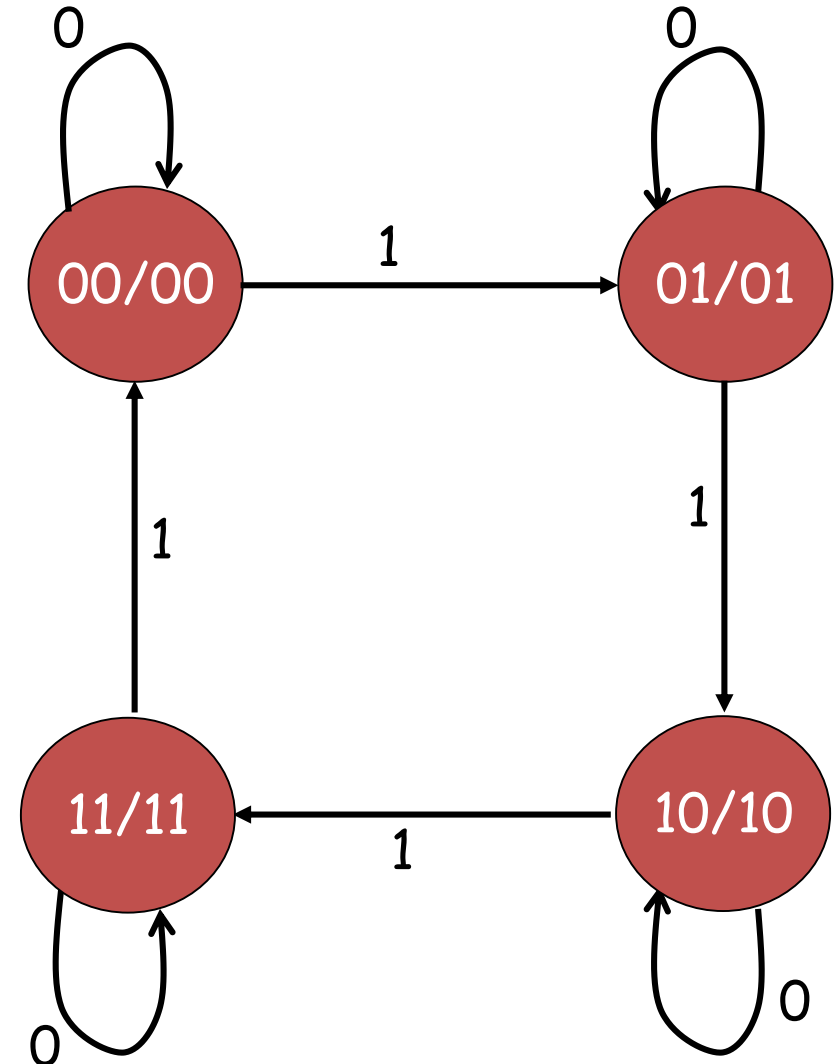
Example: Analysis with T Flip-Flops

- Characteristic equation
 - $Y_0 = T_0 \oplus y_0$
 - $Y_1 = T_1 \oplus y_1$
- Flip-flop Input equations
 - $T_1 = x y_0$
 - $T_0 = x$
- State equations
 - $Y_0 = x \oplus y_0$
 - $Y_1 = x y_0 \oplus y_1$

State Table & Diagram

- $Y_0 = x \oplus y_0$
- $Y_1 = x y_0 \oplus y_1$

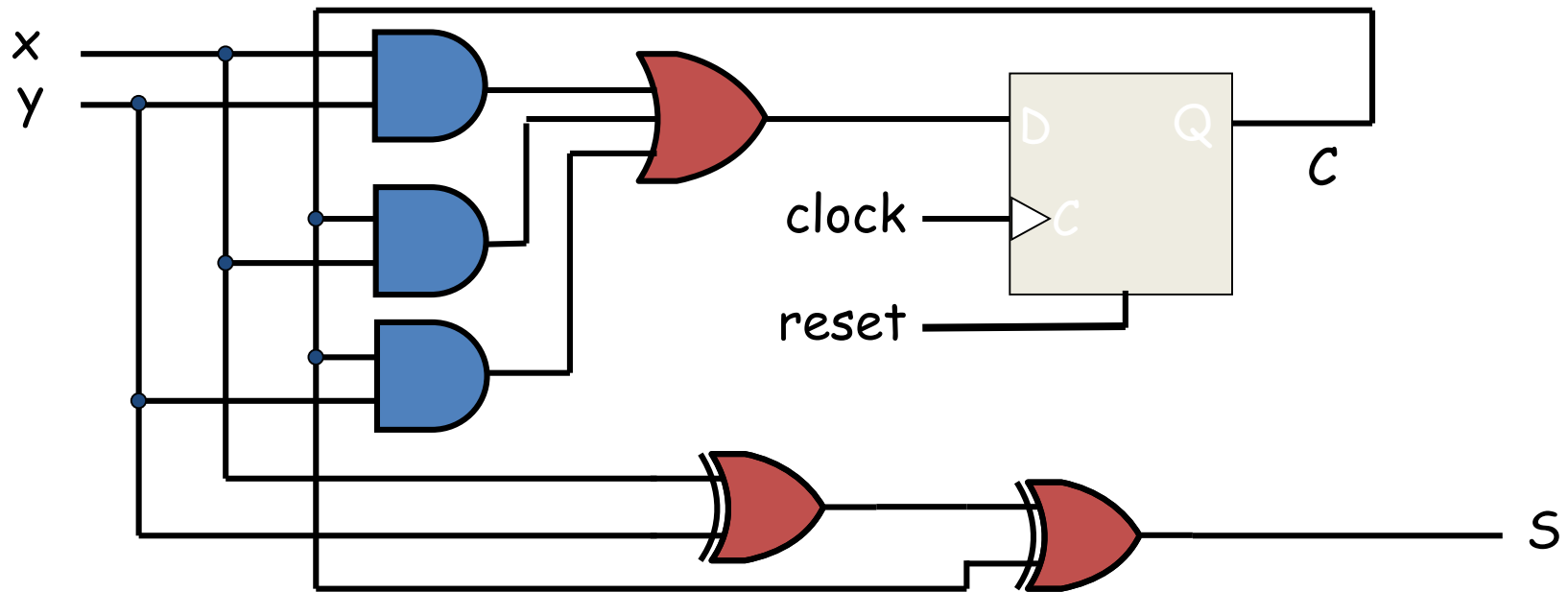
Present State		Input	Next State		Output	
y_1	y_0		Y_1	Y_0	y_1	y_0
0	0	0	0	0	0	0
0	0	1	0	1	0	0
0	1	0	0	1	0	1
0	1	1	1	0	0	1
1	0	0	1	0	1	0
1	0	1	1	1	1	0
1	1	0	1	1	1	1
1	1	1	0	0	1	1



Mealy and Moore Models

- There are two models for sequential circuits
 - Mealy
 - Moore
- They differ in the way the outputs are generated
 - Mealy:
 - output is a function of both present states and inputs
 - Moore
 - output is a function of present state only

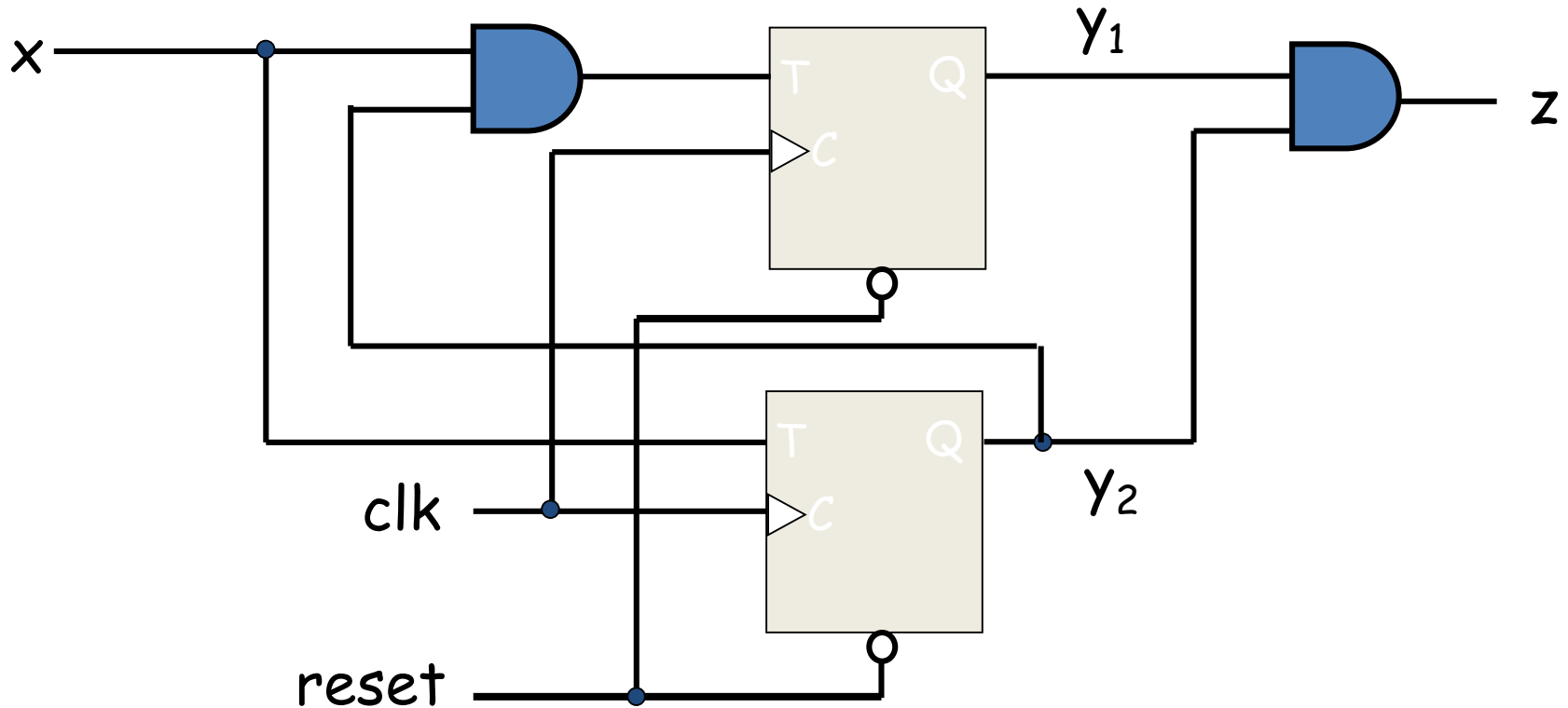
Example: Mealy and Moore Machines



Mealy Machine

- External inputs, x and y , are asynchronous
- Thus, outputs may have momentary (incorrect) values
- Inputs must be synchronized with clocks
- Outputs must be sampled only during clock edges.

