

Homework7

March 12, 2019

1 Srivani :Homework 7

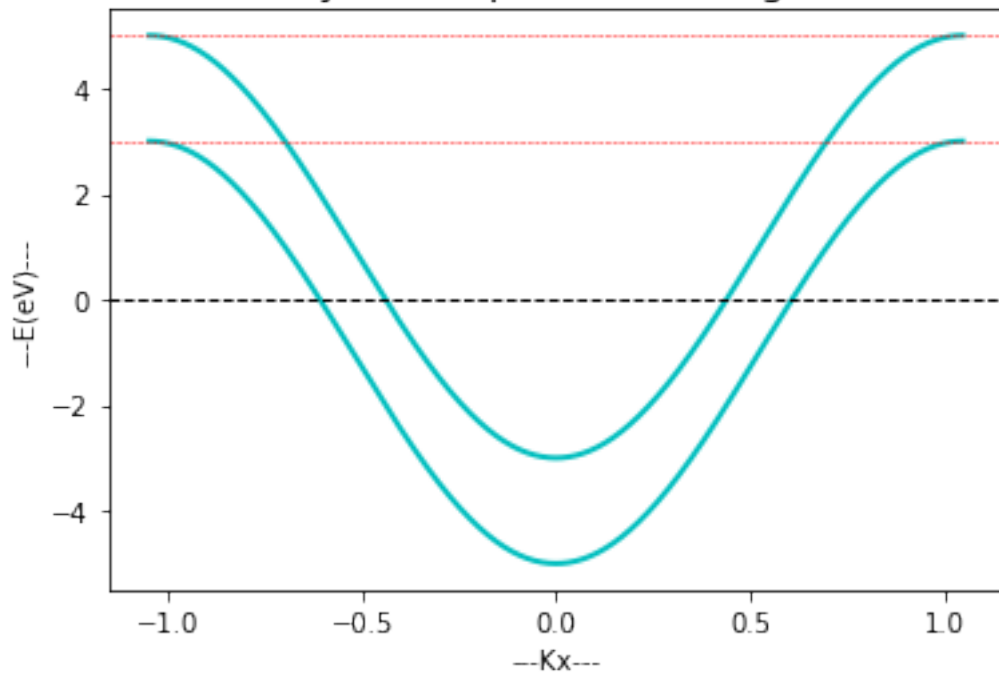
1.1 Problem 1. Band structure of two coupled linear chain of atoms separated by an horizontal interatomic distance of 3 angstroms.

1.1.1 a) Obtain the Hamiltonian and the eigenenergies analytically when one considers in-plane horizontal hopping $t_0 = -2$ eV and interchain vertical hopping terms or $t_1 = 1$ eV.

Hamiltonian and eigen energies analytically:

In [3]:

From the analytical expression of eigen values E_i :



