

# ECE 358 Assignment 4

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1. (a) (A) 1.2.3.0/30  
(B) 1.2.3.1/30  
(C) 1.2.3.2/30  
(D) 1.2.3.3/30  
(E) 1.2.3.4/30  
(F) 1.2.3.5/30  
(G) 1.2.3.6/30  
(H) 1.2.3.7/30  
(I) 10.0.0.0/16  
(J) 10.0.0.1/16  
(K) 1.2.3.8/30  
(L) 1.2.3.9/30  
(M) 1.2.3.10/30  
(N) 1.2.3.11/30  
(O) 10.0.0.2/16  
(P) 10.0.0.3/16

(b)	(i)	Destination	Next Hop	Interface
		1.2.3.4/30	myself	F
		1.2.3.0/30	myself	C
		0.0.0.0/0	1.2.3.1	C
(ii)		Destination	Next Hop	Interface
		1.2.3.8/30	myself	L
		1.2.3.0/30	myself	D
		0.0.0.0/0	1.2.3.1	D

2. During the first hop, the MTU is 1000 bytes, but the initial packet is  $20 + 1800 = 1820$  bytes. Therefore, after fragmentation,  $f_1$  will have 20 bytes of header and 976 bytes of payload since the offset has to be a multiple of 8 while maximizing the total packet size to less than 1000 bytes. Similarly,  $f_2$  will have a header of 20 bytes and payload of the remaining  $1800 - 976 = 824$  bytes (offset of 122).

Afterwards,  $f_1$  undergoes fragmentation again with MTU of 500 bytes. The first part,  $f_{1.1}$  will have 20 bytes for the header and 480 bytes for payload. The second part,  $f_{1.2}$  will have 20 bytes for the header and 480 bytes for payload (offset of 60). The third part,  $f_{1.3}$  will have 20 bytes for the header and  $976 - 480 - 480 = 16$  bytes for the payload (offset of 120).

In conclusion, the final fragments received at the destination in order of offset is:

- First fragment: ID = abcd, More fragments = 1, Fragment offset = 0, Total length = 500 bytes (480 bytes of payload)
  - Second fragment: ID = abcd, More fragments = 1, Fragment offset = 60, Total length = 500 bytes (480 bytes of payload)
  - Third fragment: ID = abcd, More fragments = 1, Fragment offset = 120, Total length = 36 bytes (16 bytes of payload)
  - Fourth fragment: ID = abcd, More fragments = 0, Fragment offset = 122, Total length = 844 bytes (824 bytes of payload)
3. (a) The header checksum is not necessarily the same, because the TTL field is decremented at each hop, so the header checksum is recomputed at each hop (hence, a different value than the initial checksum).
  - (b) I do not concur, even if an odd number of bits are flipped, it is not guaranteed to detect an error. A counter-example is 01 FF (checksum FE) because if you flip all nine 1-bits into 00, the checksum is still FE.
  - (c) Yes, the UDP checksum at the destination should match that of the source because UDP checksums are end-to-end and is not modified in transit (except when it passes through NAT).
  - (d) No, the converse is "if the MTU is supported, you will always get a response". This is not necessarily true, because there are other reasons for no response other than just a non-supported MTU (such as network congestion).
  4. Like the assignment suggested, we adopt two premises. (i) at the point in time the slide considers, for every  $a \in N'$ ,  $D(a) = d(a)$ . (ii) The path  $u \rightsquigarrow y$  in the picture,  $u \rightsquigarrow x \rightarrow y$ , is a cheapest path from u to y. Let's call this path  $p_1$ .

First we prove  $D(y) \leq \text{cost}(p_1)$ . By definition  $\text{cost}(p_1) = d(x) + c(x, y)$ . Since  $x \in N'$ , by premise (i),  $\text{cost}(p_1) = D(x) + c(x, y)$ . When x was added to  $N'$ , since y is adjacent to x, the algorithm performs  $D(y) = \min\{D(y), D(x) + c(x, y)\}$ , and since the only operations performed on  $D(y)$  is to assign it a min of its old value and another value,  $D(y)$  never increases. Thus  $D(y) \leq D(x) + c(x, y)$ , which combined with  $\text{cost}(p_1) = D(x) + c(x, y)$ , implies  $D(y) \leq \text{cost}(p_1)$ .