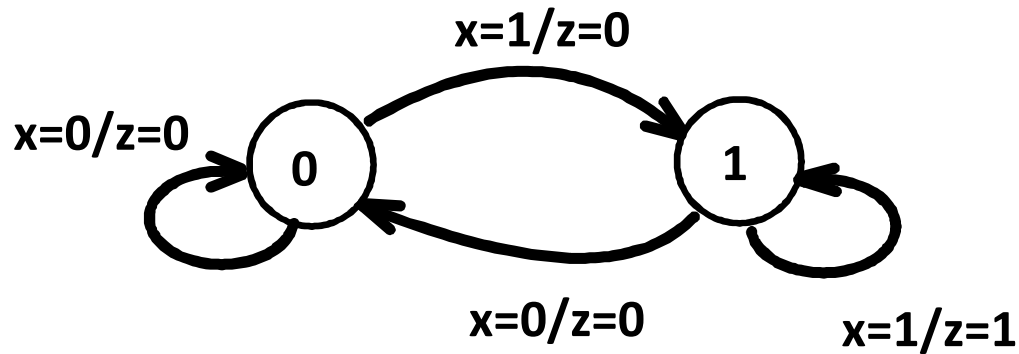
Example: Moore Machines



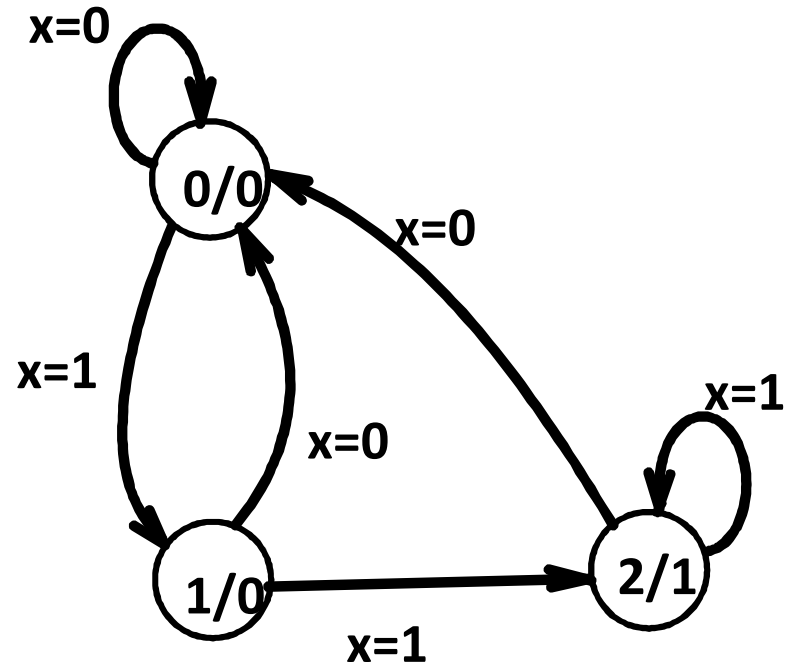
- Outputs are already synchronized with clock.
- They change synchronously with the clock edge.

Example State Diagrams for Moore and Mealy Machines

- State Diagram for Mealy Model



- State Diagram for Moore Model



Design Process

1. Verbal description of desired operation
2. Draw the state diagram
3. Reduce the number of states if necessary and possible: s = number of states
4. Determine the number of flip-flops: $n = \lceil \log_2 s \rceil$
5. State assignment: $\underbrace{00\dots0}_{n\text{-bits}}, \underbrace{00\dots1}_{n\text{-bits}}, \underbrace{00\dots10}_{n\text{-bits}}, \dots$
6. Obtain the **encoded** state table
7. Choose the type of the flip-flops
8. Derive the **simplified flip-flop input equations**
9. Derive the **simplified output equations**
10. Draw the logic diagram

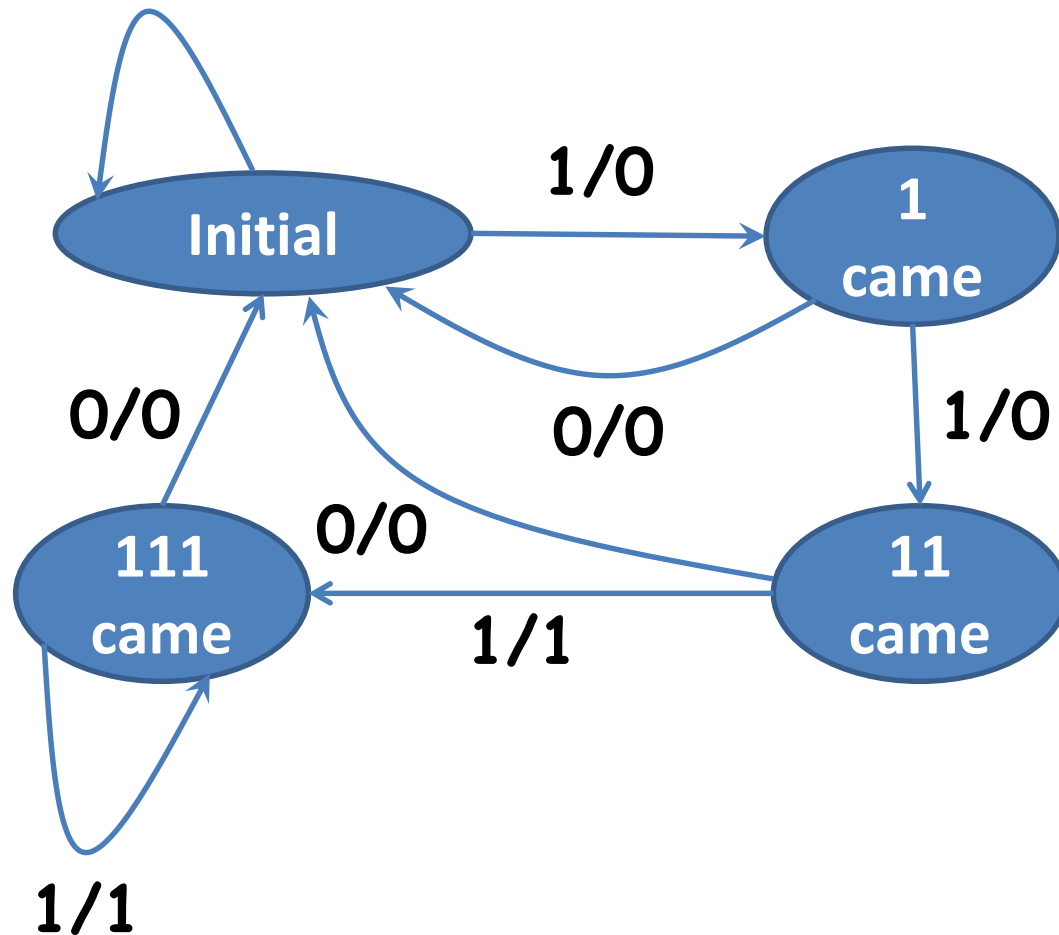
Example: Design of a Synchronous Sequential Circuit

- Verbal description
 - **1st Step:** we want a circuit that detects three or more consecutive 1's in a string of bits.
 - Input: string of bits of any length
 - Output:
 - “1” if the circuit detects such a pattern in the string
 - “0” otherwise