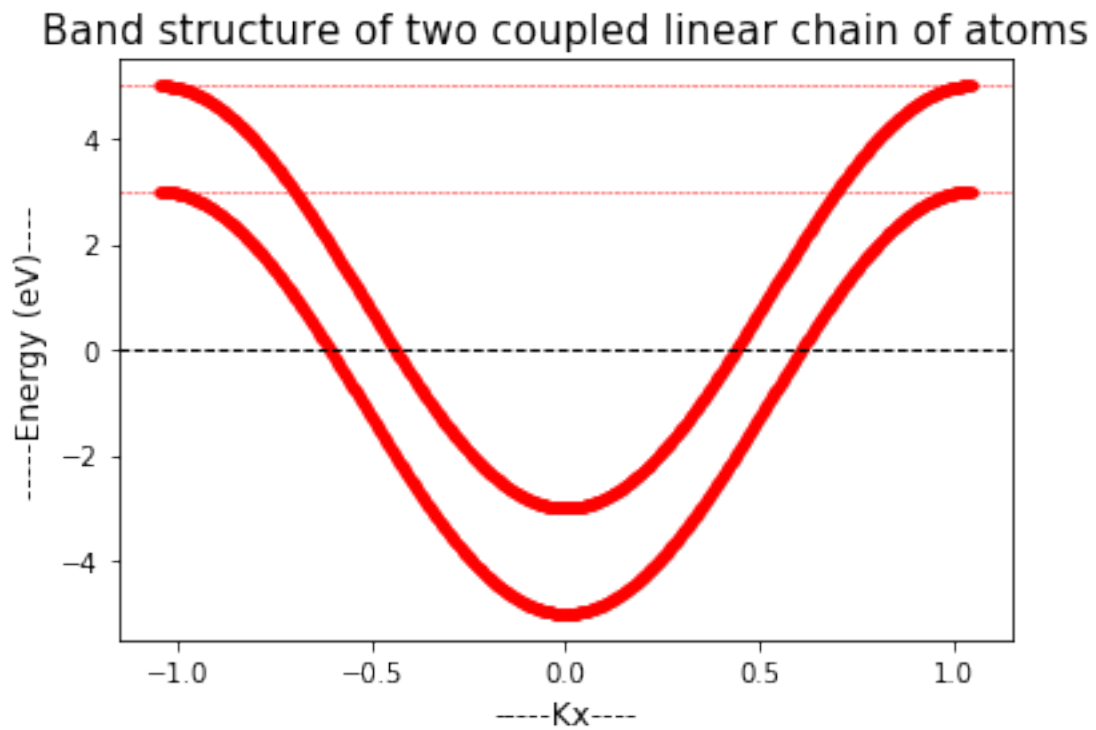
Hamiltonian and eigen energies Numerically:

In [2]:

```
[[ 4. -1.]  
 [-1.  4.]]
```

1.1.2 b) Plot the band structure.

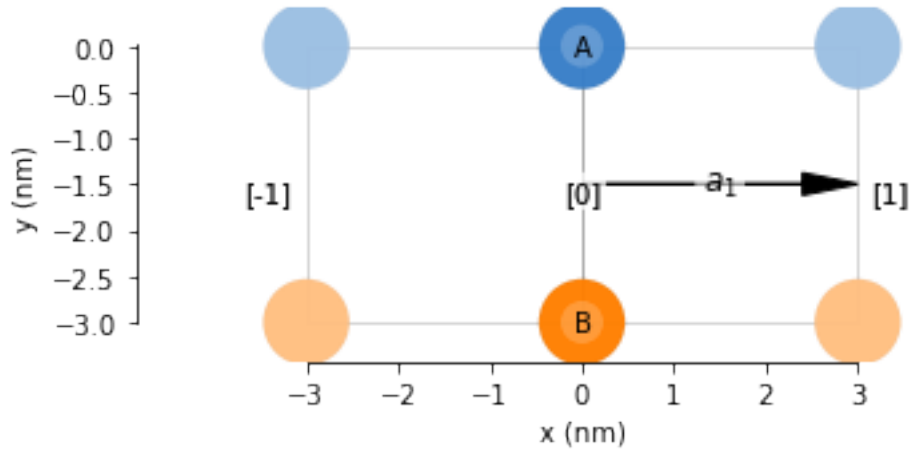
In [29]:



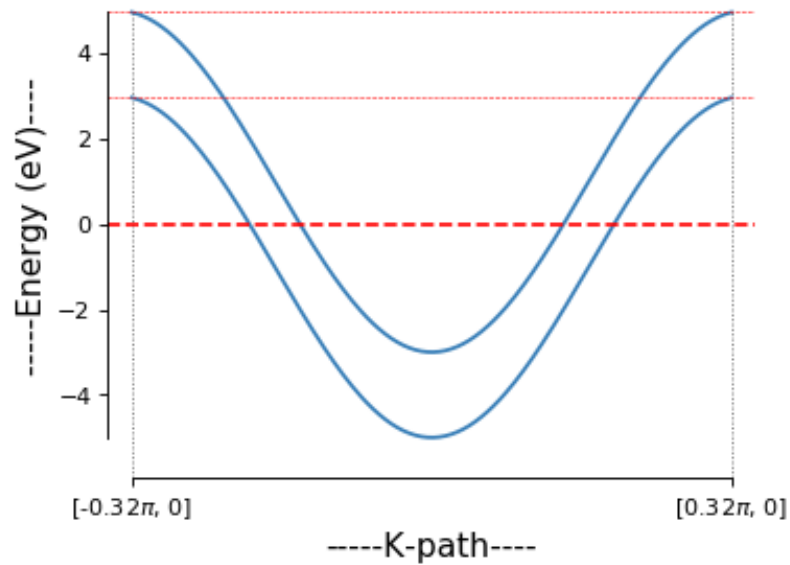
1.1.3 c) Solve the problem using pybinding.