Suppose  $D(y) \neq d(y)$ . Since  $d(y)$  is the cheapest cost from u to y, and  $D(y)$  is the cost of a path from u to y,  $D(y) \geq d(y)$ . Since  $D(y) \neq d(y)$ ,  $D(y) > d(y)$ . Since

$d(y) < D(y)$  and  $D(y) \leq \text{cost}(p_1)$ , there must be a path from  $u$  to  $y$  that is cheaper than  $p_1$ . But premise (ii) says  $p_1$  is a cheapest path from  $u$  to  $y$ , contradiction. Therefore  $D(y) = d(y)$ .

5. First we observe  $\min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$  is at least an upper bound on  $d_x(y)$ . Let  $v_1$  be a neighbour of  $x$  that achieves the minimum in  $\min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$ , i.e.  $c(x, v_1) + d_{v_1}(y) = \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$ . Let  $v_1 \rightsquigarrow y$  be a minimum path from  $v_1$  to  $y$ , i.e.  $\text{cost}(v_1 \rightsquigarrow y) = d_{v_1}(y)$ . Observe  $x \rightarrow v_1 \rightsquigarrow y$  is a path from  $x$  to  $y$ . Moreover  $\text{cost}(x \rightarrow v_1 \rightsquigarrow y) = c(x, v_1) + \text{cost}(v_1 \rightsquigarrow y) = c(x, v_1) + d_{v_1}(y) = \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$ . Since  $d_x(y)$  is the cost of the cheapest path from  $x$  to  $y$ ,  $d_x(y) \leq \text{cost}(x \rightarrow v_1 \rightsquigarrow y) = \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$ .

Suppose  $d_x(y) = \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$  is not true, since we proved  $d_x(y) \leq \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$ , it must be the case  $d_x(y) < \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$ . Let  $p = x, v_1, v_2, \dots, v_k, y$  be a cheapest path from  $x$  to  $y$ , then  $\text{cost}(p) = c(x, v_1) + \text{cost}(v_1, v_2, \dots, v_k, y) < \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$ . In particular,  $c(x, v_1) + \text{cost}(v_1, \dots, v_k, y) < c(x, v_1) + d_{v_1}(y)$ , which in turn implies  $\text{cost}(v_1, \dots, v_k, y) < d_{v_1}(y)$ . Since  $v_1, \dots, v_k, y$  is a path from  $v_1$  to  $y$  and  $d_{v_1}(y)$  is the cost of the cheapest path from  $v_1$  to  $y$ , this is a contradiction. Therefore our assumption,  $d_x(y) = \min_{v \in \text{neigh}(x)} \{c(x, v) + d_v(y)\}$  is not true, must be false.

6. The number of nodes in  $G$ .

Let  $v_1, \dots, v_k$  be the cheapest path between  $v_1, \dots, v_k$ . First we observe  $\forall i \leq k, v_1, v_2, \dots, v_i$  is the cheapest path between  $v_1$  and  $v_i$ . Suppose its not, then there must be path  $v_1, w_1, w_2, \dots, v_i$  that's cheaper, but then  $v_1, w_1, w_2, \dots, v_i, v_{i+1}, v_{i+2}, \dots, v_k$  would be cheaper than  $v_1, v_2, \dots, v_k$ . Since we defined  $v_1, v_2, \dots, v_k$  as the cheapest path between  $v_1$  and  $v_k$ , this is a contradiction. Thus  $\forall i \leq k : v_1, v_2, \dots, v_i$  must be the cheapest path between  $v_1$  and  $v_i$ .

(For the following section, by "know" the cheapest path I mean know the next hop and total cost)

In an iteration, if  $v_i$  doesn't know its cheapest path from  $v_1$  yet, since  $v_i$  updates its guess of the cheapest from  $v_1$  path based only on its neighbours guess of cheapest path from  $v_1$ ,  $v_i$  would and would only learn its true cheapest path from  $v_1$  if in the last iteration  $v_{i-1}$  knows its true cheapest path from  $v_1$ . Since by the end of the first iteration, only  $v_1$  will know its distance for  $v_1$ , it takes a total of  $i$  iterations for  $v_i$  to learn its cheapest path from  $v_1$ . Thus it takes  $k$  iterations for  $v_k$  to learn its cheapest path from  $v_1$ .

It follows that the number of iterations for everyone to know their cheapest path from everyone else will be the number of nodes in the longest path between any two nodes where that path is also the cheapest path between the two nodes. Such a path in a weighted, connected, undirected graph  $G$  could contain all the nodes in  $G$ .

7.