Example: State Diagram

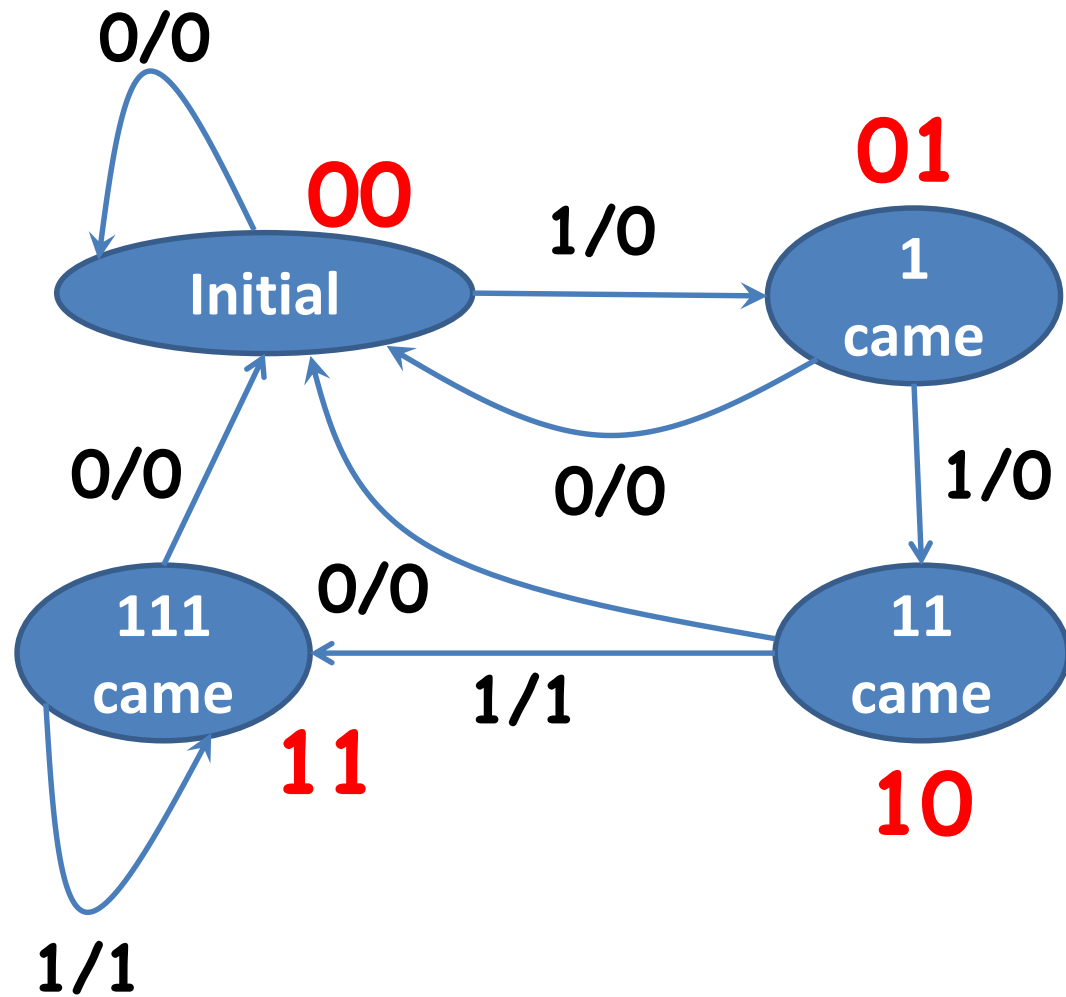
2nd Step: Draw the state diagram

0/0



Synthesis with D Flip-Flops 1/5

- **3rd Step:** State reduction
 - Not possible
- **4th Step:** Number of flip-flops
 - 4 states
 - ? flip-flop
- **5th Step:** State assignment



Synthesis with D Flip-Flops 2/5

- **6th Step:** Obtain the state table

Present State		Input	Next State		Output
Y_1	Y_2	x	Y_1	Y_2	z
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	0
0	1	1	1	0	0
1	0	0	0	0	0
1	0	1	1	1	0
1	1	0	0	0	1
1	1	1	1	1	1

Synthesis with D Flip-Flops 3/5

- **7th Step:** Choose the type of the flip-flops
 - D type flip-flops
- **8th Step:** : Derive the simplified flip-flop input equations
 - Boolean expressions for D_1 and D_2

y_2x y_1					
		00	01	11	10
0	0	0	1	0	
1	0	1	1	0	

$$D_1 = y_1x + y_2x$$

y_2x y_1					
		00	01	11	10
0	0	1	0	0	
1	0	1	1	0	

$$D_2 = y_1x + y_2'x$$

Synthesis with D Flip-Flops 4/5

- **9th Step:** : Derive the simplified output equations
 - Boolean expressions for z

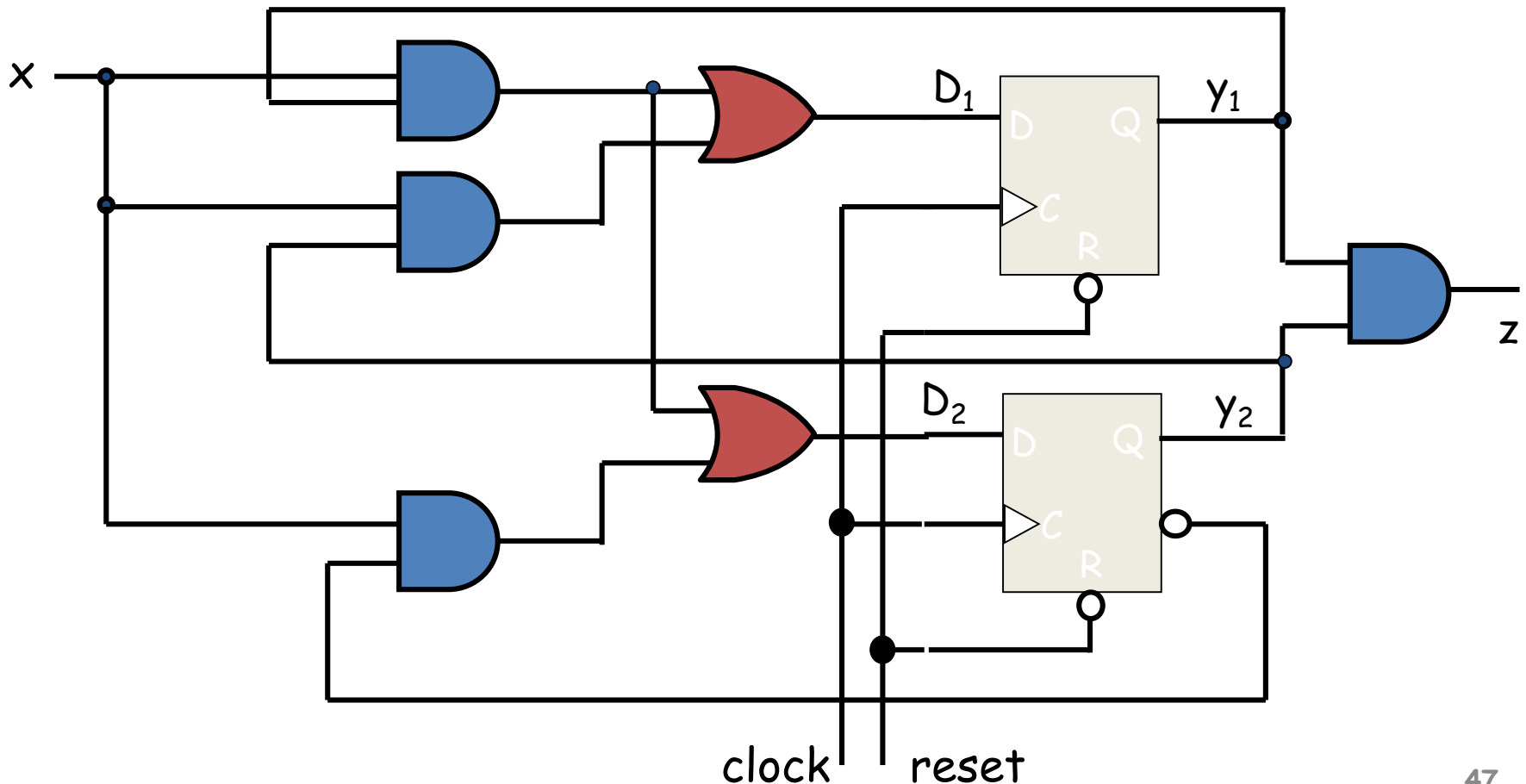
$y_2 \backslash y_1$		x			
		00	01	11	10
0	0	0	0	0	0
1	0	0	1	1	

$$z = y_1 y_2$$

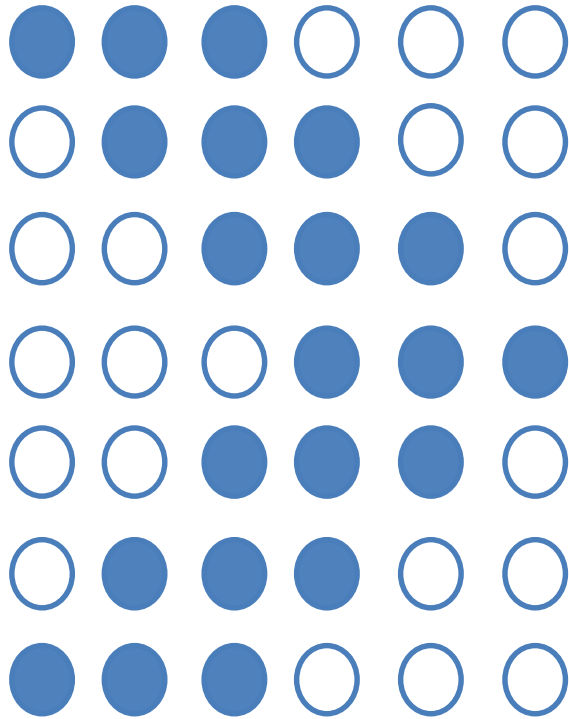
Synthesis with D Flip-Flops 5/5

- **10th Step:** Draw the logic diagram

$$D_1 = y_1x + y_2x \quad D_2 = y_1x + y_2'x \quad z = y_1y_2$$



Synthesis with JK Flip-Flops and MUXs



Number of states= 6

Number of state variables= 3

Number of flip-flops= 3

Number of Inputs= 0

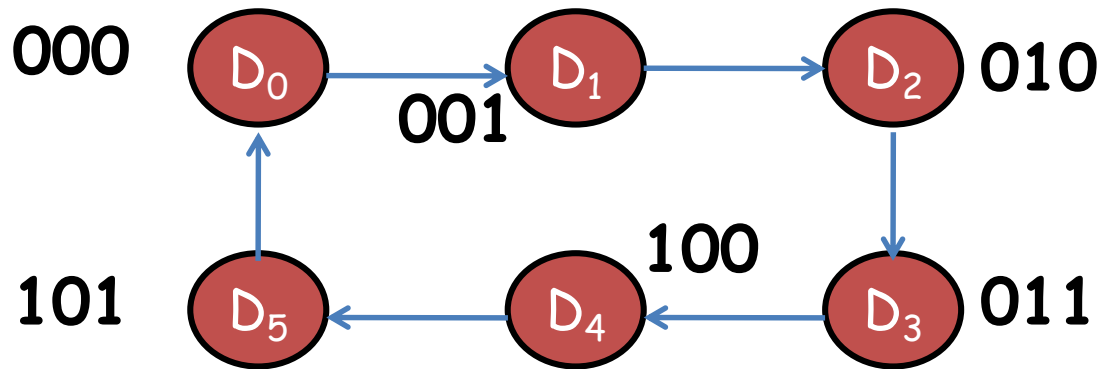
Number of Outputs= 6

- 6 shifting lights

- ● = logic-1

- ○ = logic-0

State Diagram & Table



$$Y = Jy' + K'y$$

J	K	Y
0	0	y
0	1	0
1	0	1
1	1	Q'