In [30]:

Out[30]: <matplotlib.lines.Line2D at 0x7f898acef0b8>



Band structure of two coupled linear chain of atoms



1.2 2. Band structure of two coupled staggered linear chain of atoms

1.2.1 a) Obtain the Hamiltonian when one considers in-plane horizontal hopping term of $t_0 = -2$ eV and interchain vertical hopping terms or $t_1 = 1$ eV. The site potentials for blue and orange have respectively $V_A = -1$ eV and $V_B = 1$ eV.

In [9]:

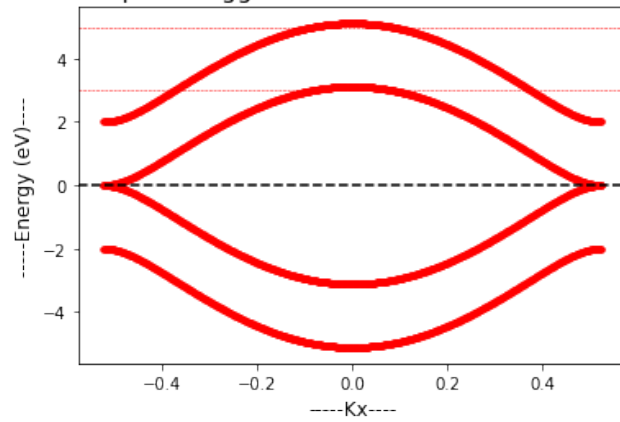
```
[[ -1.  4. -1.  0.]
 [ 4.  1.  0. -1.]]
```

```
[-1.  0. -1.  4.]
[ 0. -1.  4.  1.]]
```

1.3 b) Plot the band structure

In [10]:

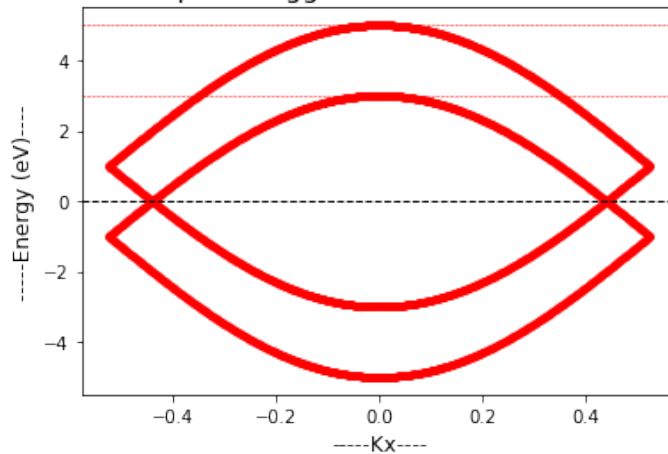
Band structure of two coupled staggered linear chain of atoms with staggered potentials



1.3.1 if $V_A = V_B = 0$

In [11]:

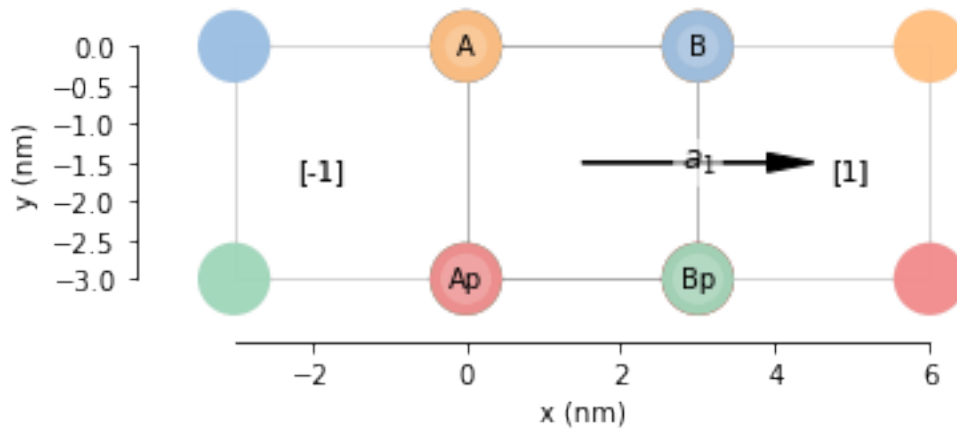
Band structure of two coupled staggered linear chain of atoms at $V_A = V_B = 0$ eV



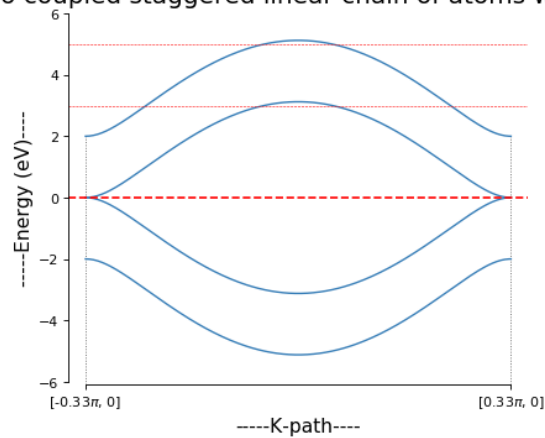
1.4 c) Solve the problem using pybinding.

In [28]:

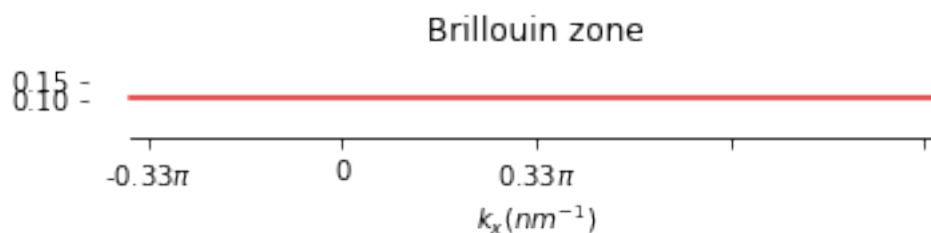
Out[28]: Text(0.5,1,'Band structure of two coupled staggered linear chain of atoms with staggered potentials



Band structure of two coupled staggered linear chain of atoms with staggered potentials



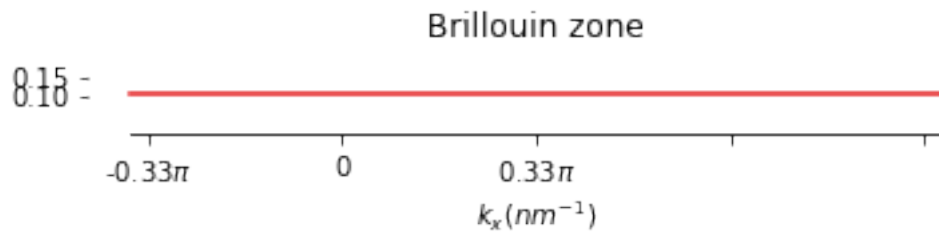
In [29]: `lattice.plot_brillouin_zone()
plt.title("Brillouin zone")
plt.show()`



In [2]:

Out[2]: Text(0.5,1,'Band structure of two coupled staggered linear chain of atoms at $V_A = V_B =$

```
In [3]: lattice.plot_brillouin_zone()
plt.title("Brillouin zone")
plt.show()
```



1.4.1 What happened to its Brillouin zone with respect to the non-staggered case? what if $V_A = V_B = 0$