

# Integer Arithmetic

- Addition

- Subtraction

Overflow! Solution → Fixed Precision  
(truncate extra bits)

★ for U  $0 \leq x, y \leq 2^w - 1$

if  $2^w \leq x+y < 2^{w+1}$   ~~$\times 2$~~

overflow happen, so bit  $w+1$   
would be removed, how?

$$x+y \bmod 2^w$$

what about signed? the same!

1, add

2, drop bit  $w+1$

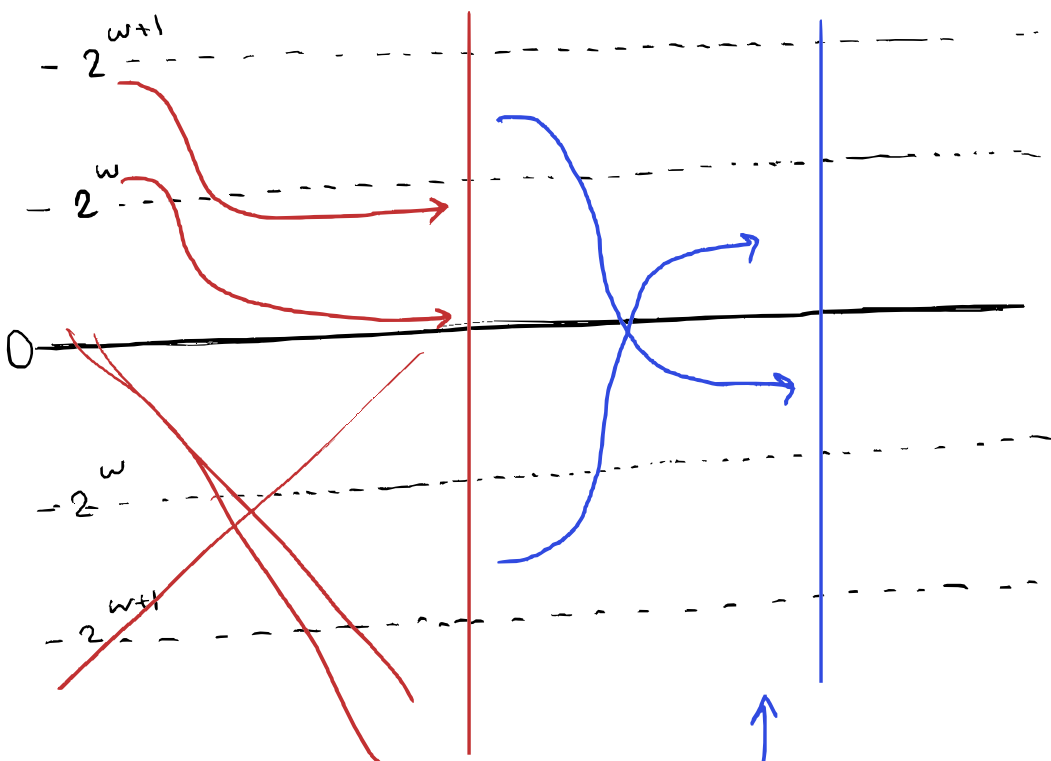
3, interpret as signed number

$$x+y = \text{int}_w((x+y) \bmod 2^w)$$

Overflow

U

T



how?

why?

Cost of ...

$+$   $\rightarrow$  1 to 2 cycle

$\times$   $\rightarrow$  5 to 10 cycle

$\div$   $\rightarrow$  20 to 39 cycle

\*  $x \cdot 2^k$  just  $k$  left shift  $<$

\*  $x \div 2^k$  just  $k$  logical right shift  $>$

$\searrow$  always floor towards 0  
for ~~negative~~ signed, values  
use arithmetic right shift  $\gg$

**Problem:** On signed value  $\gg$

round down! to solve this we add

"Bias"

How to find bias?