Present State			Next State			Flip-flop inputs						Outputs					
Y ₂	Y ₁	Y ₀	Y ₂	Y ₁	Y ₀	J ₂	K ₂	J ₁	K ₁	J ₀	K ₀	z ₅	z ₄	z ₃	z ₂	z ₁	z ₀
0	0	0	0	0	1	0	k	0	k	1	k	1	1	1	0	0	0
0	0	1	0	1	0	0	k	1	k	k	1	0	1	1	1	0	0
0	1	0	0	1	1	0	k	k	0	1	k	0	0	1	1	1	0
0	1	1	1	0	0	1	k	k	1	k	1	0	0	0	1	1	1
1	0	0	1	0	1	k	0	0	k	1	k	0	0	1	1	1	0
1	0	1	0	0	0	k	1	0	k	k	1	0	1	1	1	0	0

Implementation of Flip-Flop Input Equations

		y_1y_0			
		00	01	11	10
y_2	0	0	0	0	1
	1	k	k	k	k

$$J_2 = y_1y_0'$$

		$J_2 - y_1y_0$			
		y_1y_0	00	01	11
y_2	0	0	1	k	k
	1	0	0	k	k

$$J_1 = y_2'y_0$$

		$J_1 = y_2' y_0$			
		$y_1 y_0$	00	01	11
y_2	0	1	k	k	1
	1	1	k	k	k

$$J_0 = 1$$

		y_1y_0			
		00	01	11	10
y_2	0	k	k	k	k
	1	0	1	k	k

$$K_2 = y_0$$

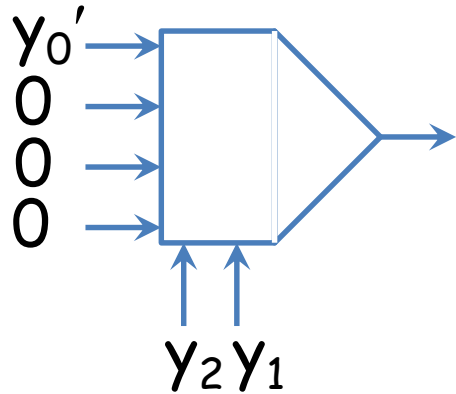
		$K_2 = y_0$			
		y_1y_0	00	01	11
y_2	0	k	k	1	0
	1	k	k	k	k

$$K_1 = y_0$$

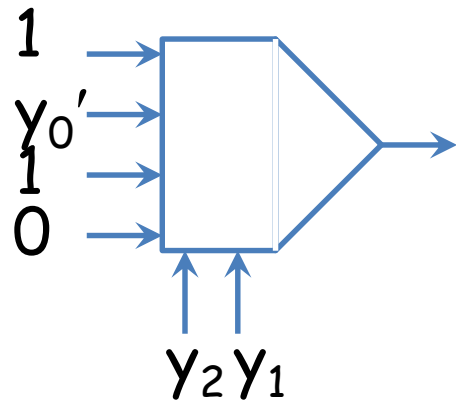
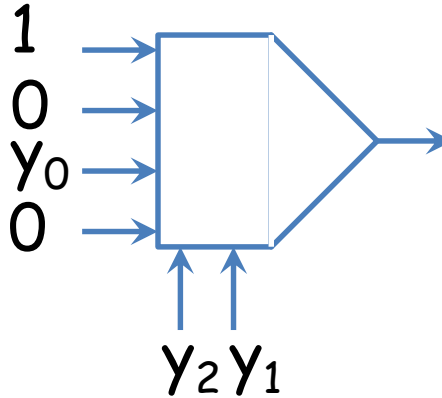
y_1y_0		$K_1 = y_0$			
		00	01	11	10
y_2	0	k	1	1	k
	1	k	1	k	k

$$K_0 = 1$$

Implementation of Output Equations

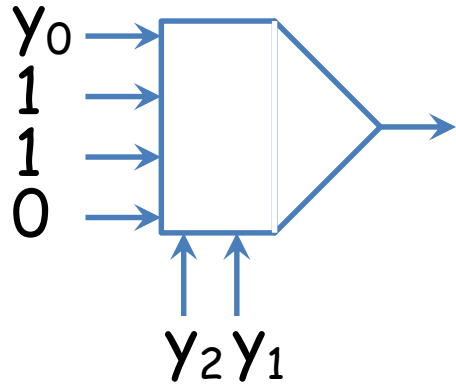


$$z_5 = y_2' y_1' y_0' + k(y_2 y_1 y_0' + y_2 y_1 y_0) \quad z_4 = y_2' y_1' y_0' + y_2' y_1' y_0 + y_2 y_1' y_0 + k(y_2 y_1 y_0' + y_2 y_1 y_0)$$

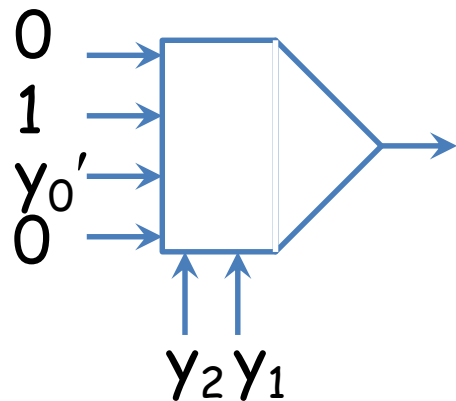


$$z_3 = y_2' y_1' y_0' + y_2' y_1' y_0 + y_2' y_1 y_0' + y_2 y_1' y_0' + y_2 y_1' y_0 + k(y_2 y_1 y_0' + y_2 y_1 y_0)$$

Implementation of Output Equations

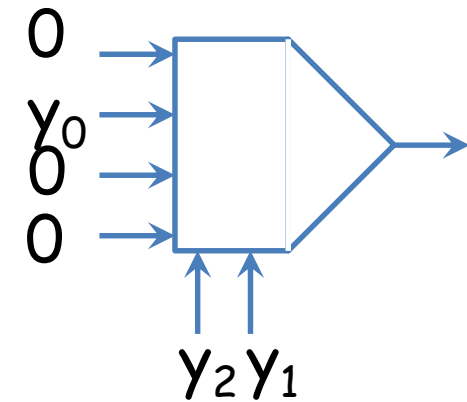


$$z_2 = y_2' y_1' y_0 + y_2' y_1 y_0' + y_2' y_1 y_0 + y_2 y_1' y_0' + y_2 y_1' y_0 + k(y_2 y_1 y_0' + y_2 y_1 y_0)$$



$$z_1 = y_2' y_1 y_0' + y_2' y_1 y_0 + y_2 y_1' y_0' + k(y_2 y_1 y_0' + y_2 y_1 y_0)$$

