

1) PDA to CFG

$$B_3 \Rightarrow A_1 A_3 A_2$$

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Soln

$N(M) \rightarrow$ lang. accepted by PDA by empty stack

$L(M) \rightarrow$ lang. accepted by PDA by final state

$$CFG \rightarrow G = (V, T, P, S)$$

$V \rightarrow$ set of variable of non-terminals

$T \rightarrow$ set of terminals

$P \rightarrow$ set of production

$S \rightarrow$ start symbol.

For V ,

we have to use $\underset{\text{state}}{\underbrace{[q, z, p]}}^{\text{stack}}$

$$\therefore V = \{ S, [q, z, p] \}$$

$$V = \{ S, [q_0, x, q_0], [q_0, x, q_1], [q_1, x, q_0], [q_1, x, q_1], [q_0, z, q_0], [q_0, z, q_1], [q_1, z, q_0], [q_1, z, q_1] \}$$

$T = \Sigma \rightarrow$ input symbol. $\gamma = \{0, 1\}$

for p we have to use transition.

p a Set of transitions or production

$$(i) \delta(q_0, 0, z_0) = (q_0, x, z_0)$$

we have to use $A \rightarrow \emptyset$

non terminal

terminal.

$$\begin{aligned} (q_0, 0, z_0) &= (q_0, x, z_0) \\ \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ x \quad [q_0, z_0, q_0] &\rightarrow 0 [q_0, x, q_0] [q_0, z_0, q_0] \\ [q_0, z_0, q_0] &\rightarrow 0 [q_0, x, q_1] [q_1, z_0, q_0] \text{ elim. } x \text{ in } z_0 \\ x [q_0, z_0, q_1] &\rightarrow 0 [q_0, x, q_0] [q_0, z_0, q_1] \\ [q_0, z_0, q_1] &\rightarrow 0 [q_0, x, q_1] [q_1, z_0, q_1] \end{aligned}$$

$$(ii) \delta(q_0, 0, x) = (q_0, x, x)$$

$$\begin{aligned} x \quad [q_0, x, q_0] &\rightarrow 0 [q_0, x, q_0] [q_0, x_0, q_0] \text{ eliminated } x \text{ in } x_0 \\ [q_0, x, q_0] &\rightarrow 0 [q_0, x, q_1] [q_1, x_0, q_0] \\ x [q_0, x, q_1] &\rightarrow 0 [q_0, x, q_0] [q_0, x_0, q_1] \\ [q_0, x, q_1] &\rightarrow 0 [q_0, x, q_1] [q_1, x_0, q_1] \end{aligned}$$

$$(iii) \delta(q_0, 1, x) = \{ (q_1, \epsilon) \} \quad [q_0, x, q_1] \rightarrow 1$$

$$[q_0, x, q_1] \rightarrow \epsilon$$

$$(iv) \delta(q_1, 1, x) = \{ (q_1, \epsilon) \} \quad [q_1, x, q_1] \rightarrow 1$$

$$x [q_1, x, q_1] \rightarrow 1 \quad [q_1, x, q_1] \rightarrow \epsilon$$

$$(v) \delta(q_1, \epsilon, x) = \{ (q_1, \epsilon) \} \quad [q_1, x, q_1] \rightarrow \epsilon$$

$$(vi) \delta(q_1, \epsilon, z_0) = \{ (q_1, \epsilon) \} \quad [q_1, z_0, q_1] \rightarrow \epsilon$$

$$x [q_1, z_0, q_1] \rightarrow \epsilon$$

Word has

for each state is

$$S \rightarrow [q_0, z_0, q_0]$$

initial state

initial state

$$q_1, q_2, q_3$$

$$S \rightarrow [q_0, z_0, q_1]$$

We have check the V elements with result we have

$$V = \{ S, [q_0, z_0, q_1], [q_0, \times q_1], [q_0 \times q_1, q_1], [q_1 \times q_1] \rightarrow 1, [q_1, \times q_1] \rightarrow \epsilon, [q_1, z_0, q_1] \rightarrow \epsilon \}$$

(4) Theorem ①.

Complex of recursion (log is recursion)