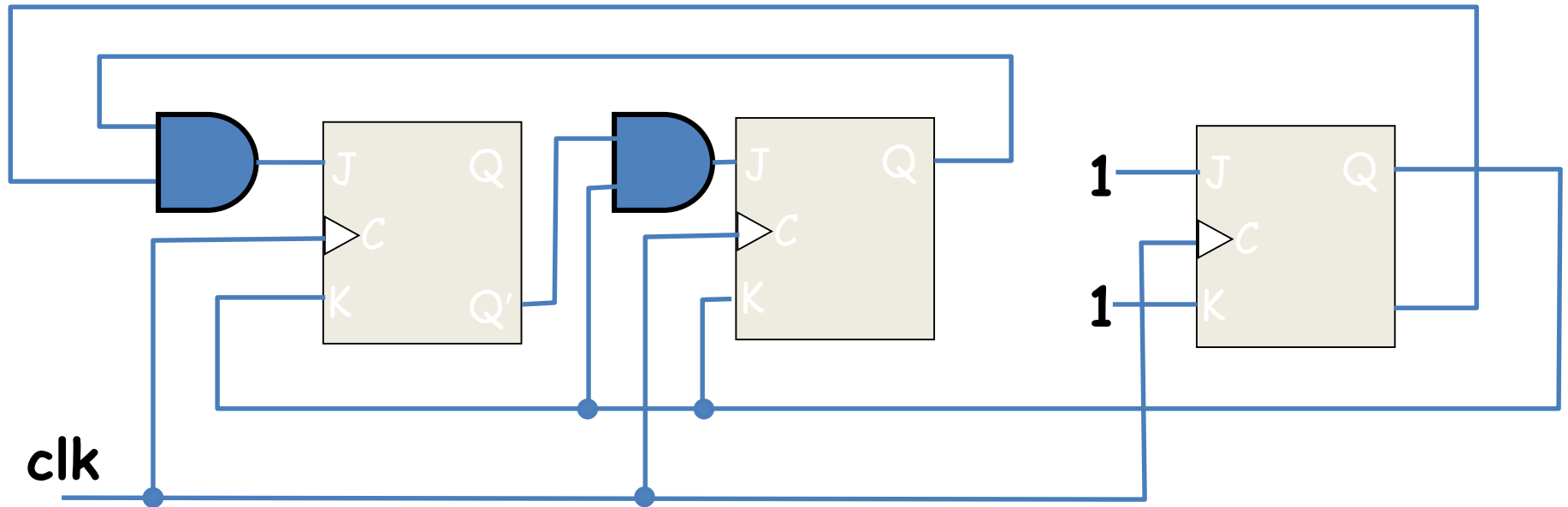
Implementation of Output Equations



$$z_0 = y_2' y_1 y_0 + k(y_2 y_1 y_0' + y_2 y_1 y_0)$$

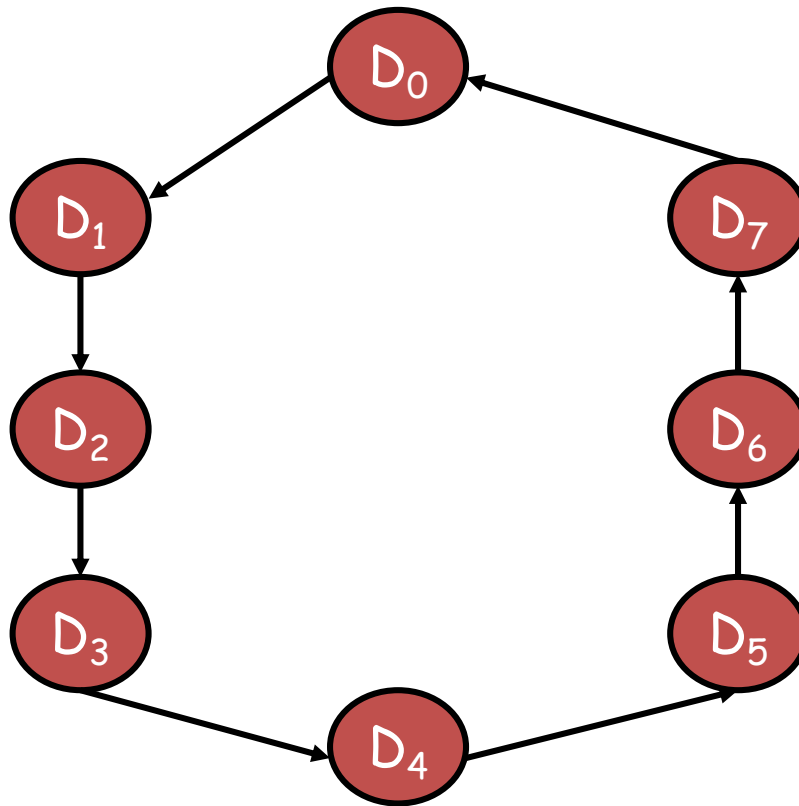
Logic Diagram

$$J_2 = y_1 y_0' \quad K_2 = y_0 \quad J_1 = y_2' y_0 \quad K_1 = y_0 \quad J_0 = 1 \quad K_1 = 1$$



Synthesis with T Flip-Flops 1/4

- Example: 3-bit binary counter
 $0 \rightarrow 1 \rightarrow 2 \rightarrow \dots \rightarrow 7 \rightarrow 0 \rightarrow 1 \rightarrow 2$



State Diagram

How many flip-flops?

State assignments

- $D_0 \rightarrow 000$
- $D_1 \rightarrow 001$
- $D_2 \rightarrow 010$
- \dots
- $D_7 \rightarrow 111$

Synthesis with T Flip-Flops 2/4

- State Table

present state			next state			FF inputs		
y_2	y_1	y_0	Y_2	Y_1	Y_0	T_2	T_1	T_0
0	0	0	0	0	1	0	0	1
0	0	1	0	1	0	0	1	1
0	1	0	0	1	1	0	0	1
0	1	1	1	0	0	1	1	1
1	0	0	1	0	1	0	0	1
1	0	1	1	1	0	0	1	1
1	1	0	1	1	1	0	0	1
1	1	1	0	0	0	1	1	1

Synthesis with T Flip-Flops 3/4

- Flip-Flop input equations

		$y_1 y_0$			
		00	01	11	10
y_2	0	0	0	1	0
	1	0	0	1	0

$$T_2 = y_1 y_0$$

$$T_0 = 1$$

		$y_1 y_0$			
		00	01	11	10
y_2	0	0	1	1	0
	1	0	1	1	0

$$T_1 = y_0$$

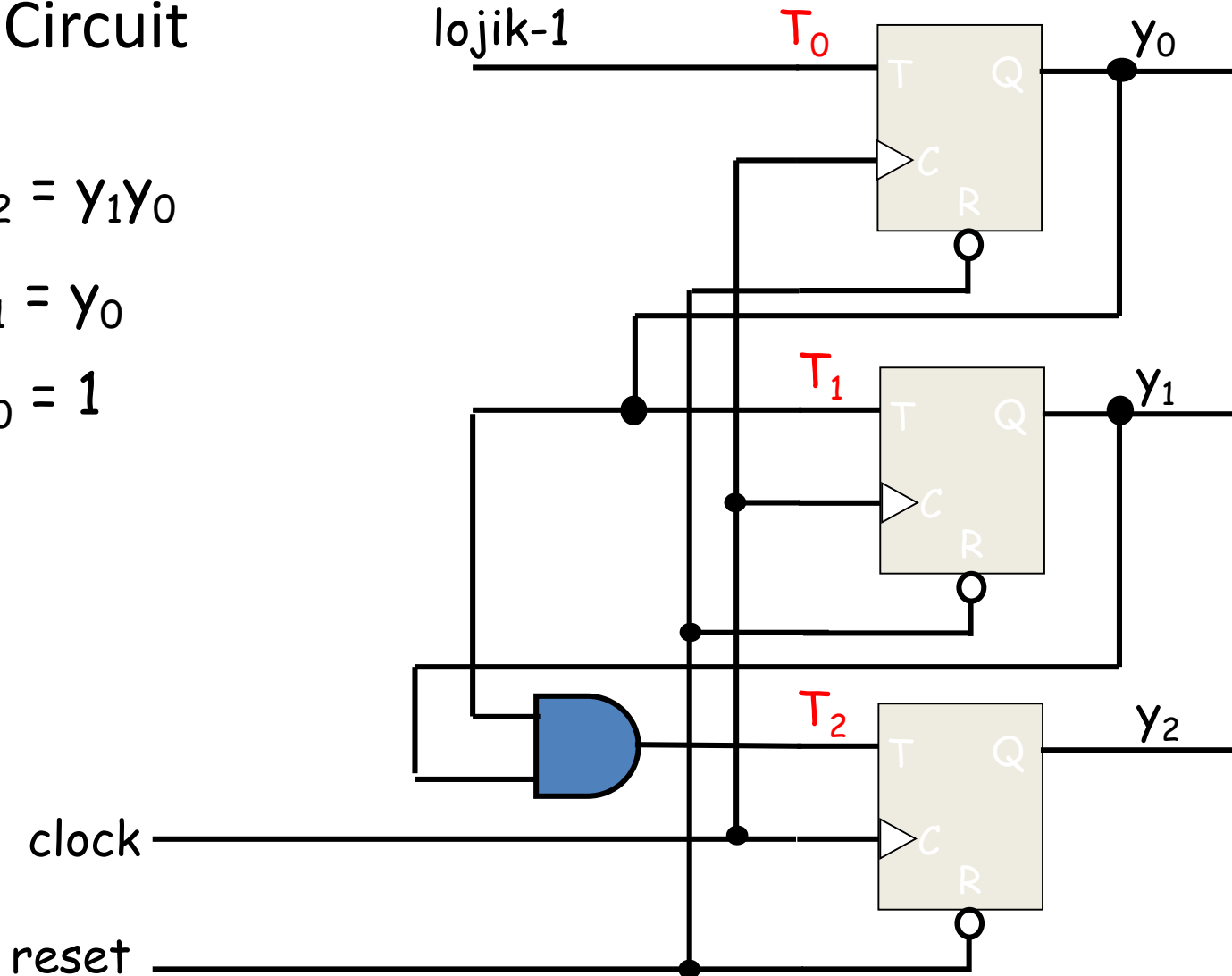
Synthesis with T Flip-Flops 4/4

- Circuit

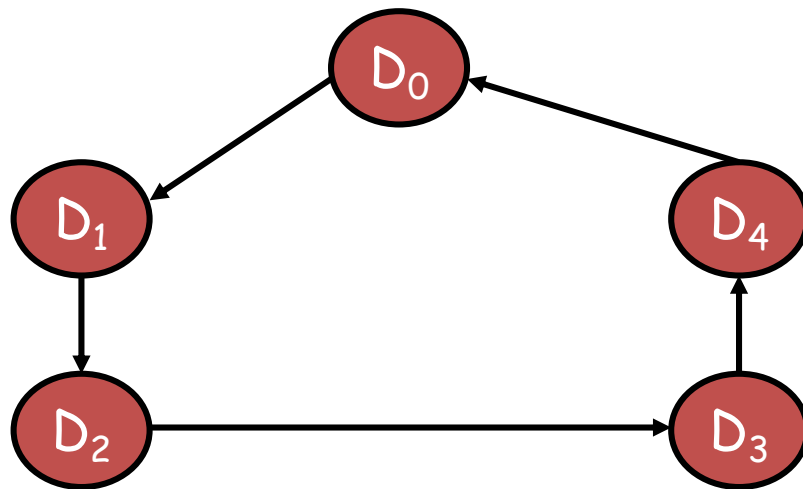
$$T_2 = y_1 y_0$$

$$T_1 = y_0$$

$$T_0 = 1$$



Unused States



Modulo-5 counter

Present State			Next State		
Y_2	Y_1	Y_0	Y_2	Y_1	Y_0
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	0	0

Example: Unused States 1/4

Present State			Next State		
y_2	y_1	y_0	Y_2	Y_1	Y_0
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	0	0

$y_1 y_0$		00	01	11	10
y_2					
0		0	0	1	0
1		0	X	X	X

$$Y_2 = y_1 y_0$$

$y_1 y_0$		00	01	11	10
y_2					
0		0	1	0	1
1		0	X	X	X

$$\begin{aligned}
 Y_1 &= y_1' y_0 + y_1 y_0' \\
 &= y_1 \oplus y_0
 \end{aligned}$$

$y_1 y_0$		00	01	11	10
y_2					
0		1	0	0	1
1		0	X	X	X

$$Y_0 = y_2' y_0'$$

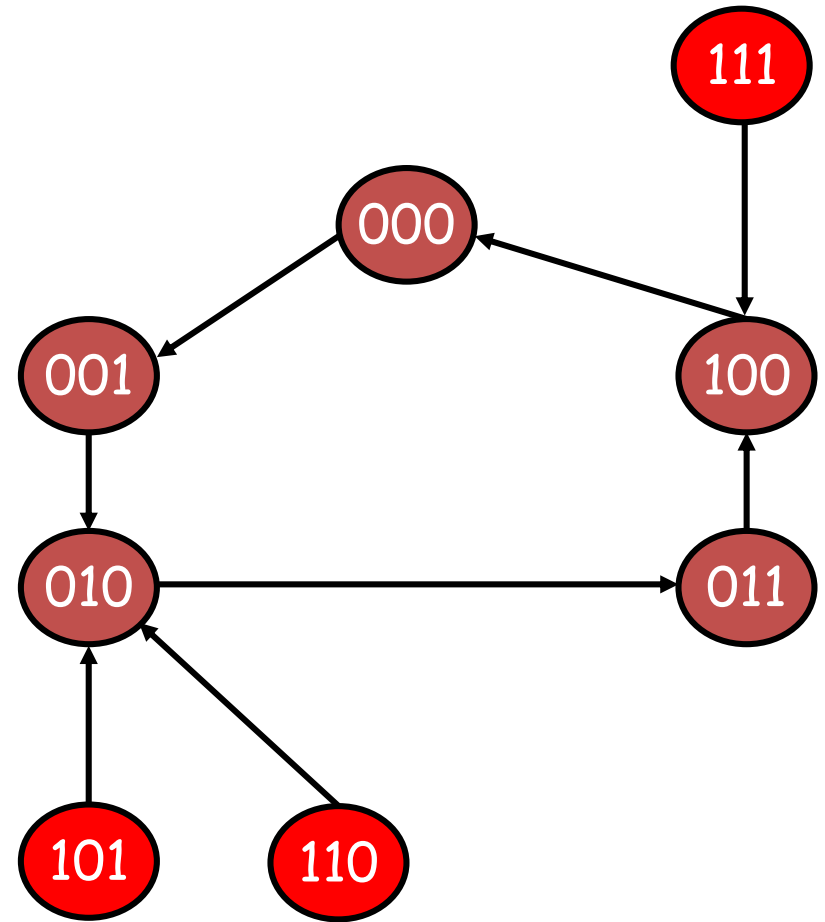
Example: Unused States 2/4

Present State			Next State		
Y_2	Y_1	Y_0	Y_2	Y_1	Y_0
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	0	0
1	0	1	0	1	0
1	1	0	0	1	0
1	1	1	1	0	0

$$Y_2 = Y_1 Y_0$$

$$Y_1 = Y_1 \oplus Y_0$$

$$Y_0 = Y_2' Y_0'$$



The circuit is not locked type.

Example: Unused States 3/4

- Not using don't care conditions

Present State			Next State		
A	B	C	A	B	C
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	0	0

A	BC			
	00	01	11	10
0	0	1	0	1
1	0	0	0	0

$$B(t+1) = A'B'C + A'BC'$$

$$= A'(B \oplus C)$$

A	BC			
	00	01	11	10
0	0	0	1	0
1	0	0	0	0

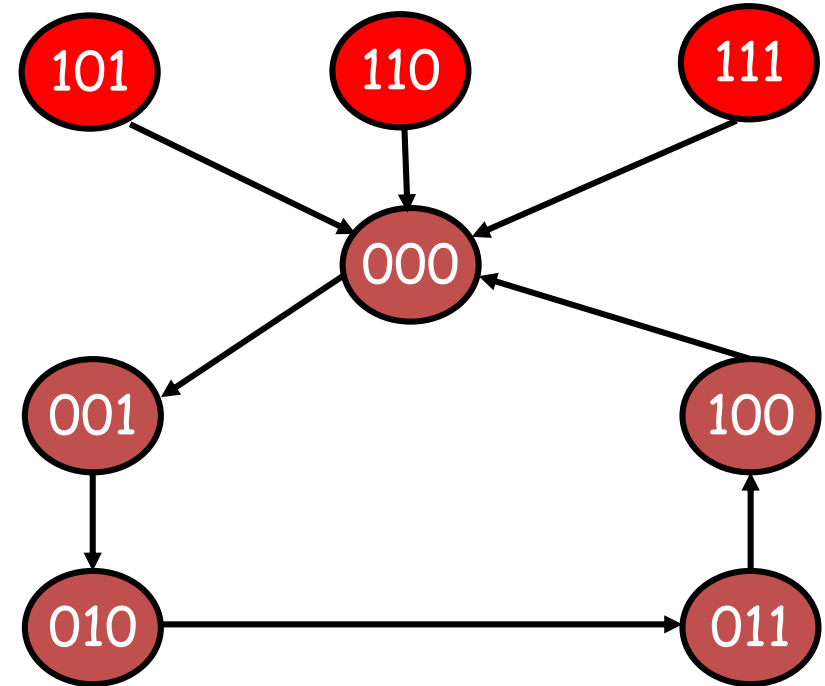
$$A(t+1) = A'BC$$

A	BC			
	00	01	11	10
0	1	0	0	1
1	0	0	0	0

$$C(t+1) = A'C'$$

Example: Unused States 4/4

Present State			Next State		
A	B	C	A	B	C
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	0	0



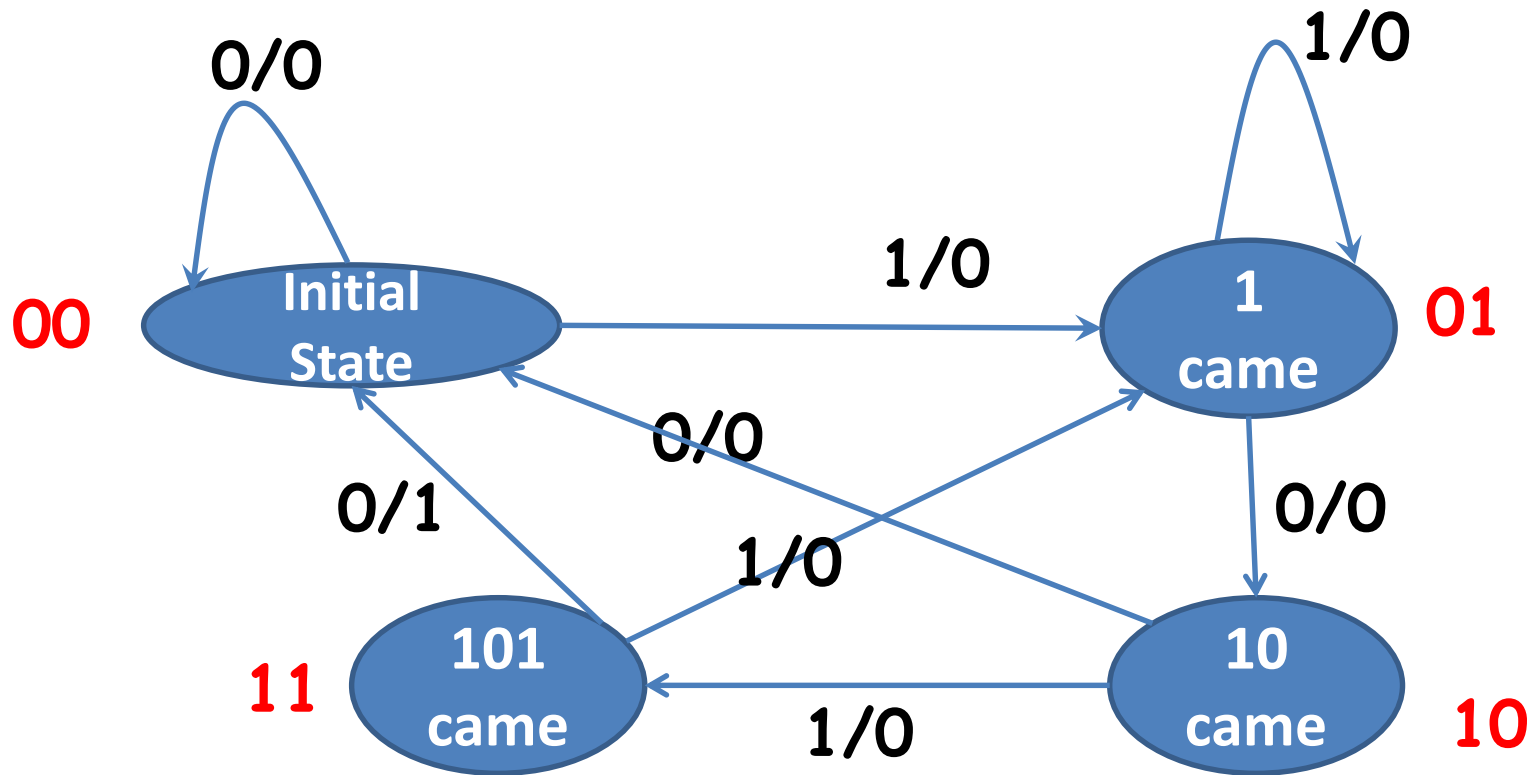
$$A(t+1) = A'BC$$

$$B(t+1) = A'(B \oplus C)$$

$$C(t+1) = A'C'$$

Design Example

- Design the synchronous sequential circuit which gives “1” as output when the last 4 values from the 1-bit input are 1010.
- Example: $x = \underline{1010} \underline{1011}$ ise $z = 0001 \ 0000$



Mealy Machine

State Table

Present State		Input	Next State		Output
y_1	y_2	x	y_1	y_2	z
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	1	0	0
0	1	1	0	1	0
1	0	0	0	0	0
1	0	1	1	1	0
1	1	0	0	0	1
1	1	1	0	1	0

Verilog Code

```
module MealyMachine(x,y,clk,rst);
    input x,clk,rst;
    output y;

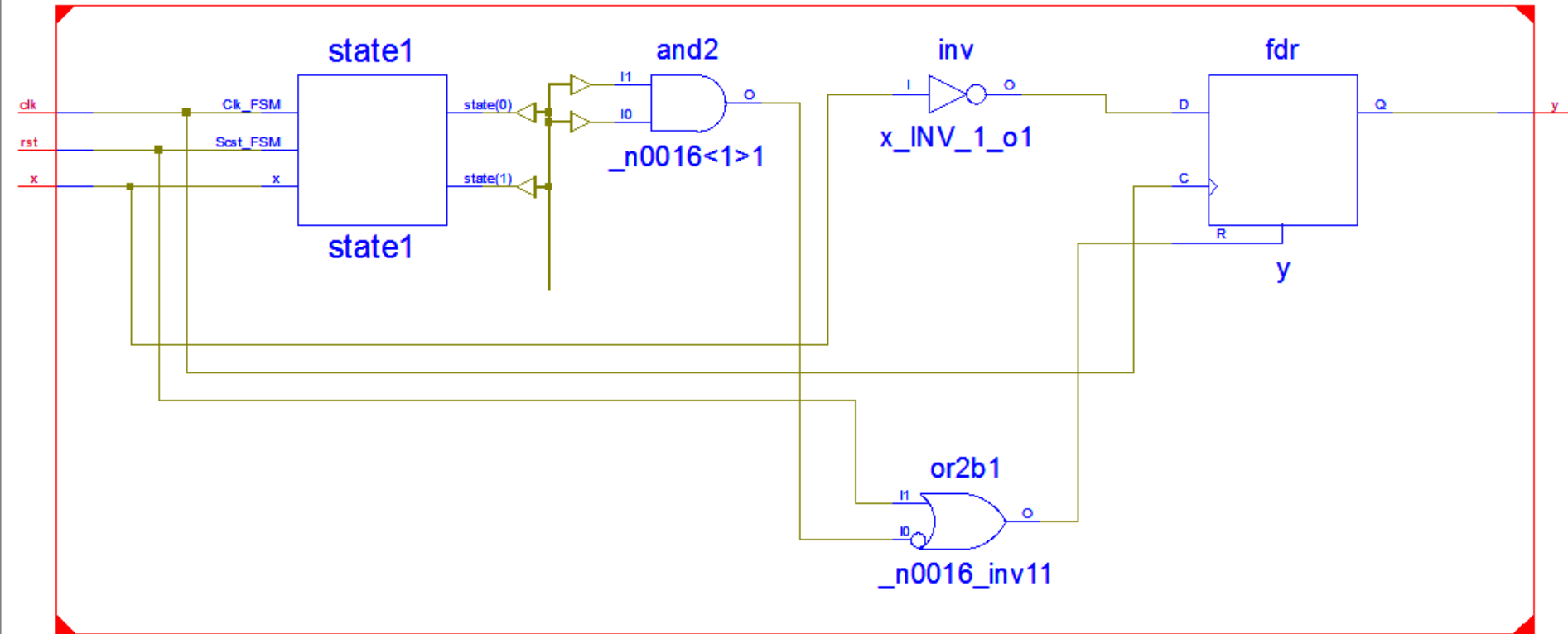
    parameter IS=0, S_1=1, S_10=2, S_101=3;

    reg [1:0] state;
    reg y;

    always @(posedge clk) begin
        if (rst) state = IS; y = 0;
        end else
            case (state)
                IS: begin
                    y = 0;
                    if(x) state = S_1;
                    else state = IS;
                end
                S_1: begin
                    y = 0;
                    if(x) state = S_1;
                    else state = S_10;
                end
                S_10: begin
                    y = 0;
                    if(x) state = S_101;
                    else state = IS;
                end
                S_101: begin
                    if(x) begin
                        state = S_1; y =0;
                    end else begin
                        state = IS; y =1;
                    end
                end
            endcase
        end
    end
endmodule
```

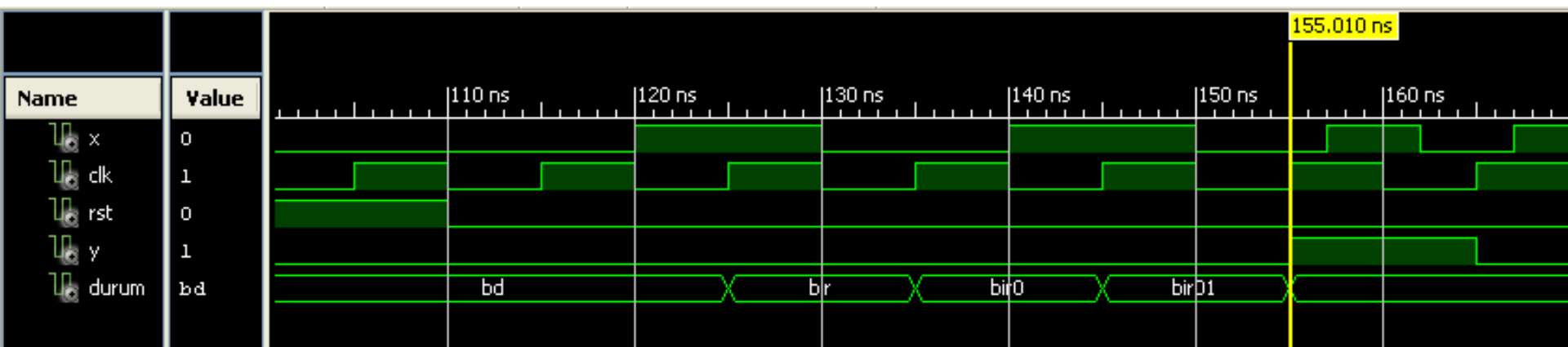
RTL Schematic

MealyMachine:1

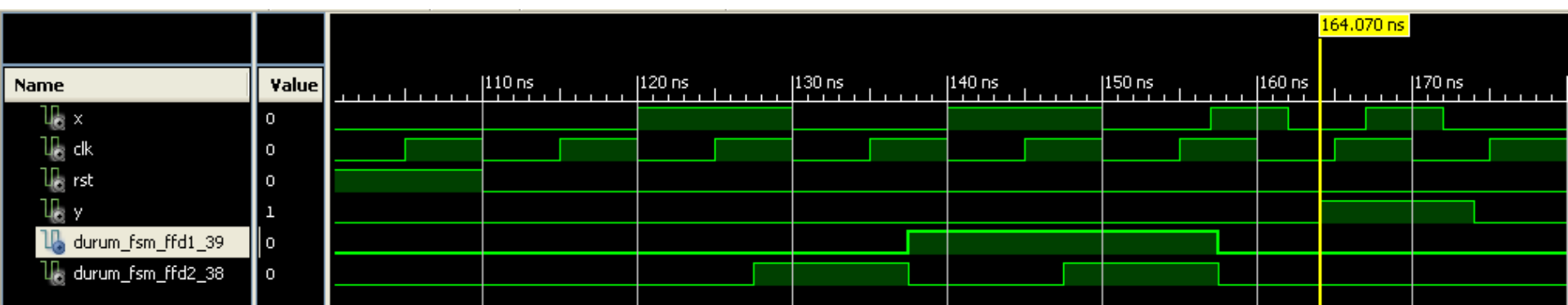


MealyMachine

Timing Diagram

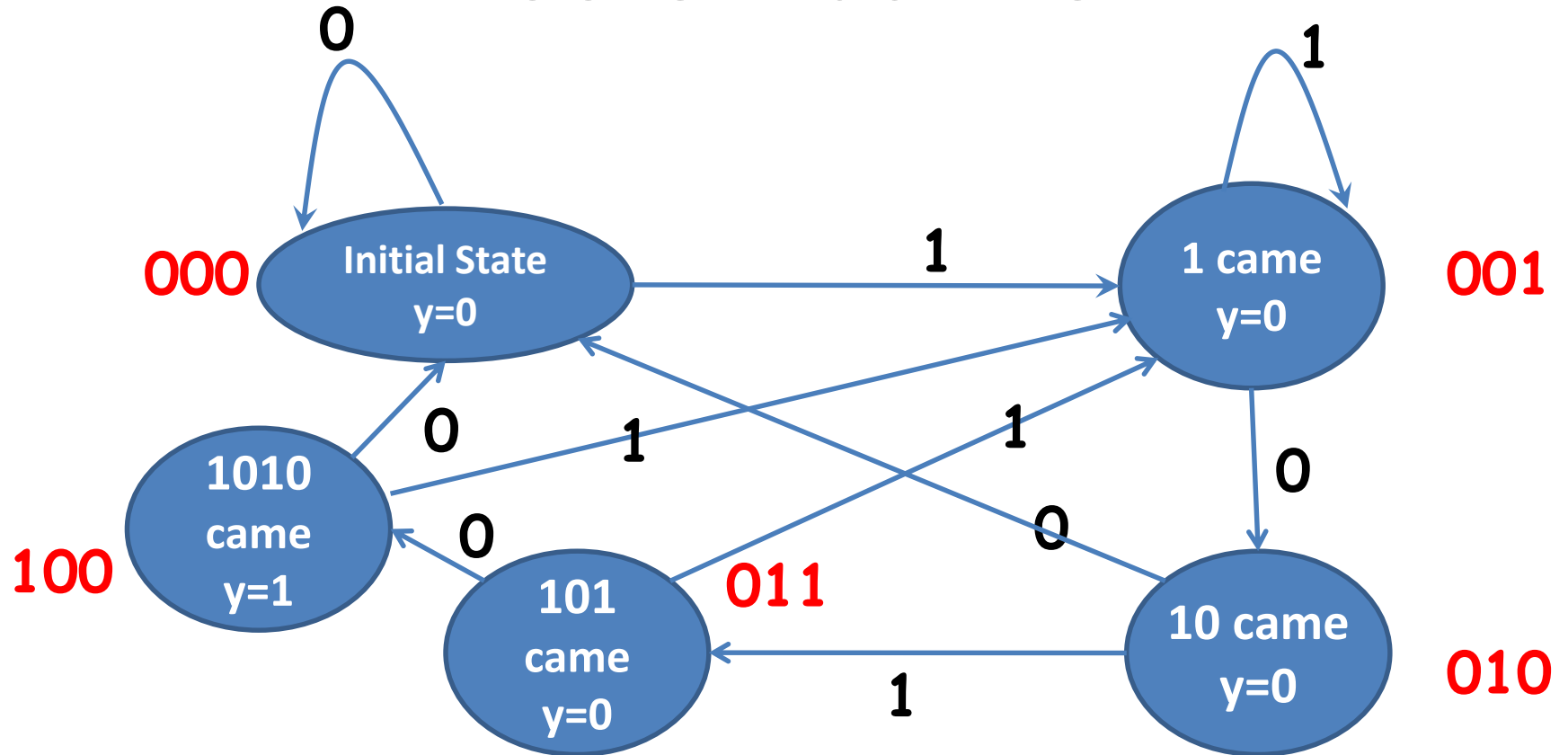


Ideal Case: Delay = 0



Not Ideal Case: Delay $\neq 0$

Moore Machine



Verilog Code

```
module
    MealyMachine(x,y,clk
    ,rst);

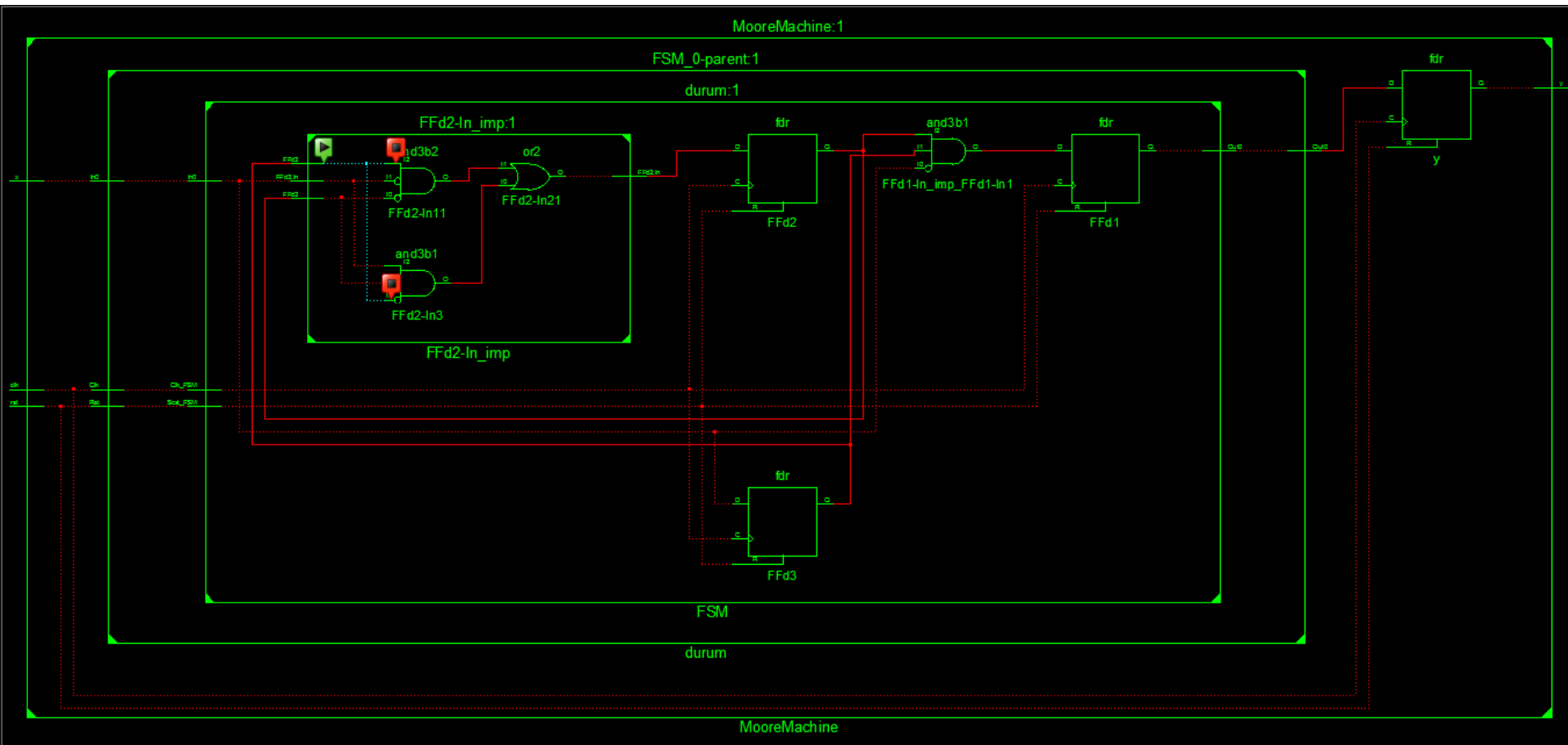
    Input x,clk,rst;
    output y;

    Parameter IS=0, S_1=1,
        S_10=2, S_101=3,
        S_1010=4;

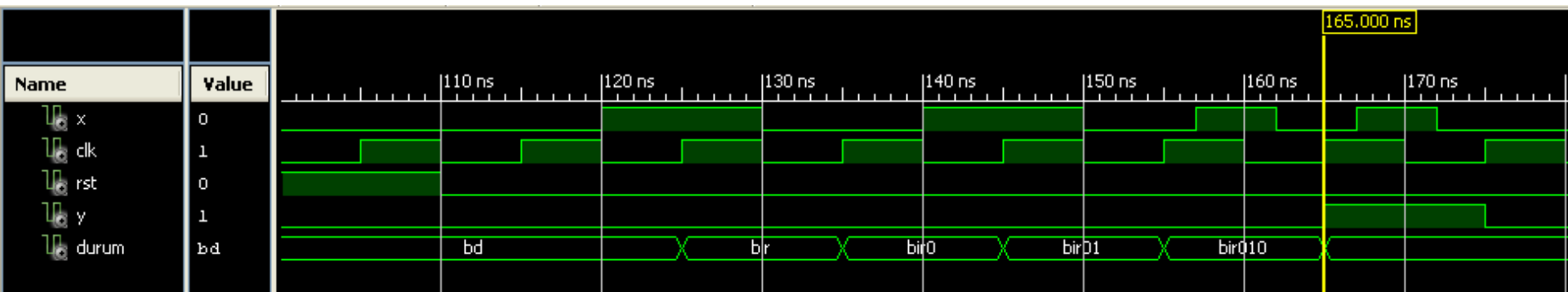
    reg [2:0] state;
    reg y;

    always @(posedge clk)
    begin
        if (rst) state = IS; y = 0;
        else
            case (state)
                IS:
                    y =0;
                    if(x) state = S_1;
                    else state = IS;
                S_1:
                    y =0;
                    if(x) state = S_1;
                    else state = S_10;
                S_10:
                    y =0;
                    if(x) state = S_101;
                    else state = IS;
                S_101:
                    y =0;
                    if(x) state = S_1;
                    else state = S_1010;
                S_1010:
                    y =1;
                    if(x) state = S_1;
                    else state = S_IS;
            endcase
        end
    endmodule
```

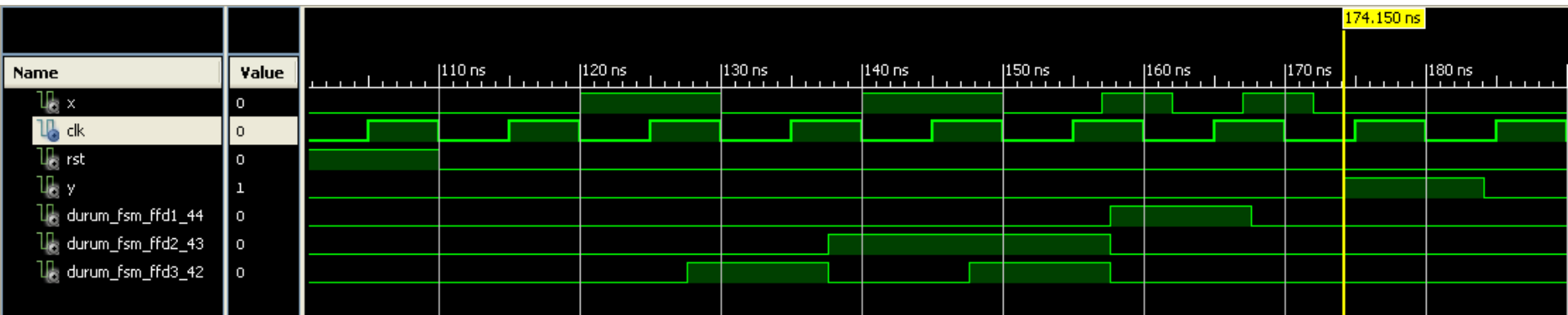
RTL Schematic



Timing Diagram



Ideal Case: Delay = 0



Not Ideal Case: Delay \neq 0